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Global Dynamic Modeling of a Transmission System

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NOMENCLATURE

A	=	rotor modal displacement of (X, θ_x)
A_c	=	casing modal displacement of $(X_c, X_{c\theta})$
B	=	rotor modal displacement of (Y, θ_y)
B_c	=	rotor modal displacement of $(Y_c, Y_{c\theta})$
$[C_b]$	=	bearing damping matrix
$[C_c]$	=	casing structure damping matrix
$[\bar{C}_b]$	=	$[\Phi]^T [C_b] [\Phi]$
$[\bar{C}_b]$	=	$[\Phi_c]^T [C_b] [\Phi_c]$
$[\bar{C}_c]$	=	$[\Phi_c] [C_c] [\Phi_c]$
D	=	rotor modal displacement of Z
D_t	=	rotor modal displacement of θ_t
D_c	=	casing modal displacement of $(Z_c, Z_{c\theta})$
$\{F(t)\}$	=	external and mass-imbalance excitations
$\{F_G(t)\}$	=	gear force
$\{F_c(t)\}$	=	force acting on casing structure
$\{F_s(t)\}$	=	shaft bow force = $[K_s] \{W_s\}$
$[G_A]$	=	rotor angular acceleration
$[G_v]$	=	gyroscopic
$[\bar{G}_A]$	=	$[\Phi]^T [G_A] [\Phi]$
$[\bar{G}_v]$	=	$[\Phi]^T [G_v] [\Phi]$
$[K_b]$	=	bearing stiffness

NOMENCLATURE (cont'd)

$[K_c]$ = casing structure **stiffness**

$[K_s]$ = shaft bow **stiffness**

$[K_A]$ = $\frac{1}{2} \{[K_{bx}] + [K_{by}]\}$

$[\bar{K}_b]$ = $[\Phi]^T [K_b] [\Phi]$

$[\bar{K}_A]$ = $[\Phi]^T [K_A] [\Phi]$

$[\bar{K}_c]$ = $[\Phi_c]^T [K_b] [\Phi_c]$

$[M]$ = mass matrix of **rotor**

$[M_c]$ = mass matrix of casing structure

$[W]$ = generalized displacement vector of **rotor**

$[W_c]$ = generalized displacement vector of casing

μ = friction coefficient between the **gear teeth surface**

α = angle of orientation

ω = critical speed of **rotor**

ω_c = critical speed of casing

GLOBAL DYNAMIC MODELING OF A TRANSMISSION SYSTEM

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ABSTRACT

This report outlines the work performed on global dynamic simulation and noise correlation of gear transmission systems at The University of Akron. The objective of this work is to develop a comprehensive procedure to simulate the dynamics of the gear transmission system coupled with the effects of gear box vibrations. The developed numerical model is benchmarked with results from experimental tests at NASA Lewis Research Center.

The modal synthesis approach is used to develop the global transient vibration analysis procedure used in the model. Modal dynamic characteristics of the rotor-gear-bearing system are calculated by the matrix transfer method while those of the gear box are evaluated by the finite element method (NASTRAN). A three-dimensional, axial-lateral coupled bearing model is used to couple the rotor vibrations with the gear box motion. The vibrations between the individual rotor systems are coupled through the non-linear gear mesh interactions. The global equations of motion are solved in modal coordinates and the transient vibration of the system is evaluated by a variable time-stepping integration scheme.

The relationship between housing vibration and resulting noise of the gear transmission system is generated by linear transfer functions using experimental data. A nonlinear relationship of the noise components to the fundamental mesh frequency is developed using the hypercoherence function. The numerically simulated vibrations and

predicted noise of the gear transmission system are compared with the experimental results from the gear noise test rig at **NASA Lewis Research Center**. Results of the comparison indicate that the global dynamic model developed can accurately simulate the dynamics of a gear transmission system.

1. INTRODUCTION

1.1 Introduction

Recently there has been an increase in the use of gear transmissions in both defense and commercial applications. The ever increasing speed and torque requirements of newer transmission systems often result in excessive noise and vibration at both the gear mesh and the gear box structure. Large vibrations in gear transmission systems result in excessive gear tooth wear and possible tooth root crack formation which, in turn, will lead to premature gear failure. In addition, excessive noise produced by a gear transmission in an aircraft, results in strained communications between crew and ground stations, and possible hearing loss for crew and passengers. Thus, in order to assure a quiet, smooth and safe operation of a gear transmission system it is necessary to understand the dynamics of the system under various operating conditions as well as the noise produced under these conditions.

To understand the global dynamics of the system during operation, the vibrational characteristics of the following major components need to be examined:

- i) The dynamics of the rotor bearing system - The dynamics of each rotor system are excited by its rotational torque, gear mesh dynamics, and imbalance effects. The dynamics of each individual rotor are coupled with other rotors through the gear mesh forces. Each rotor is also coupled with the gear box structure through the bearing support system.
- ii) The dynamics of the gear mesh system - The forces produced by the meshing of the gear teeth can be evaluated through the relative motion and the torque transfer between the two rotor systems.

- iii) The dynamics of the gear box system - The vibration of the gear box and its coupling effects with each rotor system is evaluated. In addition, the coupling effects of the gear box vibrations with the foundation motion through the ground support system is also examined.
- iv) The global system vibration - The determination of the global vibration of the system during various operating conditions is necessary.
- v) The relationships between noise and vibration - To understand the source of excessive noise, the relationships between noise and vibration of the system is required.

To further understand the present state of the art and the necessary effort to accomplish the above requirements, a brief description of previous work performed and the scope of this study are presented in the next two sections.

1.2 Review of Previous Work

In the past two decades, significant progress has been achieved in analytical/numerical simulations as well as experimental investigations of gear transmission systems. For both analytical and experimental studies, two major trends of investigations were developed, namely, i) the study of localized dynamics, stress and deformation, and thermal interactions between the two meshing gear teeth, and ii) the global dynamics and noise of the system due to the effects of the gear teeth interactions. An outline of the previous work in these areas is presented in the following paragraphs.

A large amount of work is reported in the literature on analyzing the localized effects of gear tooth interactions. In the area of experimental investigations, a significant amount of work was performed at NASA Lewis Research Center over the last ten years. These studies include the measurement of tooth stress [Oswald 1987, Krantz 1992], gear tooth lubricant and thermal effects [Akin 1989, Lewicki 1992, Townsend 1991a 1991b, El-

Bayoumy 1989], gear tooth friction [Rebbechi 1991], and gear tooth material and fatigue [Townsend 1979, 1988]. Some analytical studies include gear surfaces stresses, lubricant cooling effect [El-Bayoumy 1989], gear tooth surface profile investigations [Kittur 1989, Lin 1988, Litvin 1991a, 1991b] and the dynamics of bevel gears [Handschuh 1991a, 1991b, Mark 1987]. The above outline represents only a small portion of the literature on the state of the art in gear tooth analysis.

In comparison, there is much less available in the literature on the study of the global dynamics of a transmission system. There have been some studies on the vibration analysis of a single gear stage [August 1982, Choy 1988, Cornell 1981, Lin and Houser 1987, Mark 1982, Pike 1987]. Some work has been reported on multistage gear dynamic analysis [Choy 1990, David 1987, Ozguven and Houser 1988]. However, only limited work is reported in the area of experimental analysis of the global dynamics of a transmission system [Mitchell 1986, Oswald 1992]. Similarly, there is limited work on the comparison of experimental results with analytical studies [Choy 1987, 1991, Singh 1990]. Reported research is even more limited in the areas of noise analysis and noise prediction in gear transmission systems. Some work on predicting and verifying the noise field of a gear transmission system has only recently been reported (Seybert 1991, Oswald 1992).

1.3 Scope and Objectives

As illustrated above, with the limited amount of literature available on modeling gear transmission systems, a comprehensive analytical and experimental procedure is necessary for the complete understanding of the dynamics and resulting noise of a transmission system. In this project, a numerical model is developed to simulate the vibrations of a multistage gear

system. The ultimate goal in this project is to develop a methodology to predict the noise and vibration of a gear transmission system.

During the early stages of this work several main objectives were established in an effort to guide the development of the global model in the direction of achieving the project goal. These main objectives are:

- 1) The gear/rotor part of the model should be capable of simulating multistage gear systems, variable rotor geometries, shaft residual bow, mass imbalances, and non-linear stiffness and friction of the gear tooth.
- 2) The bearing support part of the model must be capable of coupling the dynamics of the gear/rotor system with the housing dynamics in both the in-plane and out-of-plane directions.
- 3) The finite element model of the housing must accurately predict the major vibration modes of the actual housing. Experimental results will be used to verify and improve the model.
- 4) A relationship needs to be established between the housing vibrations and resulting noise production to complete the gear initiated vibration/noise transmission path.

The key to achieving the ultimate goal of developing a global dynamic model that accurately predicts the noise and vibration of a transmission system was to successfully meet each of the main objectives presented above. Meeting these objectives required comparing and validating each part of the model, and the total model, with experimental data during each stage of development of the global dynamic model.

The remaining sections of this report document the details of developing the global model and verifying/refining the model with experimental data from the gear noise test rig at NASA Lewis Research Center.

2. FORMULATION OF GENERALIZED EQUATIONS OF MOTION

2.1 Dynamics of Rotor-Bearing-Gear System

The equations of motion for each individual gear-shaft system can be written in matrix form [Choy 1991] as:

$$\begin{aligned} [M]\{\ddot{W}\} + [G_v]\{\dot{W}\} + [G_A]\{\dot{W}\} + [C_b]\{\dot{W} - \dot{W}_c\} \\ + [K_b]\{W - W_c\} + [K_r]\{W - W_r\} = \{F(t)\} + \{F_G(t)\} \end{aligned} \quad (2.1)$$

where the generalized displacement vector $\{W\}$ consists of the three displacement vectors, X, Y, Z, with the corresponding lateral θ_x , θ_y , and torsional θ_t rotational vectors as

$$\{W\} = \begin{Bmatrix} (X) \\ (\theta_x) \\ (Y) \\ (\theta_y) \\ (Z) \\ (\theta_t) \end{Bmatrix} \quad (2.2)$$

The equations of motion shown in Eq. (2.1) includes the effects of a) inertia, $[M]$, b) gyroscopic forces $[G_v]$, c) rotor angular acceleration, $[G_A]$, d) bearing direct and cross-coupling damping, $[C_b]$, e) bearing axial and lateral cross-coupling stiffness, $[K_b]$, [LIM 1990], f) casing vibration, $\{W - W_c\}$, g) shaft residual bow, $\{W - W_r\}$, h) external and mass-imbalance excitations, $\{F(t)\}$, and i) nonlinear gear forces through gear mesh coupling

$\{F_G(t)\}$. For a multiple gear-shaft system, the equations of motion presented in Eq. (2.1) will be repeated for each individual shaft. The motions of the individual shafts are coupled to each other through the gear mesh forces, and the shaft motions are coupled to the casing through the bearing stiffness $[K_b]$ and damping $[C_b]$.

2.2 Dynamics of Gear Box Structure

The equations of motion for the casing can be written as:

$$[M_c]\{\ddot{W}_c\} + [C_b]\{\dot{W}_c - \dot{W}\} + [K_b]\{W_c - W\} + [C_c]\{\dot{W}_c\} + [K_c]\{W_c\} = \{F_c(t)\} \quad (2.3)$$

where $\{W_c\}$ represents the generalized displacement vector of the casing structure,

$$\{W_c\} = \begin{Bmatrix} (X_c) \\ (X_{c\theta}) \\ (Y_c) \\ (Y_{c\theta}) \\ (Z_c) \\ (Z_{c\theta}) \end{Bmatrix} \quad (2.4)$$

The equations of motion of the casing structure, given in Eq. (2.3), include the effects of concentrated mass $[M_c]$, structure members damping $[C_c]$, stiffness of the structural members $[K_c]$, and casing-to-rotor bearing stiffness $[K_b]$ and damping $[C_b]$. The effects of foundation motion are incorporated into the system through the forcing function $F_c(t)$.

2.3 Coupled System Dynamics

The dynamics between each individual rotor system and the casing structure are coupled through the bearing support and the gear mesh systems. Three models are used to couple the dynamics of the system, namely; i) the 3-D lateral-axial bearing, ii) the normal and frictional gear mesh forces, and iii) the casing-ground support system.

3-D Lateral-Axial Bearing Model

This model is used to develop two types of coupling in the system dynamics. a) The relative motion between the rotor and the casing structure at the bearing locations will be used to generate the coupling forces. b) The dynamics between the lateral and axial motion at the bearing supports will be coupled due to the effects of the bearing configuration.

In this simulation, a previously developed bearing model [Singh and Lim 1990] is used. A six degrees of freedom ball bearing stiffness matrix $[K_{bi}]$ is used for each bearing support location, where

$$[K]_{bi} = \begin{bmatrix} k_{xx} & k_{x\theta_x} & k_{xy} & k_{x\theta_y} & k_{xz} & 0 \\ & k_{\theta_x\theta_x} & k_{\theta_x y} & k_{\theta_x\theta_y} & k_{\theta_x z} & 0 \\ & & k_{yy} & k_{y\theta_y} & k_{yz} & 0 \\ \text{symmetric} & & & k_{\theta_y\theta_y} & k_{\theta_y z} & 0 \\ & & & & k_{zz} & 0 \\ & & & & & 0 \end{bmatrix}_{bi} \quad (2.5)$$

Note that the bearing stiffness matrix generated not only couples the displacement in all three directions, it also provides coupling between the moments generated due to the bending of the rotor. In this analysis, the bearing stiffness matrix generated for each bearing is incorporated into the global bearing stiffness matrix $[K_b]$ in equations 2.1 and 2.3.

Gear Mesh Normal and Frictional Forces

The gear mesh forces are evaluated using a previously developed methodology [Boyd and Pike 1985]. The procedure evaluates the nonlinear gear mesh stiffness $[K_g]$ for a variety of multi-mesh epicyclic gear systems with internal, buttress, or helical tooth forms. The major assumptions used in this procedure are as follows:

1. The flexible ring gear rim and carrier flexibility option is assumed to be only along the line-of-action of each respective gear mesh.
2. The static output torque is assumed to be divided evenly among either the planet carrier segments or the ring gear rim segments, depending on the type of planetary system.
3. Any radial component of motion is assumed to be secondary to the tooth-pair motion along the line-of-action.
4. The damping of carrier and ring rim segments is assumed to be insignificant relative to the tooth-pair mesh damping.

The nonlinear gear mesh forces for the Kth individual gear-shaft system, Fig. 2.1, using nonlinear gear stiffness [Boyd 1989] and gear tooth friction [Rebbechi 1991], are given as:
x-force

$$F_{Gxk} = \sum_{i=1, i \neq k}^n K_{iki} [-R_{ci} \Theta_{ci} - R_{ck} \Theta_{ck} + (X_{ci} - X_{ck}) \cos \alpha_{ki} + (Y_{ci} - Y_{ck}) \sin \alpha_{ki}] [\cos \alpha_{ki} + (\text{sign})(\mu)(\sin \alpha_{ki})] \quad (2.6)$$

y-force

$$F_{Gyk} = \sum_{i=1, i \neq k}^n K_{iki} [-R_{ci} \Theta_{ci} - R_{ck} \Theta_{ck} + (X_{ci} - X_{ck}) \cos \alpha_{ki} + (Y_{ci} - Y_{ck}) \sin \alpha_{ki}] [\sin \alpha_{ki} + (\text{sign})(\mu)(\cos \alpha_{ki})] \quad (2.6)$$

and torsional

$$F_{Gtk} = \sum_{i=1, i \neq k}^n R_{ck} \{K_{iki} [(-R_{ci} \Theta_{ci} - R_{ck} \Theta_{ck}) + (X_{ci} - X_{ck}) \cos \alpha_{ki} + (Y_{ci} - Y_{ck}) \sin \alpha_{ki}]\} \quad (2.8)$$

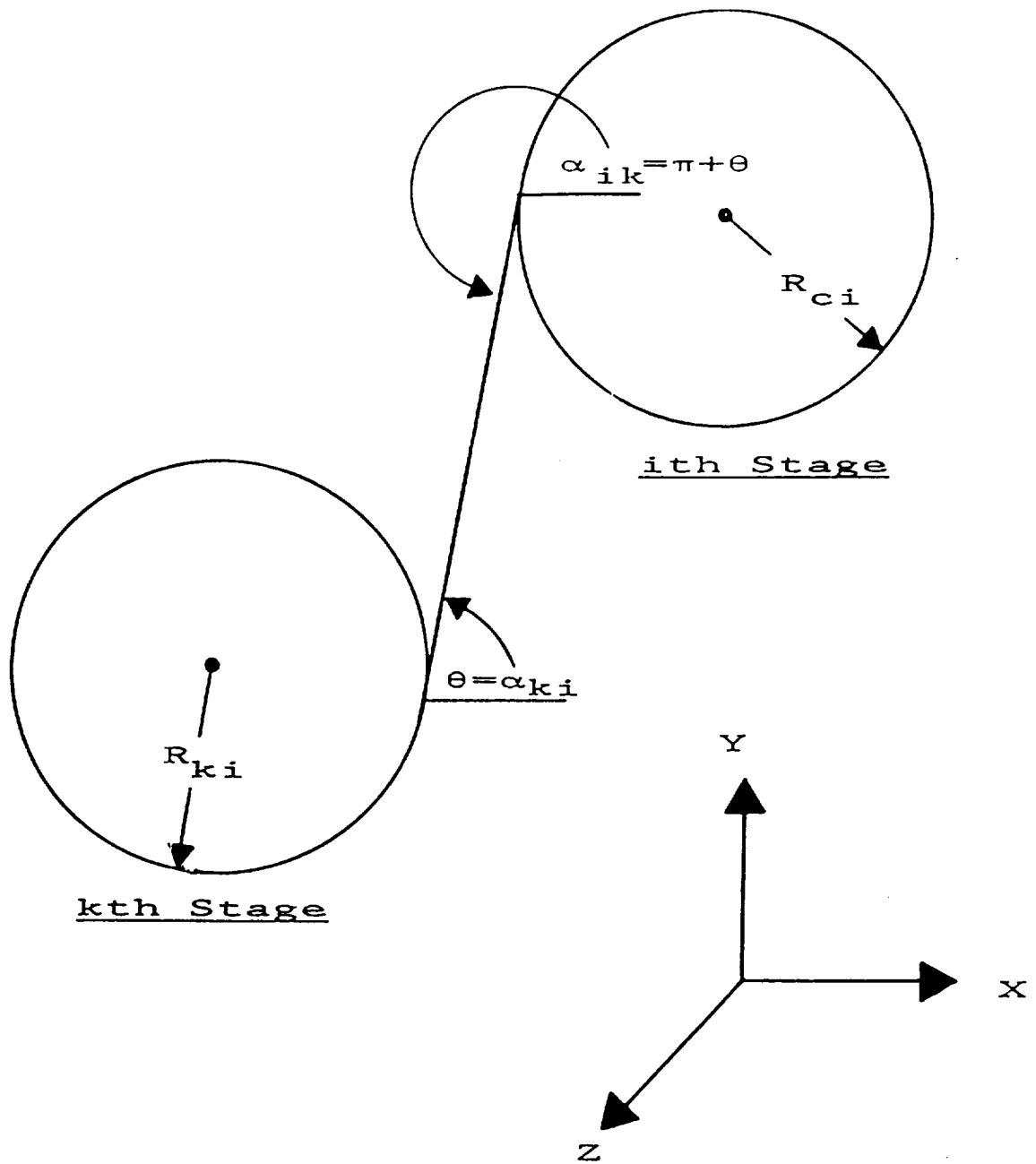


Figure 2.1 Gear Mesh Geometry for Force Calculation

where μ is the coefficient of friction between the gear tooth surface and "SIGN" is the unity sign function to provide the sign change when the mating teeth pass the pitch point [Rebbechi 1991].

Effects of Foundation Motion

The effects of foundation motion are incorporated as part of the forcing function input $F_c(t)$ in the casing equation (Eq. 2.3). The forcing function due to foundation motion can be calculated as the product of the support stiffness $[K_p]$ and the relative motion between the casing and ground at the support locations as

$$\{F_c(t)\} = [K_p] \{W_c - W_g\} \quad (2.9)$$

where W_g is the vector for ground displacement as a function of time.

3. FORMULATION OF MODAL SYNTHESIS PROCEDURE

The generalized equations of motion developed in the previous chapter are solved through the modal synthesis procedure. Using the undamped modes for both the rotor-bearing-gear system and the gear box structure, the generalized equations of motion for the system are transformed into the corresponding modal coordinates. This procedure will significantly reduce the degrees of freedom of the system, and also provide an estimate of the modal excitations at the various modes. A detailed description of the procedure is outlined in the following sections.

3.1 Modal Characteristics of Rotor-Bearing-Gear Systems

For each rotor-bearing-gear system, the modal characteristics are evaluated using the matrix-transfer method [Choy 1988, 1989, 1991]. In this analysis, the rotor system is modelled by sections of massless shafts and concentrated masses. For simplicity in computation, the following assumptions are used in this procedure.

- i) The complexity in the rotor geometry is modelled by sections of massless shafts with concentrated mass attached at both ends.
- ii) Only the direct stiffness of the bearing is incorporated in the calculation of the undamped natural frequencies and mode shapes. The cross-coupling stiffness and damping terms are cast into the right-hand-side of the equation as a forcing function.
- iii) An averaged stiffness for both x and y direction is used and assures a circular symmetric system.

- iv) Gyroscopic moments are not considered in the modal calculations and will be incorporated as forcing functions in the transient calculations. However, rotational inertia effects are included in this procedure.

A detailed description of the equations used in this matrix transfer procedure is given in Appendix A. The natural frequencies and corresponding mode shapes calculated for each rotor system, are incorporated into the modal equation described in the later sections. The undamped modal characteristics evaluation procedure is installed as part of the main computer code, with the undamped modal characteristics generated automatically during each run.

3.2 Modal Characteristics of Gear Box Structure

In evaluating the modal characteristics of the gear box structure, a finite element model is used. The NASTRAN FE code is used with the following options:

- i) Rectangular plate and beam elements are used to model the basic structure of the gear box.
- ii) Boundary elements are used to model the ground supports of the gear box with corresponding boundary support conditions.
- iii) Natural frequencies and 3-dimensional orthonormal mode shapes are evaluated and used as input for the modal synthesis program.
- iv) A description of the input/output with the NASTRAN code is given in Appendix B.

3.3 Orthogonality of Modal Shapes

For each individual rotor system, the equation of motion for the undamped system is:

$$[M]\{\ddot{W}\} + [[K_s] + [K_A]]\{W\} = 0 \quad (3.1)$$

with the average bearing support stiffness from the x-y direction [Choy 1991] given as:

$$[K_A] = \frac{1}{2} \{[K_{bx}] + [K_{by}]\} \quad (3.2)$$

The orthogonality condition for the orthonormal modes $[\Phi]$ are

$$[\Phi]^T [M] [\Phi] = [I] \quad (3.3)$$

and

$$[\Phi]^T [K_s + K_A] [\Phi] = [\omega^2] \quad (3.4)$$

Similarly, a set of orthogonality conditions can be derived for the casing equation of

$$[M_c]\{\ddot{W}_c\} + [C_c]\{\dot{W}_c\} + [K_c]\{W_c\} = 0 \quad (3.5)$$

with the orthonormal mode $[\Phi_c]$ such that

$$[\Phi_c]^T [M_c] [\Phi_c] = [I] \quad (3.6)$$

$$[\Phi_c]^T [C_c] [\Phi_c] = [\bar{C}_c] \quad (3.7)$$

$$[\Phi_c]^T [K_c] [\Phi_c] = [\omega_c^2] \quad (3.8)$$

These orthogonal conditions are used in the modal transformation presented in the next section.

3.4 Modal Transformation of Equations of Motion

The modal transformation procedure can be developed by assuming that the generalized displacements can be represented by a linear combination of the modal characteristics, such that for the rotor system

$$\{W\} = \begin{Bmatrix} [\Phi_x] \{A\} \\ [\Phi_{x\theta}] \{A\} \\ [\Phi_y] \{B\} \\ [\Phi_{y\theta}] \{B\} \\ [\Phi_z] \{D\} \\ [\Phi_t] \{D_t\} \end{Bmatrix} \quad (3.9)$$

where A, B, D, and D_t are the time dependent modal excitation functions, and $[\Phi_x]$, $[\Phi_{x\theta}]$, $[\Phi_y]$, $[\Phi_{y\theta}]$, $[\Phi_z]$, $[\Phi_t]$ are the matrix containing the orthonormal modes of the corresponding rotor system. Similarly, for the casing structure,

$$\{W_c\} = \begin{Bmatrix} [\Phi_{cx}] \{A_c\} \\ [\Phi_{cx\theta}] \{A_c\} \\ [\Phi_{cy}] \{B_c\} \\ [\Phi_{cy\theta}] \{B_c\} \\ [\Phi_{cz}] \{D_c\} \\ [\Phi_{cz\theta}] \{D_c\} \end{Bmatrix} \quad (3.10)$$

Pre-multiplying the generalized equation of motion by the orthonormal modes, and using the orthogonality condition developed in the previous section, the equation for the rotor system (2.1) can be transformed into the modal coordinates as:

$$\begin{aligned} [I] \{\ddot{Z}\} + [\bar{G}_v] \{\dot{Z}\} + [\bar{G}_A] \{Z\} + [\bar{C}_b] \{\dot{Z}\} - [\bar{K}_b - \bar{K}_A] \{Z\} + [\Phi]^T [C_b] [\Phi_c] \{\dot{Z}_c\} \\ + [\omega^2] \{Z\} - [\Phi]^T [K_b] [\Phi_c] \{Z_c\} = [\Phi]^T \{F(t) + F_G(t) + F_r(t)\} \end{aligned} \quad (3.11)$$

and for the casing (Eq. 2.3) as

$$\begin{aligned} [I] \{\ddot{Z}_c\} + [\bar{C}_c] \{\dot{Z}_c\} + [\omega_c^2] \{Z_c\} + [\bar{K}_b] \{Z_c\} + [\bar{C}_b] \{\dot{Z}_c\} \\ - [\Phi_c]^T [K_b] [\Phi] \{Z\} - [\Phi_c]^T [C_b] [\Phi] \{\dot{Z}\} = [\Phi_c]^T \{F_c(t)\} \end{aligned} \quad (3.12)$$

where

$$\{Z\} = \begin{Bmatrix} \{A\} \\ \{B\} \\ \{D\} \\ \{D_r\} \end{Bmatrix} \quad \{Z_c\} = \begin{Bmatrix} \{A_c\} \\ \{B_c\} \\ \{D_c\} \end{Bmatrix} \quad (3.13)$$

Note that in equations (3.11 and 3.12) the modal acceleration terms \ddot{Z} and \ddot{Z}_c for the rotor and the casing are uncoupled and can be evaluated by solving the set of simultaneous matrix equations.

4. NUMERICAL SOLUTION PROCEDURES

To evaluate the transient dynamics of the rotor-casing system, the modal equations (3.11 and 3.12) are rewritten as:

$$[I]\{\ddot{Z}\} = [\bar{G}_v]\{\dot{Z}\} - [\bar{G}_d]\{Z\} - [\bar{C}_b]\{\dot{Z}\} + [\bar{K}_b - \bar{K}_d]\{Z\} - [\Phi]^T[C_b][\Phi_c]\{\dot{Z}_c\} - [\omega^2]\{Z\} + [\Phi]^T[K_b][\Phi_c]\{Z_c\} + [\Phi]^T\{F(t) + F_G(t) + F_s(t)\} \quad (4.1)$$

and for the casing

$$[I]\{\ddot{Z}_c\} = [\bar{C}_c]\{\dot{Z}_c\} - [\omega_c^2]\{Z_c\} - [\bar{K}_b]\{Z_c\} - [\bar{C}_b]\{\dot{Z}\} + [\Phi_c]^T[K_b][\Phi]\{Z\} + [\Phi_c]^T[C_b][\Phi]\{\dot{Z}\} + [\Phi_c]^T\{F_c(t)\} \quad (4.2)$$

Using the appropriate initial conditions for the modal velocity $\{\dot{Z}\}$ and displacement $\{Z\}$, the modal accelerations $\{\ddot{Z}\}$ can be solved. The solution procedure for the algorithm is given as follows.

1. Input Initial Conditions to Calculate Modal Accelerations
2. Use Variable Time-stepping Integration Scheme to Evaluate Modal Velocity and Displacement at next time step.
3. Calculate Velocity and Displacement in Generalized Coordinates.

4. Calculate Nonlinear Gear Mesh Forces due to Relative Motion Between the Two Gears.
5. Calculate Bearing Forces due to Relative Motion Between the Rotor and the Casing.
6. Calculate Modal Bearing and Gear Forces.
7. Repeat from Step No. 2.

5. EXPERIMENTAL STUDIES

Test results from the gear noise test rig, Fig. 5.1, at NASA Lewis Research Center were used in this study to refine and validate the global dynamic model developed. Three phases of experimental studies were performed, namely; i) the determination of static modal characteristics using the impulse-response technique; ii) the transient vibration of both rotor and the gear box structure during operation; and iii) the noise production at the gear box surfaces. An outline of the experimental studies are presented below:

5.1 Evaluation of Experimental Modal Characteristics

The gear transmission system used in this test is shown in Fig. 5.2. The gear system consists of a pair of identical parallel axis gears supported by rolling element bearings. The surface of the gear box structure is segmented into 116 nodal points. The impulse-response technique was used to determine the transfer functions of the system. An impact hammer was applied at various nodes on the surface of the gearbox. Three accelerometers, one on a surface in the x-direction, another in the y-direction, and the last in the z-direction, were used to obtain the resulting responses from the impacts. Natural frequencies and their corresponding mode shapes excited during the experiment were evaluated using a two channel dynamic signal analyzer with a PC-based modal software. The modal characteristics

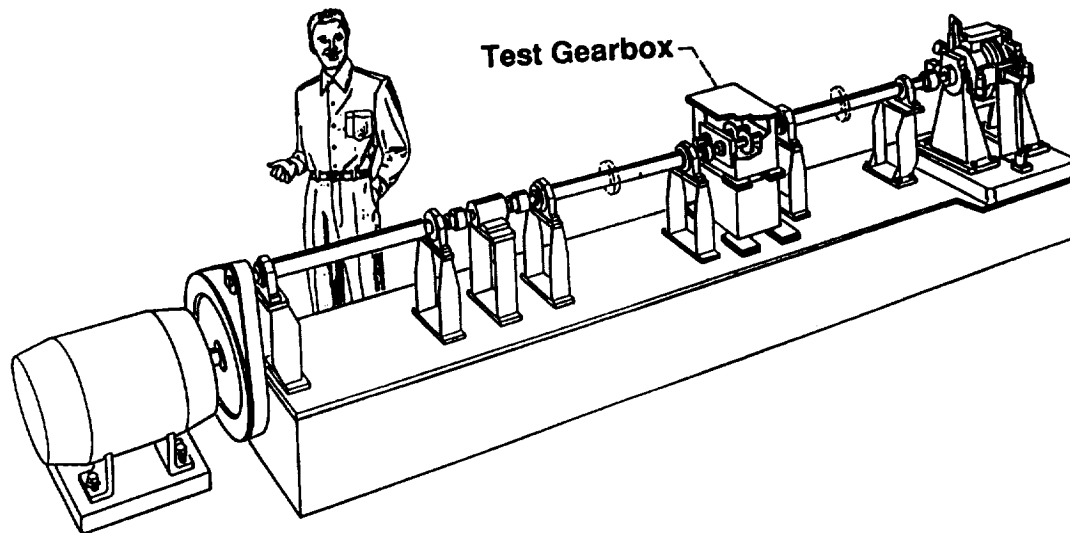


Figure 5.1 Schematic of NASA Gear Noise Rig

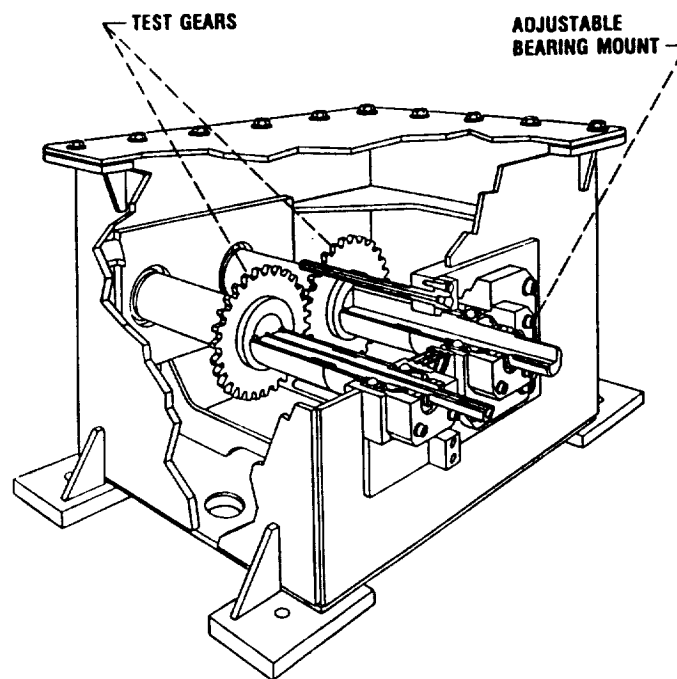


Figure 5.2 Drawing of NASA Test Gearbox

found during the experiment were compared to those generated by the numerical model for verification purposes, as well as for the selection of numerically modelled mode shapes.

5.2 Experimental Investigations of System Dynamics

To study the dynamics of the system during operation, a 150kW(200 Hp) variable speed electric motor is used to power the rig at one end. An eddy-current dynamometer is used for power absorbing at the opposite end. The parameters of the test gears are given in Table 5.1. During this test, several accelerometers were placed on the x, y, and z surfaces of the gear box to monitor the vibrations of the gear box structure. In addition, two sets of non-contacting proximitors were placed inside the gear box at locations next to the gear mesh to monitor the vibrations of the two rotor systems. The vibration signals of the gear box surface and the rotors were recorded over a range of operating speeds from 1500 to 6000 rpm. A two channel dynamic signal analyzer was used to compute the frequency spectra (waterfall diagram) of the vibrations of the gear box in x, y, and z directions. The frequency spectra for the lateral vibrations of the rotor at the gear locations were also computed. The results of this phase of the experimental work was compared to those from the numerical model for verification of the numerical procedure and improvement of the numerical modelling of the gear transmission components (bearing model, gear mesh model, rotor model, gear box model, etc.).

5.3 Experimental Investigations of Gear Box Noise

To investigate the relationship between the gear box vibration and the noise, a special noise test program was introduced. A special set of identical parallel axis gears (25 tooth) were used in this test. While the vibration measurement set-up is very similar to those mentioned in the previous section (5.2), two additional acoustic microphones were used in

this experiment. Both microphones were placed over the top cover of the gear box with one in the vertical direction and the other at a 45 degree angle from the vertical. Rotor vibration, gear box vibration, and the resulting noise was obtained while operating at various running speeds. A correlation between the gear box vibrations and the noise level was performed in the frequency domain using linear transfer and cross-correlation functions. The Nonlinear Hypercoherence function [Jong 1986] developed at NASA Marshall Space Flight Center was also used to generate a relationship between the noise and the vibration data in order to develop a noise prediction algorithm for the global dynamic model.

TABLE 5.1 - TEST GEAR PARAMETERS

Gear Type.	Standard involute, full-depth tooth
Number teeth	28
Module, mm (diametral pitch in. ⁻¹).	3.174 (8)
Face width, mm (in.)	6.35 (0.25)
Pressure angle, deg	20
Theoretical contact ratio	1.64
Driver modification amount, mm (in.)	0.023 (0.0009)
Driven modification amount, mm (in.)	0.025 (0.0010)
Driver modification start, deg	24
Driven modification start, deg	24
Tooth-root radius, mm (in.).	1.35 (0.053)
Gear quality	AGMA class 13
Nominal (100 percent) torque, N-min(in.-lb).	71.77 (635.25)

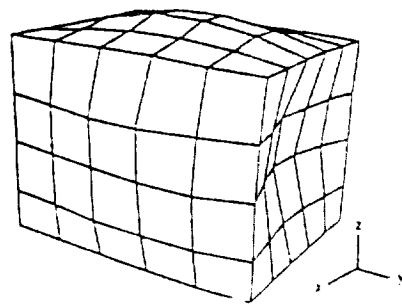
6. CORRELATION AND BENCHMARKING OF SYSTEM DYNAMICS BY NUMERICAL PROCEDURES WITH EXPERIMENTAL RESULTS

This chapter presents the correlation between the numerical simulations of the dynamics of the gear transmission system with the experimental results. Three major phases of the system dynamics were examined, namely; i) the gear box modal characteristics, ii) the dynamics of the rotor-gear systems, and iii) the vibration of the gear box structure. A detailed comparison and benchmarking of the results are given in the following sections.

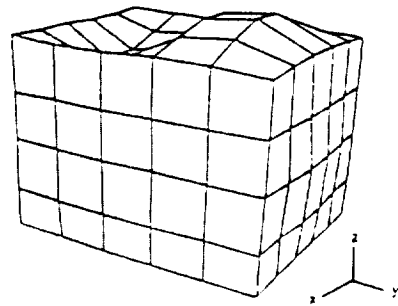
6.1 Gear Box System modal Characteristics

To experimentally determine the modal characteristics of the gear box structure, the impact testing technique described in the previous chapter was applied to obtain the natural frequencies and mode shapes of the system. During this test, a total of 8 major vibratory modes were excited between a frequency range of 0 to 3000 Hz. The excited natural frequencies and their corresponding mode shapes are shown in Fig. 6.1.

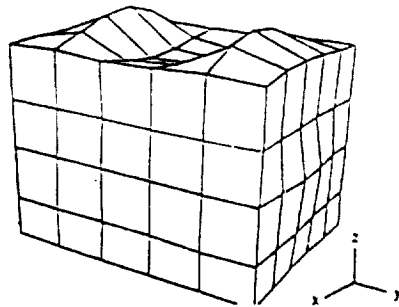
The experimentally obtained modes, shown in Fig. 6.1, represent the major vibration modes of the gear noise rig in the 0 to 3 kHz region. Although these modal frequencies are only a small part of the total modes of the system, they represent a major part of the total global vibration of the system. In order to produce an accurate analytical simulation of the test gearbox, a similar set of modes were generated using a finite element model (NASTRAN) of the gear box structure. Out of a total of 25 modes existing in the analytical model in the 0 to 3 kHz frequency region, the eight dominant modes were used to represent the gear box dynamic characteristics. These analytically simulated modes are shown in Fig. 6.2. As shown in Table 6.1, the natural frequencies of the simulated modes are within 5 percent of the measured modes. The three-dimensional analytical mode shapes are very



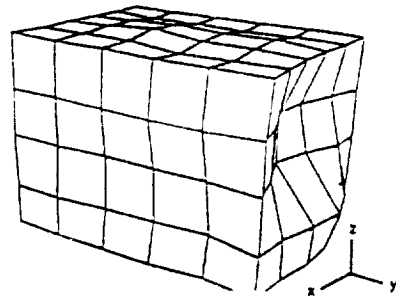
Mode 1 (658.37 Hz)



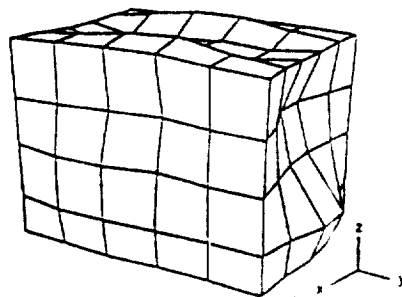
Mode 2 (1048.56 Hz)



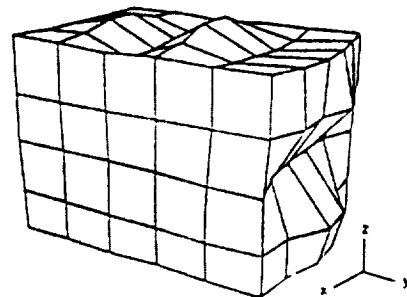
Mode 3 (1709.77 Hz)



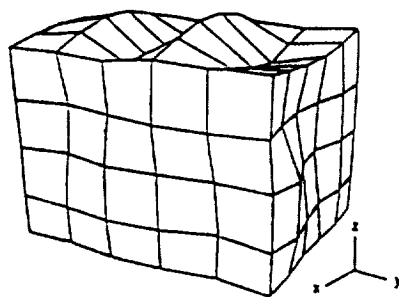
Mode 4 (1999.95 Hz)



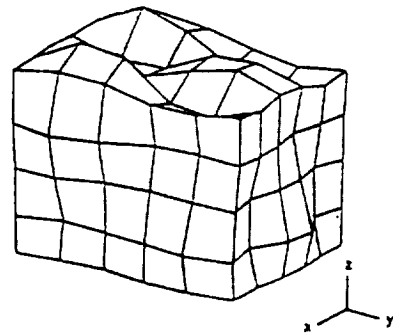
Mode 5 (2275.69 Hz)



Mode 6 (2535.77 Hz)

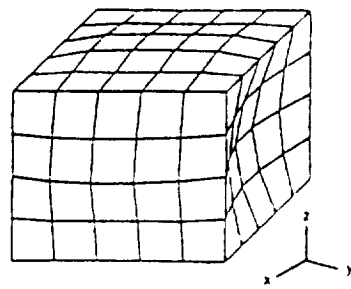


Mode 7 (2722.16 Hz)

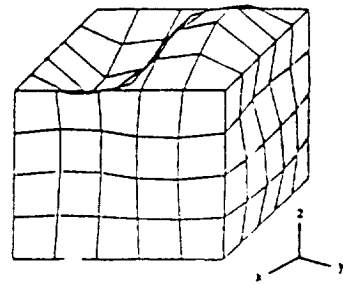


Mode 8 (2961.71 Hz)

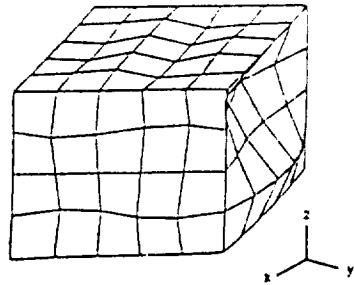
Figure 6.1 Experimentally Determined Mode Shapes of the Gear Box (0 to 3000 Hz)



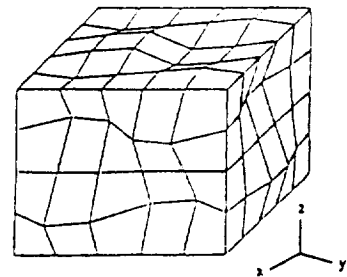
Mode 1 (658 Hz)



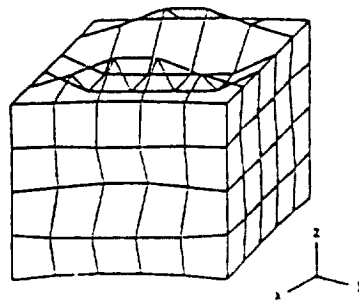
Mode 2 (1006 Hz)



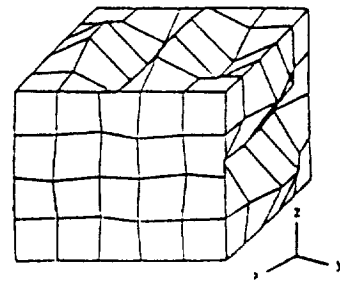
Mode 3 (1762 Hz)



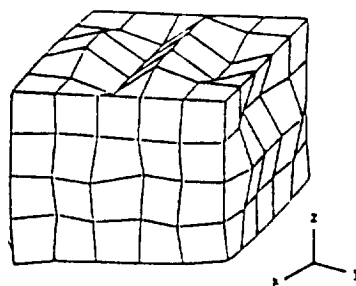
Mode 4 (2051 Hz)



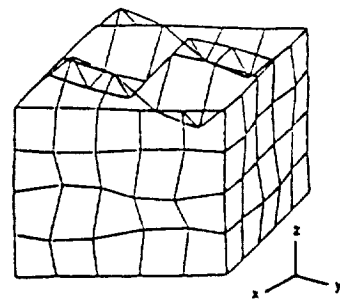
Mode 5 (2336 Hz)



Mode 6 (2536 Hz)



Mode 7 (2752 Hz)



Mode 8 (3012 Hz)

Figure 6.2 Analytically Determined Mode Shapes of the Gear Box (0 to 3000 Hz)

similar to the experimental modes shapes (Fig. 6.1). The correlation of the results between the analytical model and the experimental measurements confirms the accuracy of the dynamic representation of the test gear box using only a limited amount of modes. In addition, this correlation of the experimental modal characteristics with the numerical model also helps to reduce the number of modes being used in the numerical simulation to achieve an accurate result.

6.2 Rotor-Bearing-Gear Transient Vibrations

For the dynamic study of the rotor-bearing system, it was found that, during a slow roll (low speed run) of the rotor-gear assembly, a substantial residual bow exists in the rotor system as shown by its large orbital motion given in Fig. 6.3. Figure 6.3A represents the orbit of the driver rotor at the gear location and Fig. 6.3B represents those of the driven rotor. Note that the circular orbit existed in the driver rotor at slow roll represents the residual bow deformation of the rotor. The elliptical orbit in the driven rotor is due to a combination of the residual bow effects and the vertical gear force from the torque of the driving rotor. In order to analytically simulate the influence of this effect, a residual bow of 2 mils (0.05 mm) is incorporated into the numerical model.

To numerically simulate the dynamics of the rotor-bearing-gear system, the model shown in Fig. 6.4 was used. Figures 6.5 - 6.14 show the comparison of the rotor orbital motion between the numerical simulations and experimental studies for a range of operating speeds from 1500 - 6000 rpm, with a 500 rpm increment. In these figures (6.5 - 6.14), stage 1 represents the motion of the driving rotor near the gear mesh and stage 2 represents the driven rotor

**TABLE 6.1 - COMPARISON OF EXPERIMENTAL
MEASURED AND ANALYTICAL MODELED NATURAL FREQUENCIES**

Experimental, Hz	Analytical, Hz	Difference, percent
658	658	0
1049	1006	-4.1
1710	1762	3.0
2000	2051	2.6
2276	2336	2.6
2536	1536	0
2722	2752	1.1
2962	3012	1.7

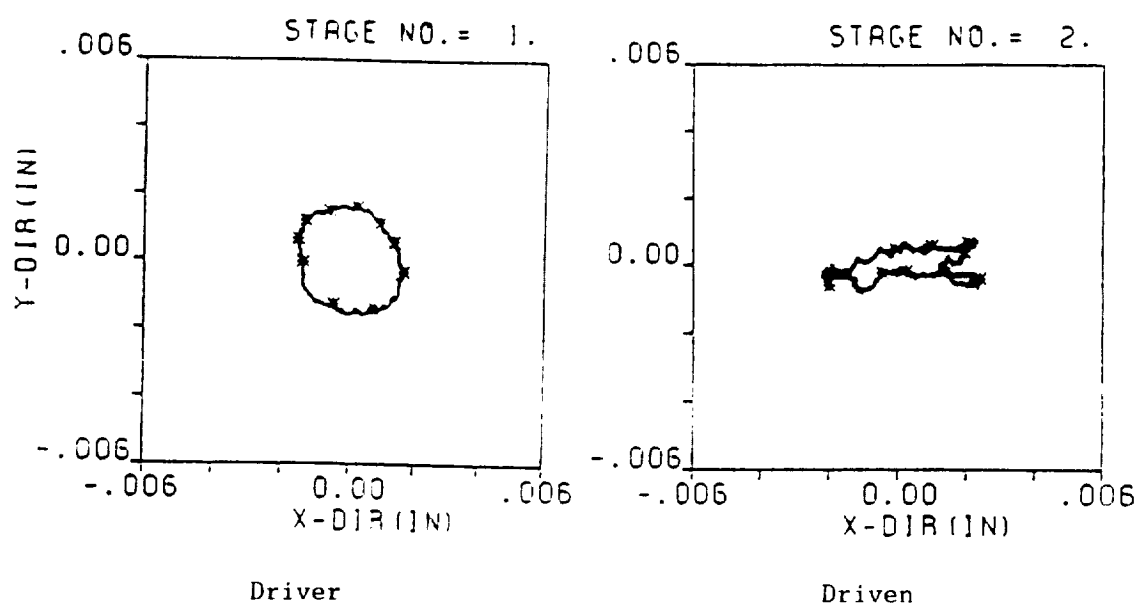


Figure 6.3 Orbital Motion of the Driver and the Driven Rotors During Slow Roll from Experimental Study

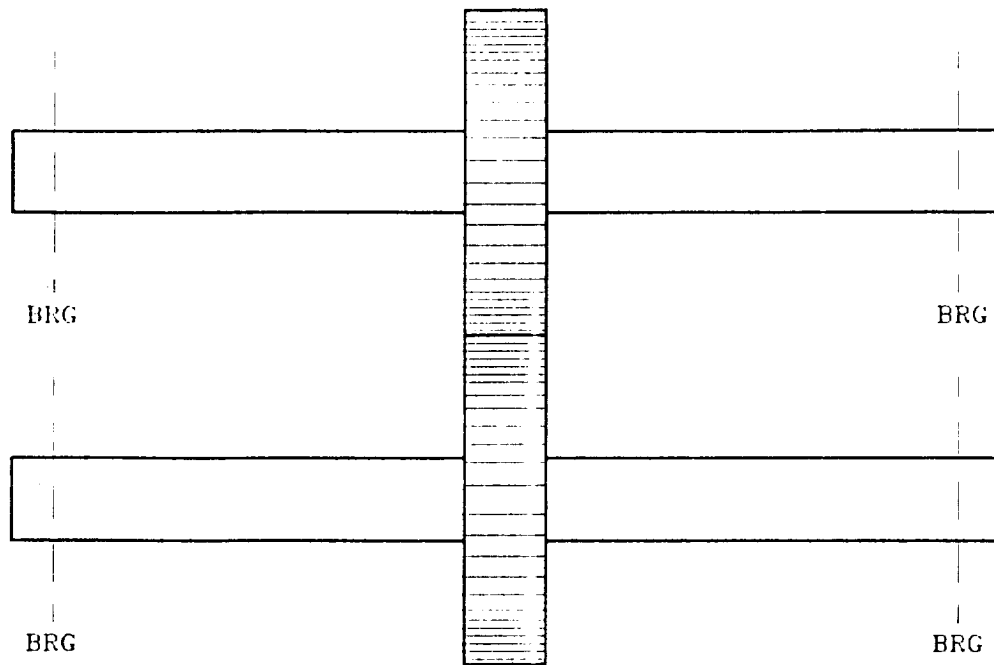


Figure 6.4 Schematic of Rotor-Gear-Bearing Model

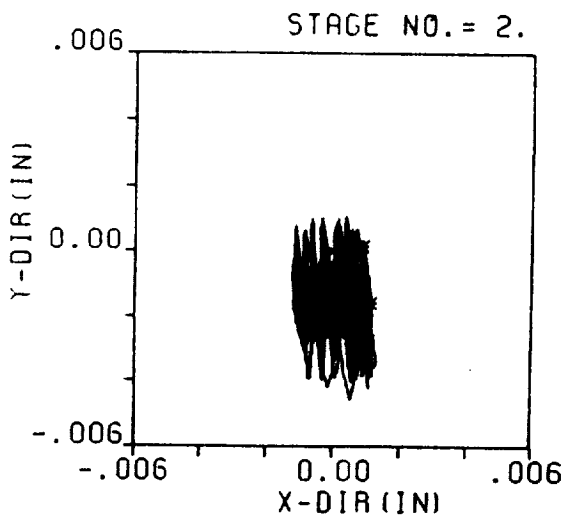
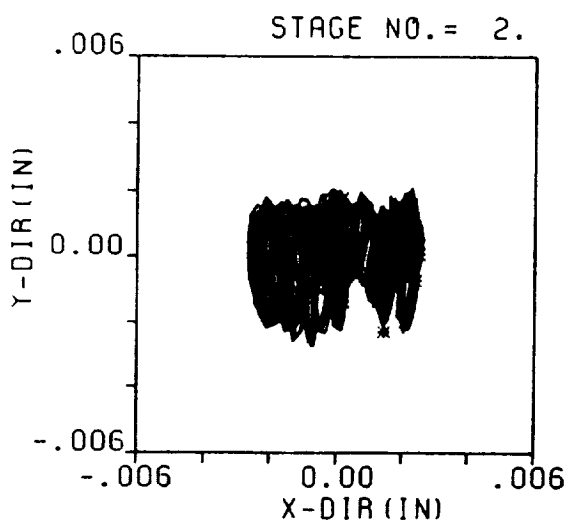
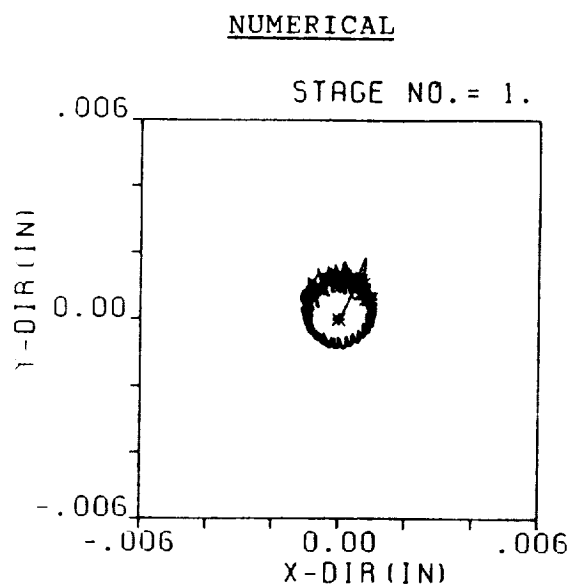
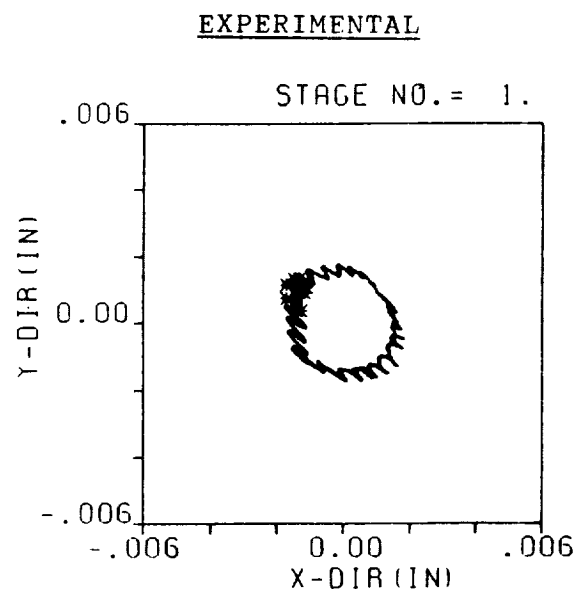


Figure 6.5 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulation
at 1500 rpm

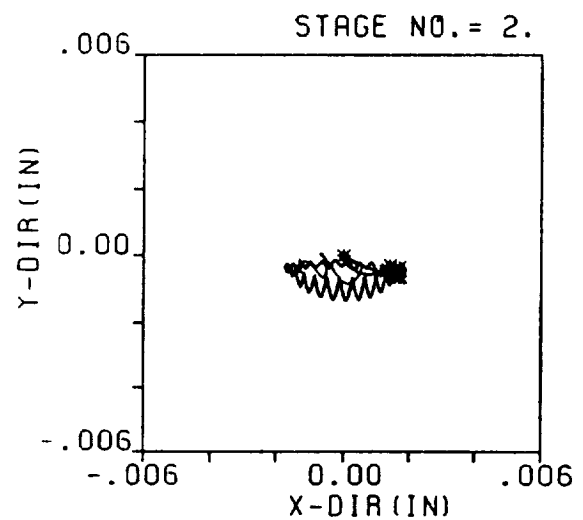
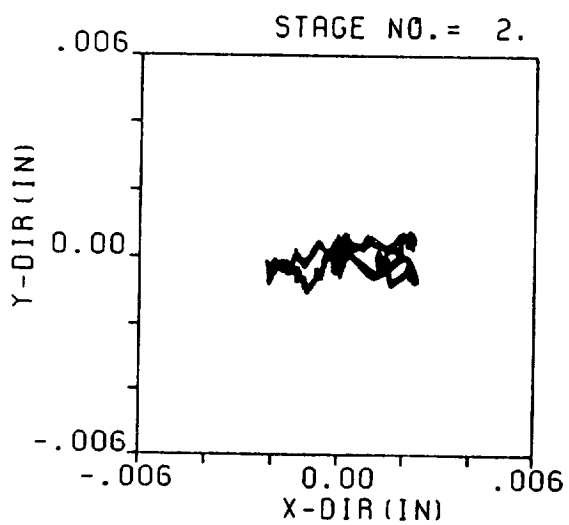
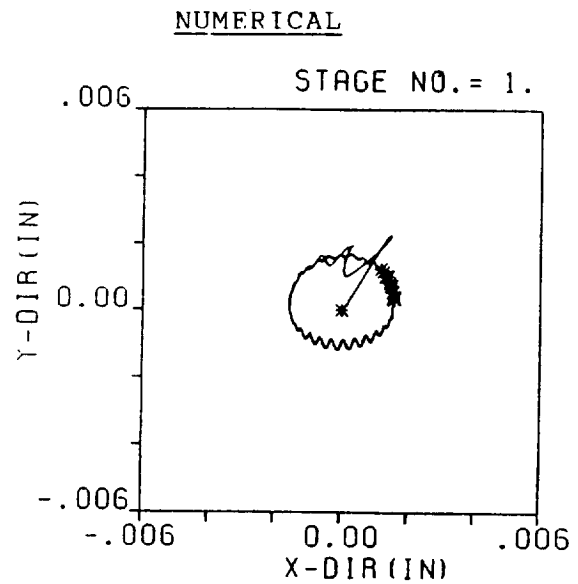
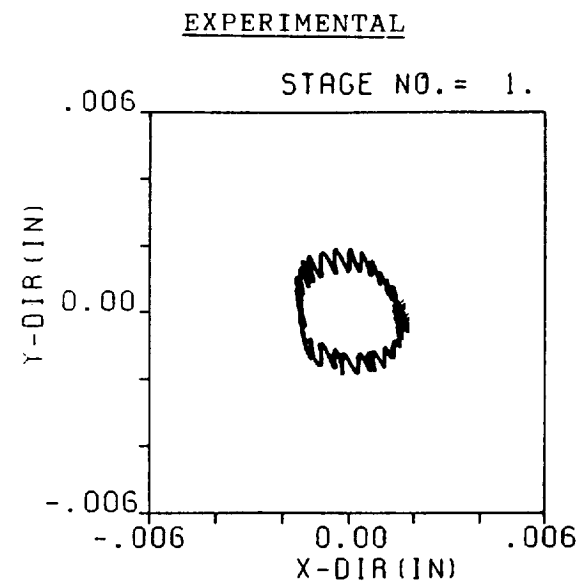


Figure 6.6 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulations
at 2000 rpm

EXPERIMENTAL

NUMERICAL

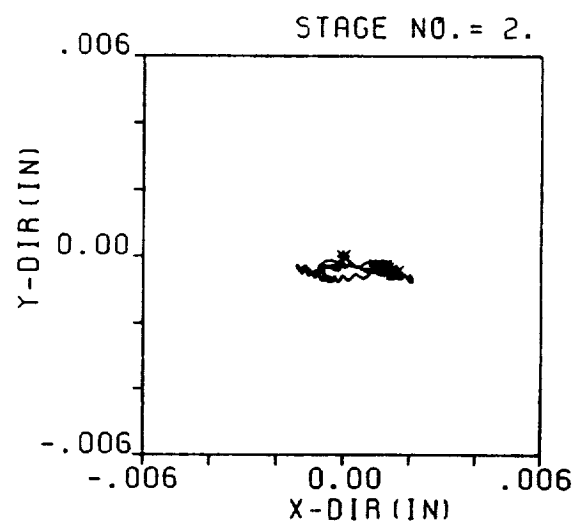
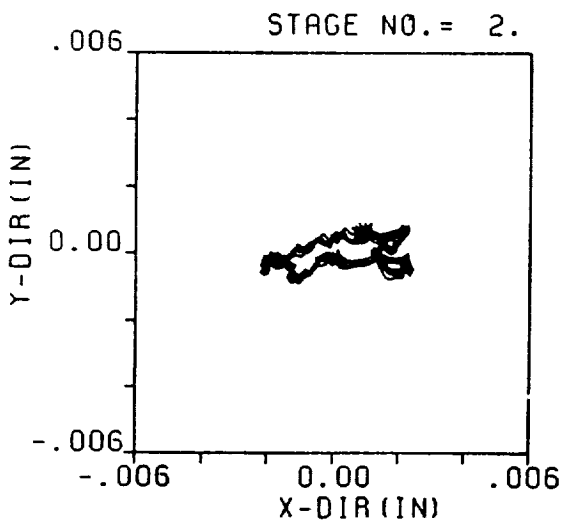
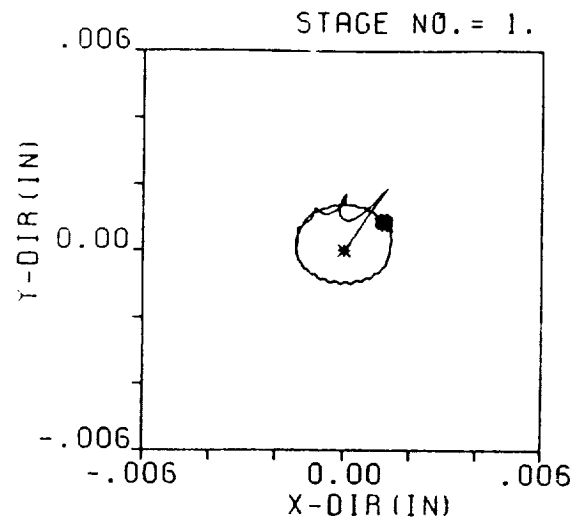
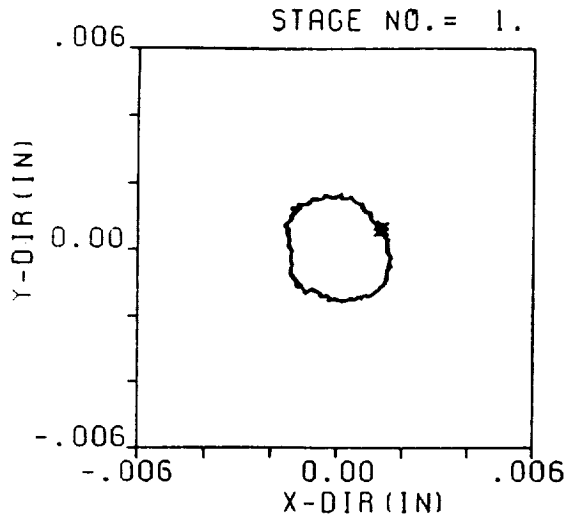
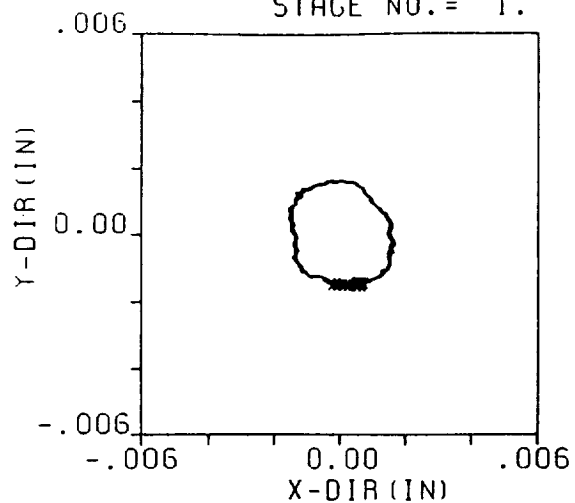


Figure 6.7 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulation
at 2500 rpm

EXPERIMENTAL

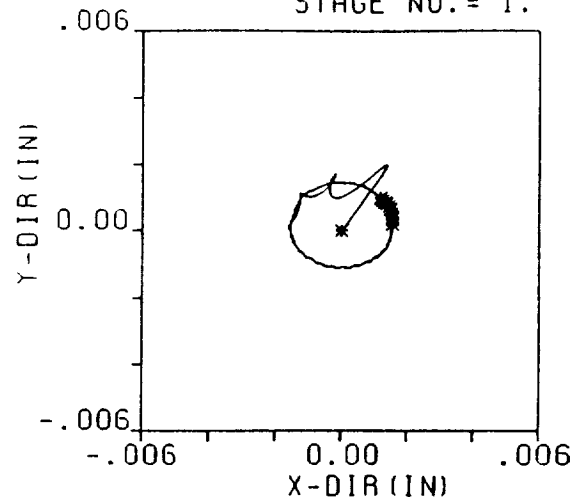
SPEED = 3000.

STAGE NO.= 1.



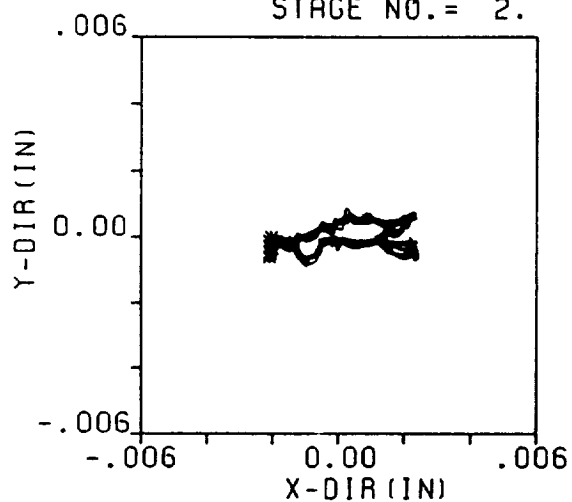
NUMERICAL

STAGE NO.= 1.



SPEED = 3000.

STAGE NO.= 2.



STAGE NO.= 2.

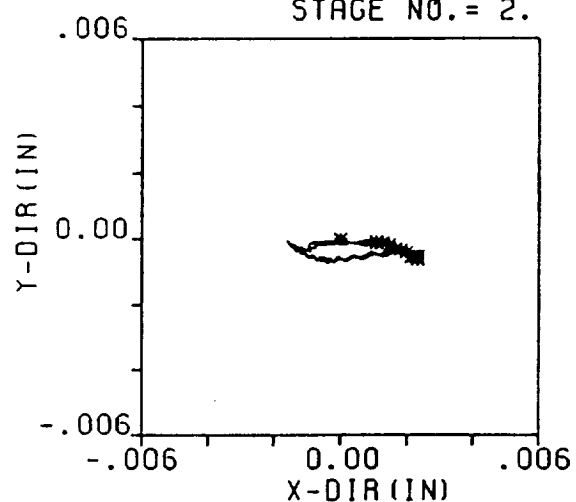
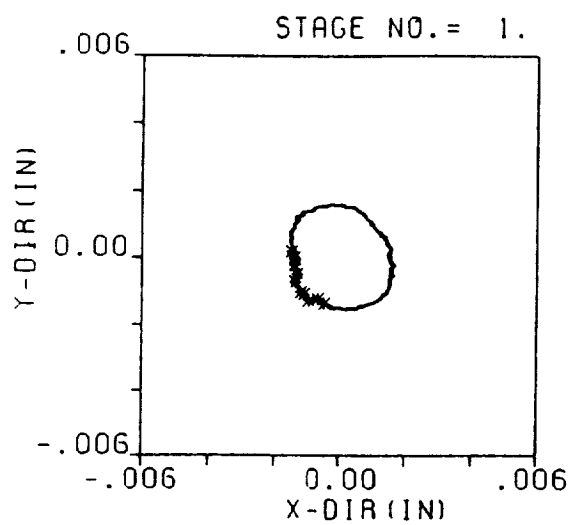


Figure 6.8 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulation
at 3000 rpm

EXPERIMENTAL



NUMERICAL

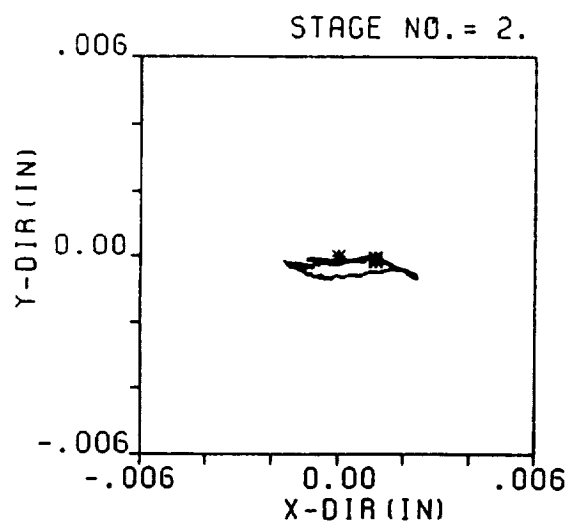
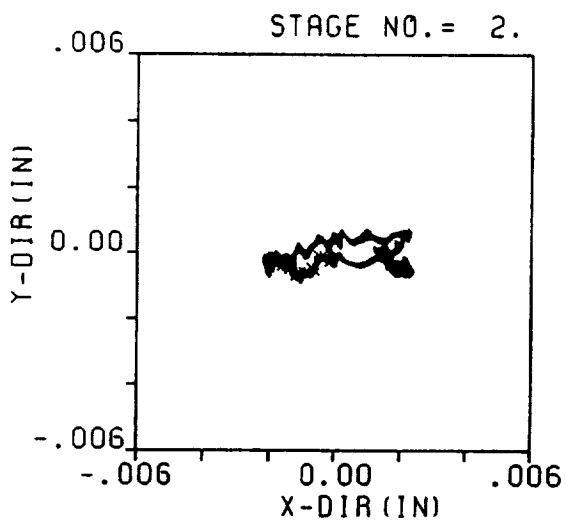
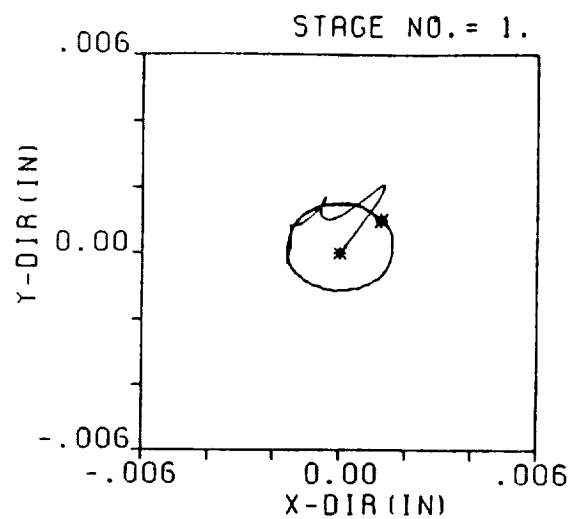
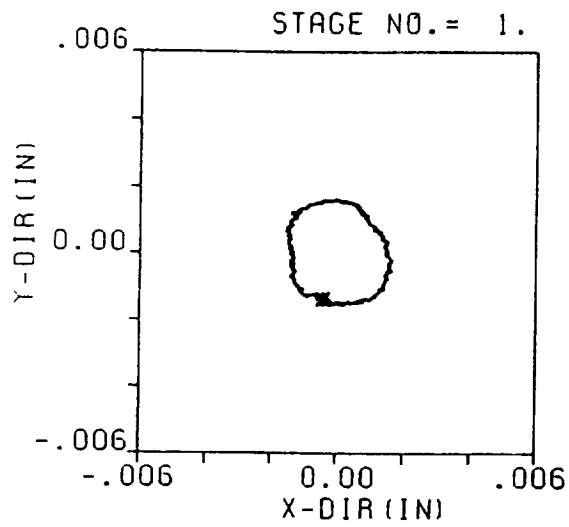


Figure 6.9 Orbital Motion of the Driver and the Driven Rotors from Experimental Study and Numerical Simulations at 3500 rpm

EXPERIMENTAL



NUMERICAL

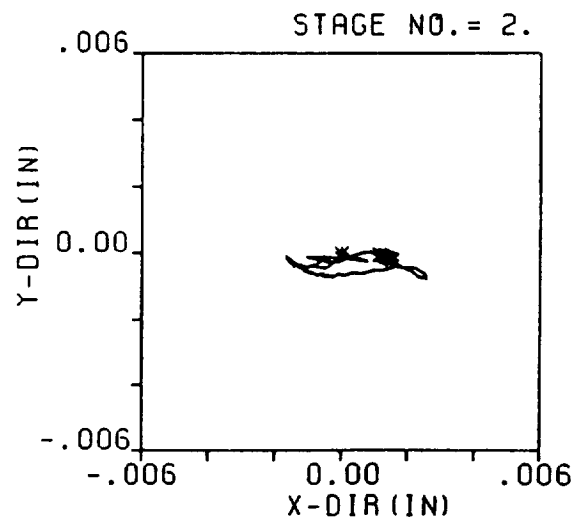
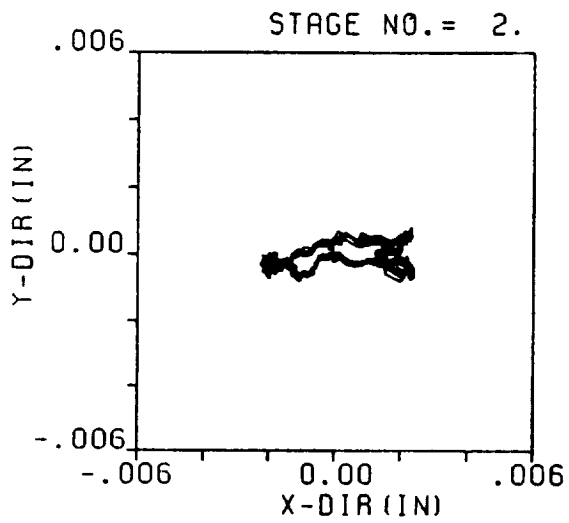
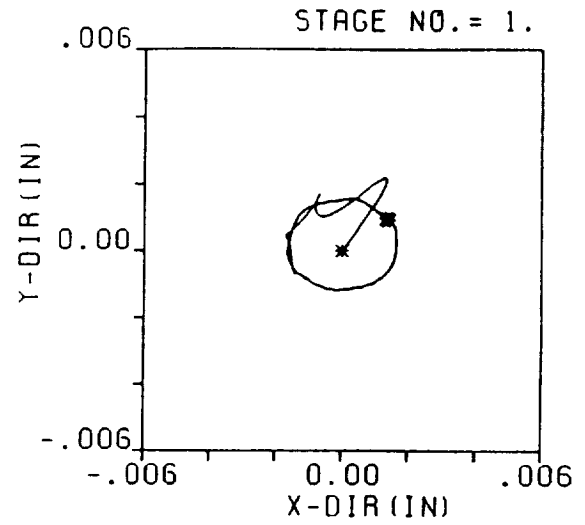
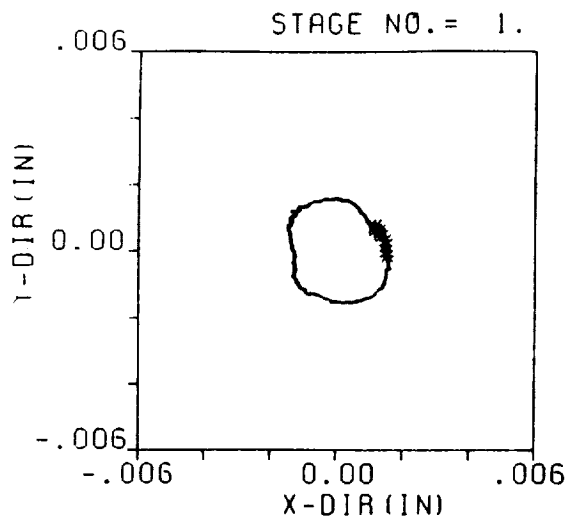


Figure 6.10 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulations
at 4000 rpm

EXPERIMENTAL



NUMERICAL

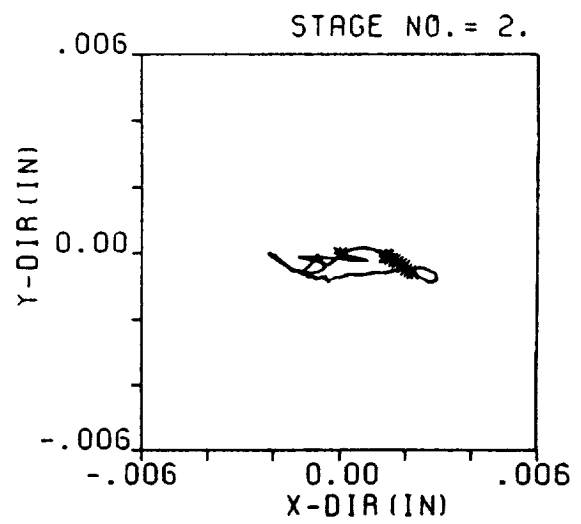
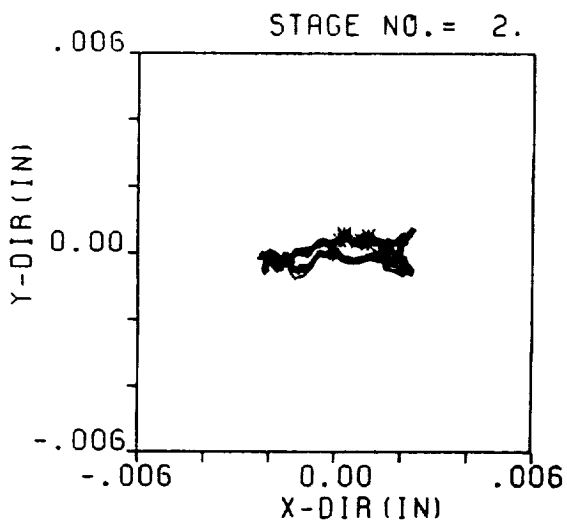
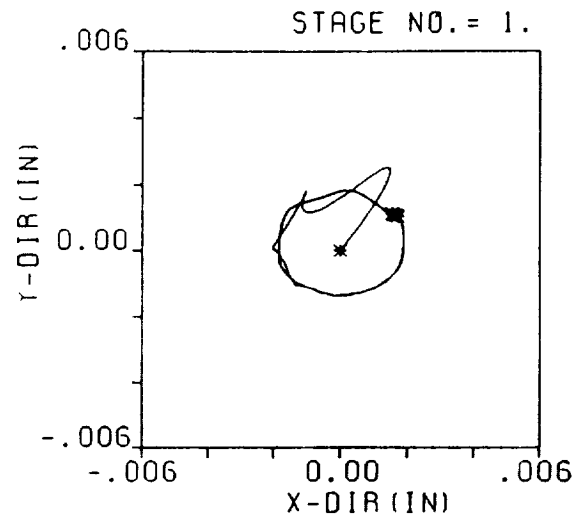
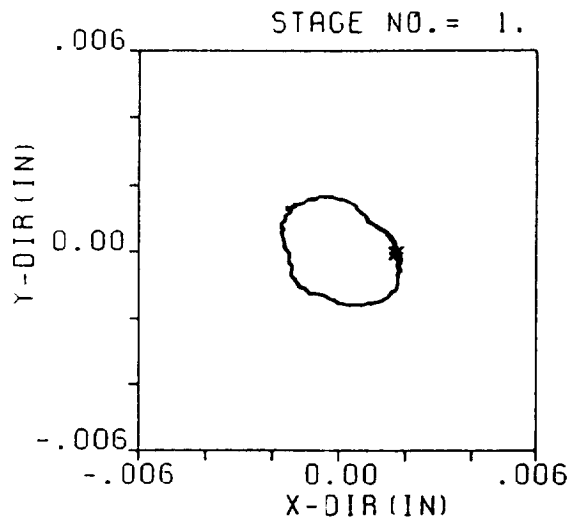


Figure 6.11 Orbital Motion of the Driver and the Driven Rotors from Experimental Study and Numerical Simulations at 4500 rpm

EXPERIMENTAL



NUMERICAL

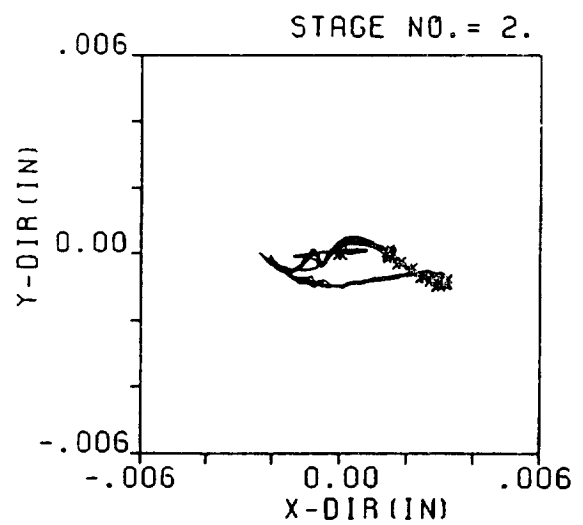
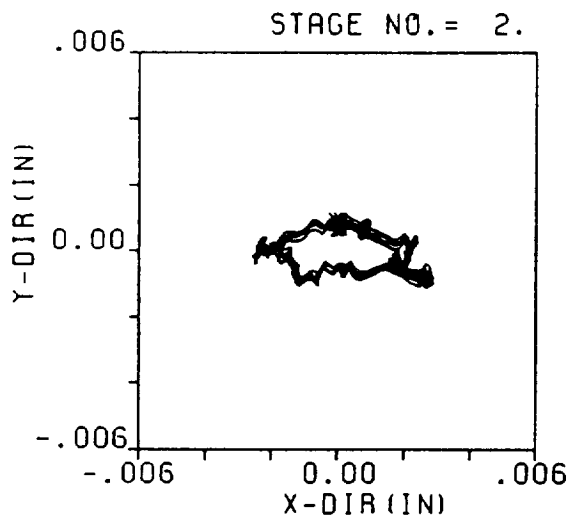
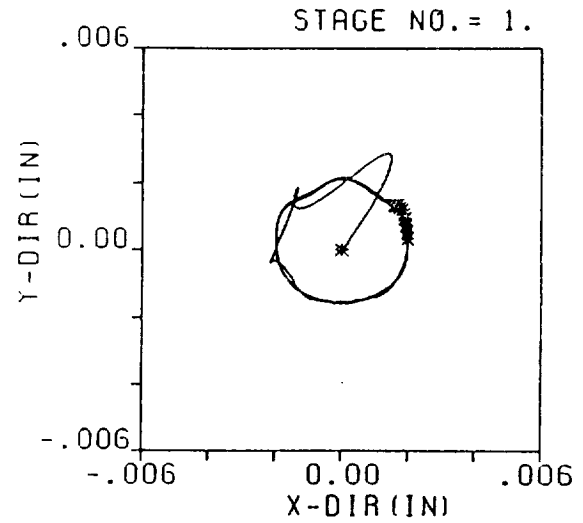
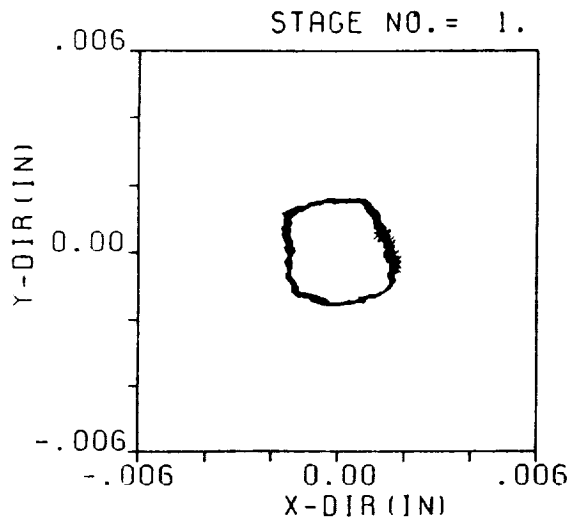


Figure 6.12 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulations
at 5000 rpm

EXPERIMENTAL



NUMERICAL

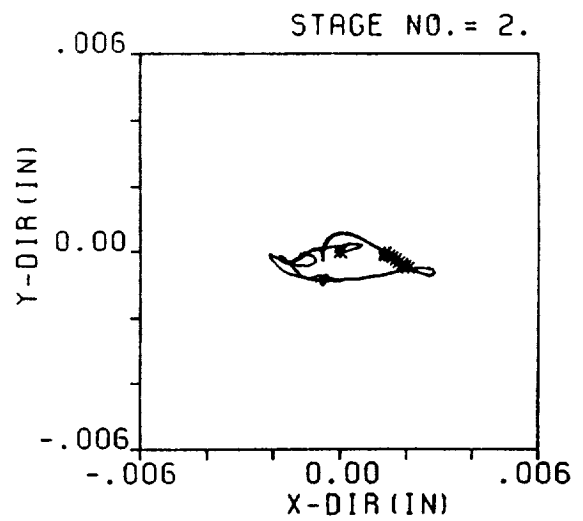
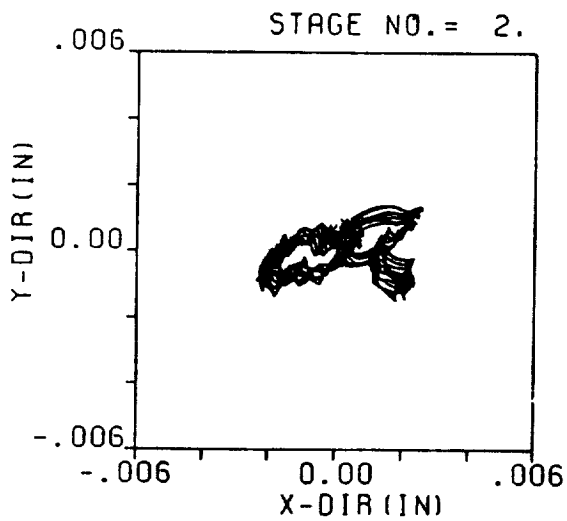
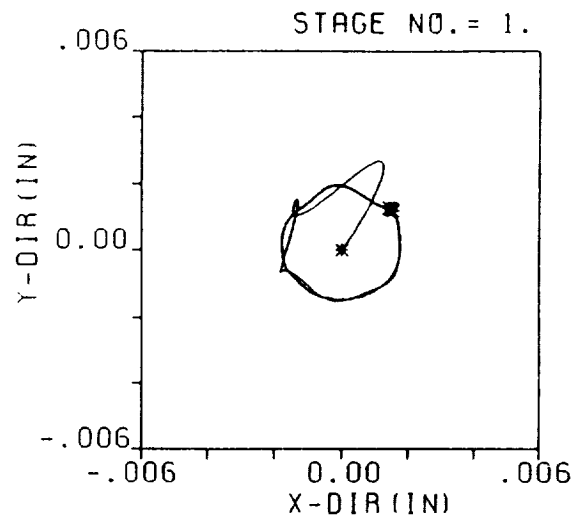
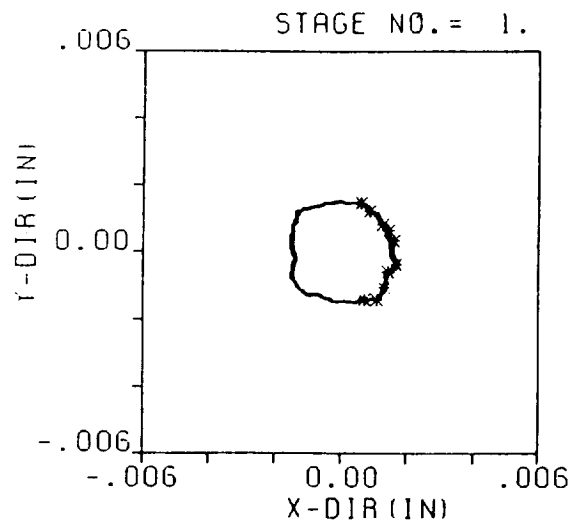


Figure 6.13 Orbital Motion of the Driver and the Driven Rotors from Experimental Study and Numerical Simulations at 5500 rpm

EXPERIMENTAL



NUMERICAL

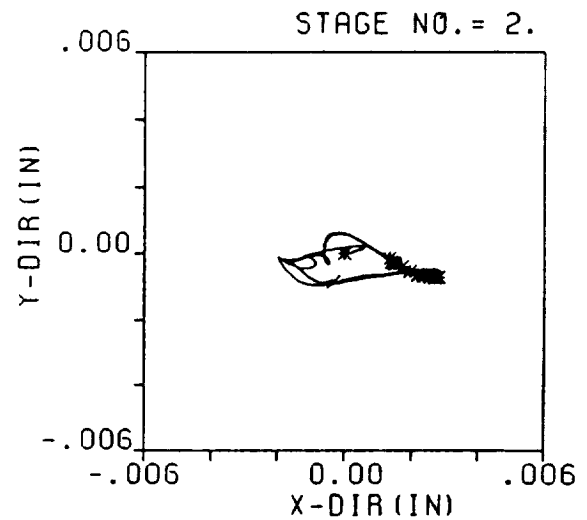
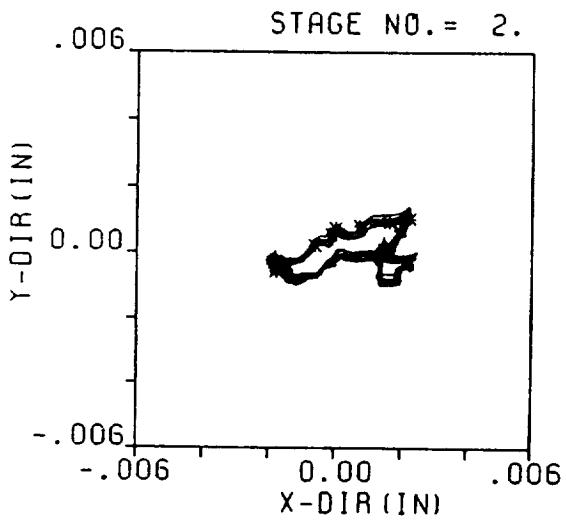
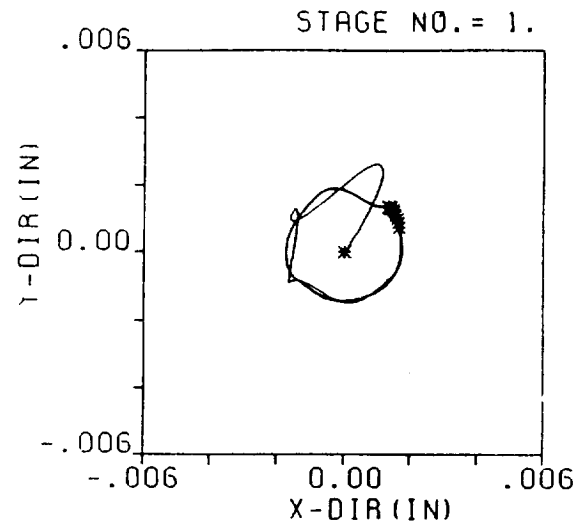


Figure 6.14 Orbital Motion of the Driver and the Driven Rotors
from Experimental Study and Numerical Simulations
at 6000 rpm

near the gear mesh. Note that a substantial magnitude of the circular orbit in the driver rotor represents the residual bow deformation of the rotor. The elliptical orbit in the driven rotor is attributed to a combination of the residual bow effects and the normal gear force from the torque of the driving rotor. The slightly large amplitudes of orbital motion existing at running speeds of 1500 rpm and 5000 rpm are due to the excitation frequencies being closed to one of the natural frequencies of the rotor system. Very similar trends in orbital shapes and magnitudes were observed in both the experimental and numerical studies, which verifies the validity of the numerical procedures as well as the modelling accuracy. Figure 6.15 and 6.16 represent frequency spectra of the vibration generated from both the experimental and the numerical procedures. The excellent agreement in both results further verifies the validity of the numerical study.

6.3 Gear Box Transient Dynamics

In order to predict the noise of the transmission system during operation, the vibration of the gear box must be accurately modelled. In this section, the comparison between experimental and predicted gear box vibrations is presented.

Figure 6.17, 6.18, and 6.19 present the vibration frequency spectra of the gear box surface from both experimental and numerical studies, in the x, y, and z directions, respectively.

Note in Fig. 6.17A, the experimental results of the casing vibration in the x-direction shows a major vibration component at 28 times the shaft frequency. This is due to the excitation of the gear tooth pass frequency (28 tooth gear) at the various shaft speeds. A closer examination of this excited frequency component shows that two major vibration peaks

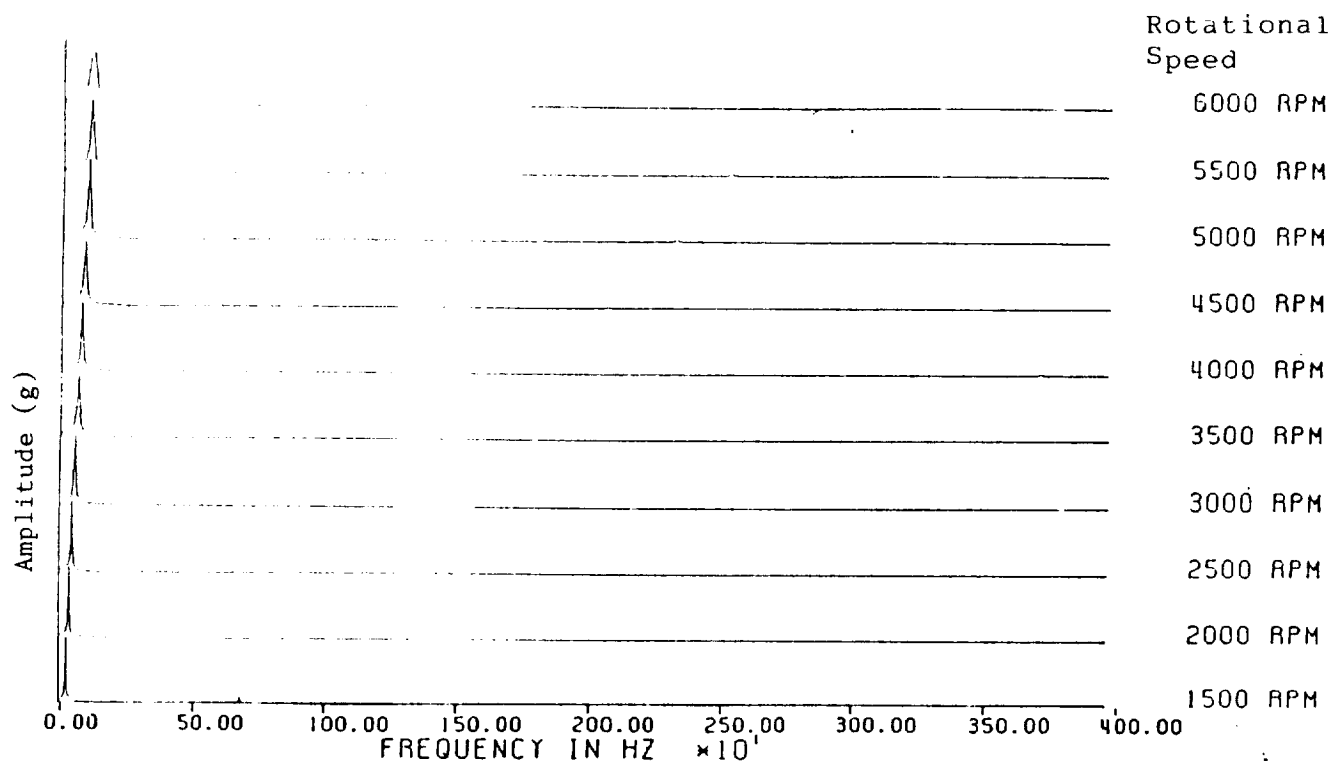


Figure 6.15A Frequency Spectra of the X-direction Vibration of the 1st Rotor from Experimental Study

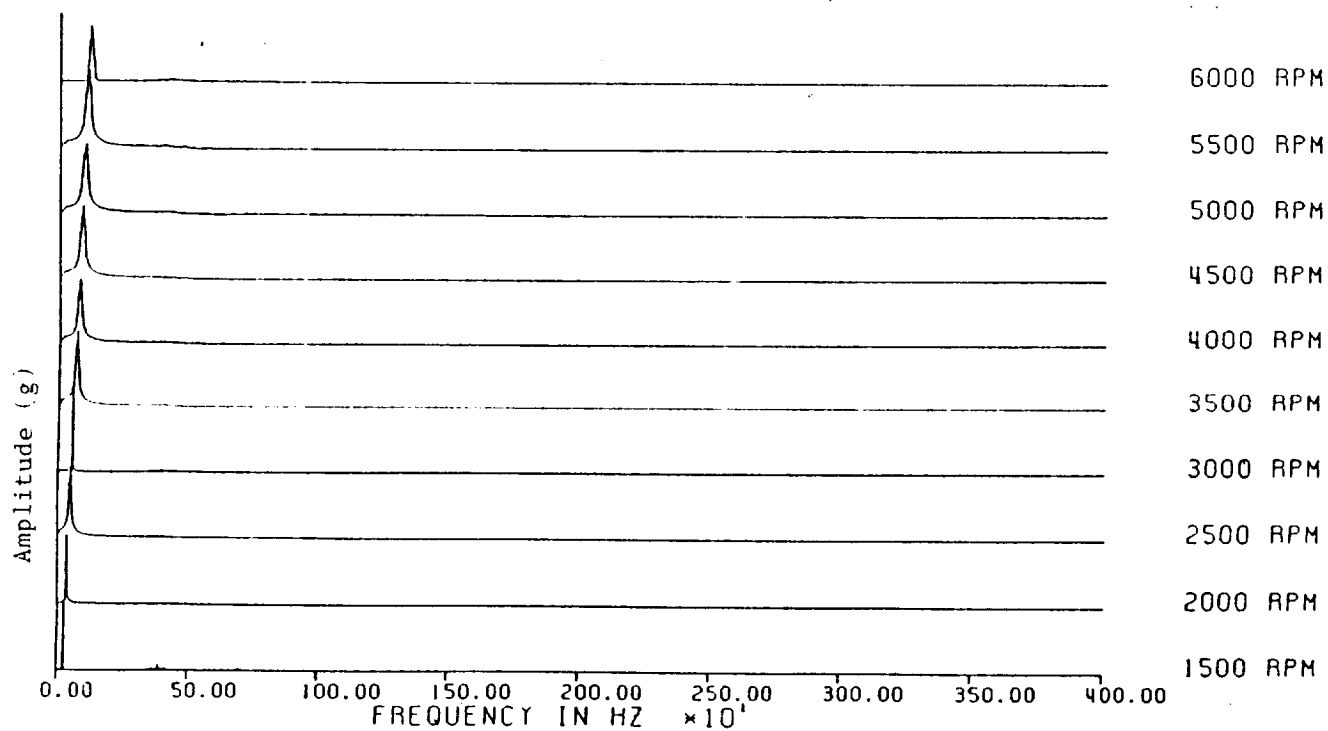


Figure 6.15B Frequency Spectra of the X-direction Vibration of the 1st Rotor from Numerical Simulation

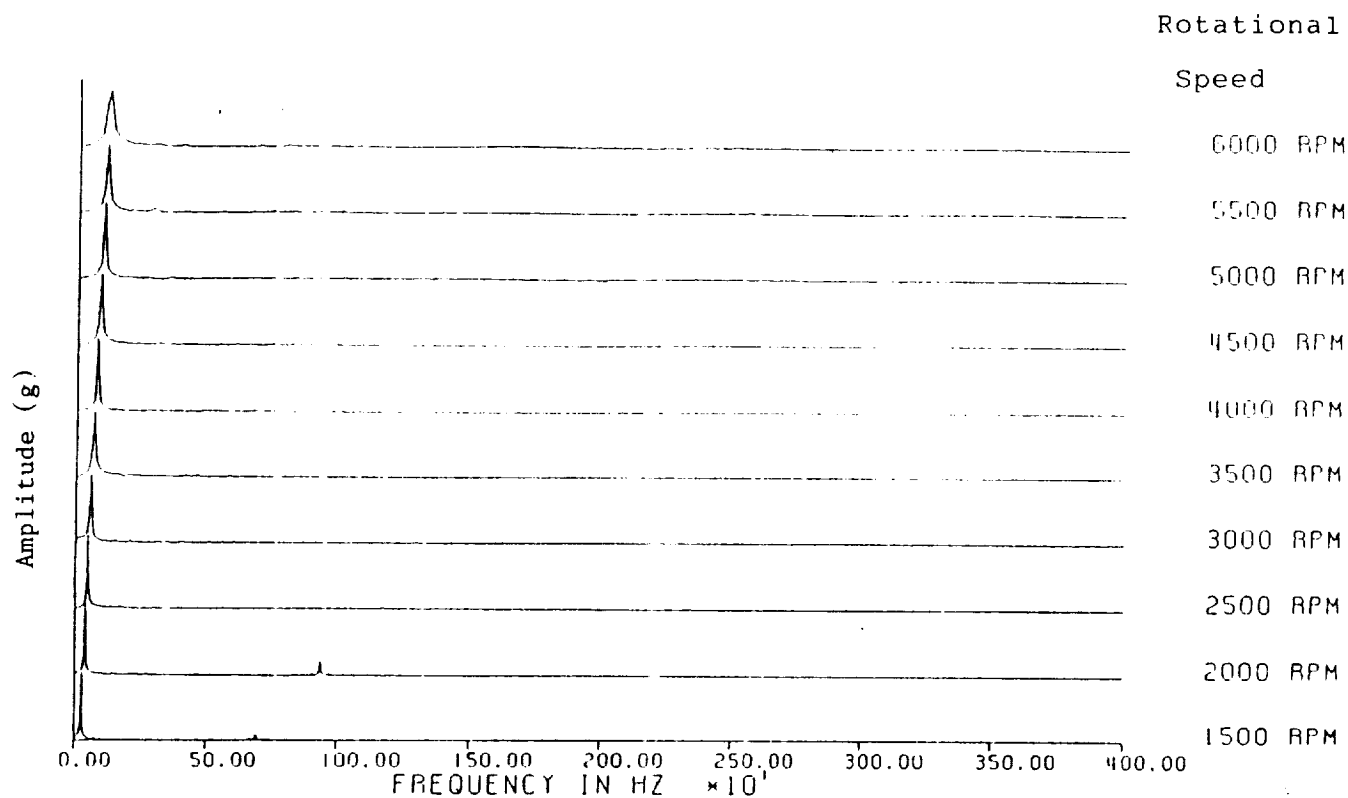


Figure 6.15C Frequency Spectra of the Y-direction Vibration of the 1st Rotor from Experimental Study

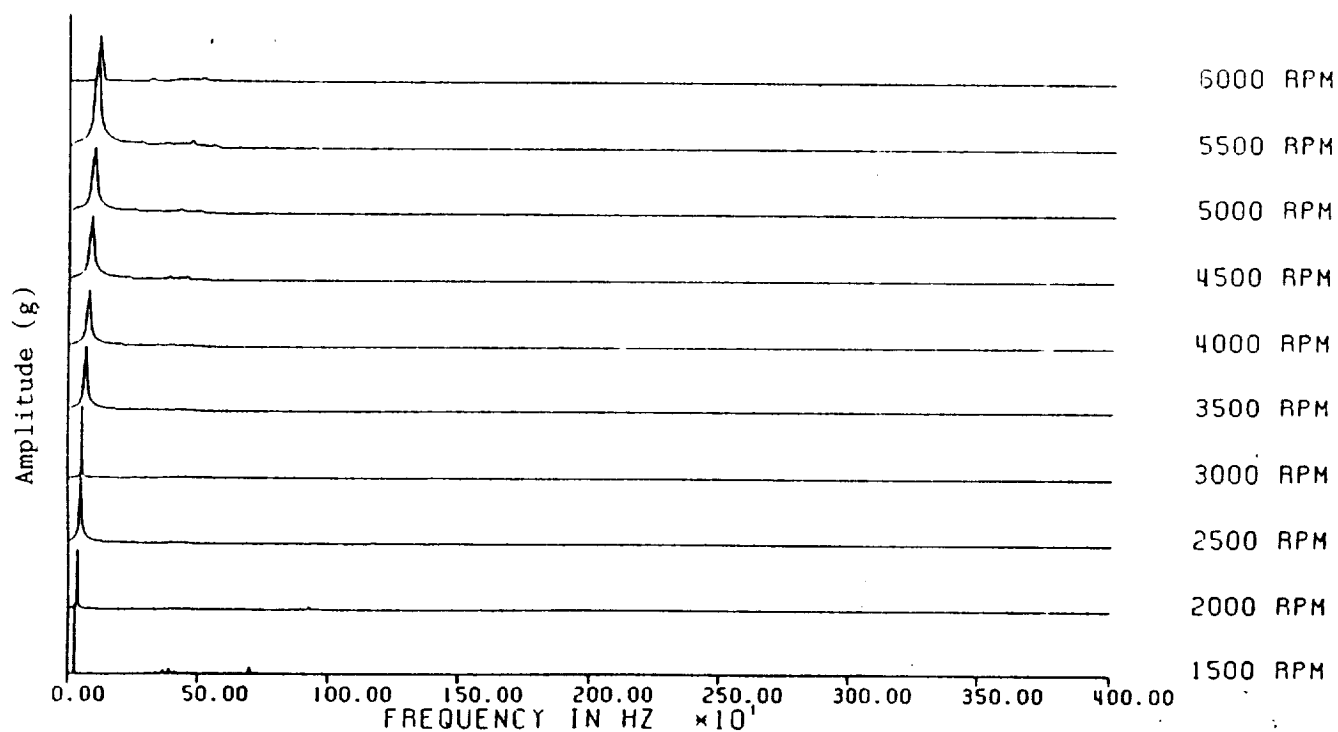


Figure 6.15D Frequency Spectra of the Y-direction Vibration of the 1st Rotor from Numerical Simulation

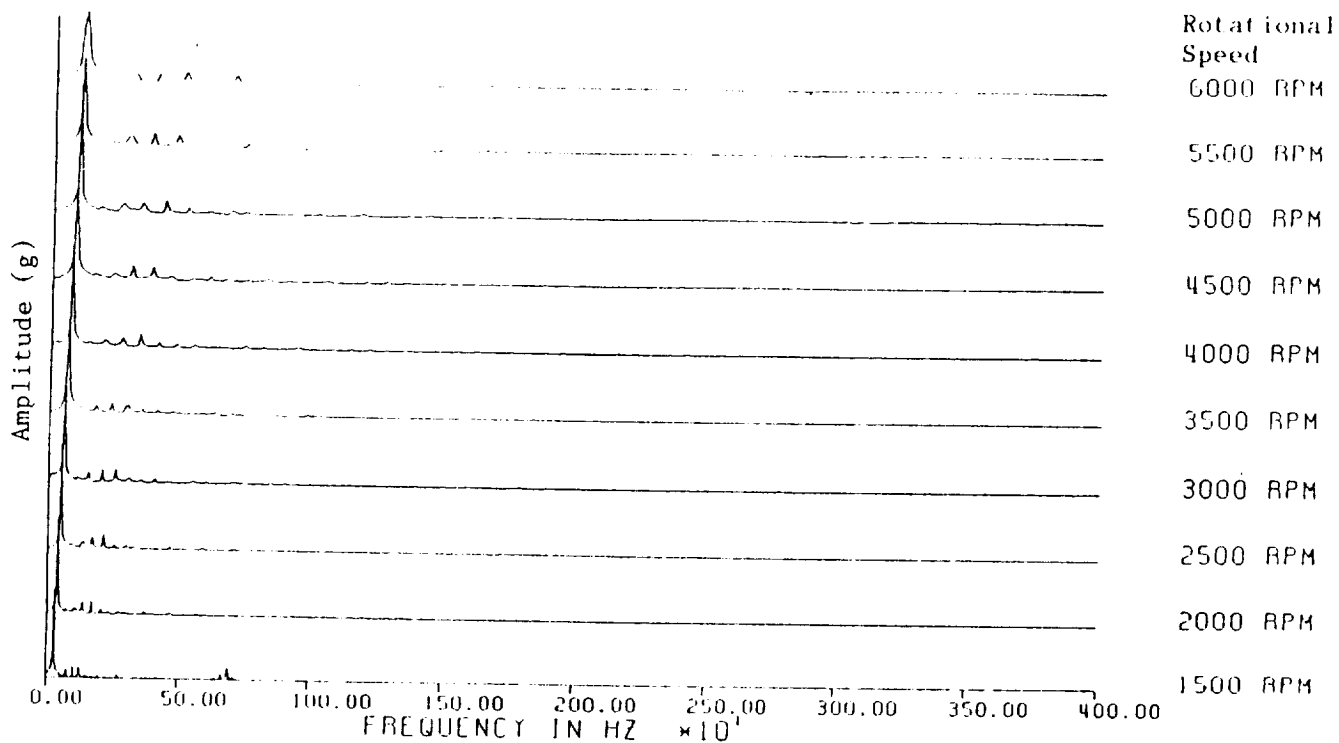


Figure 6.16A Frequency Spectra of the X-direction Vibration of the 2nd Rotor from Experimental Study

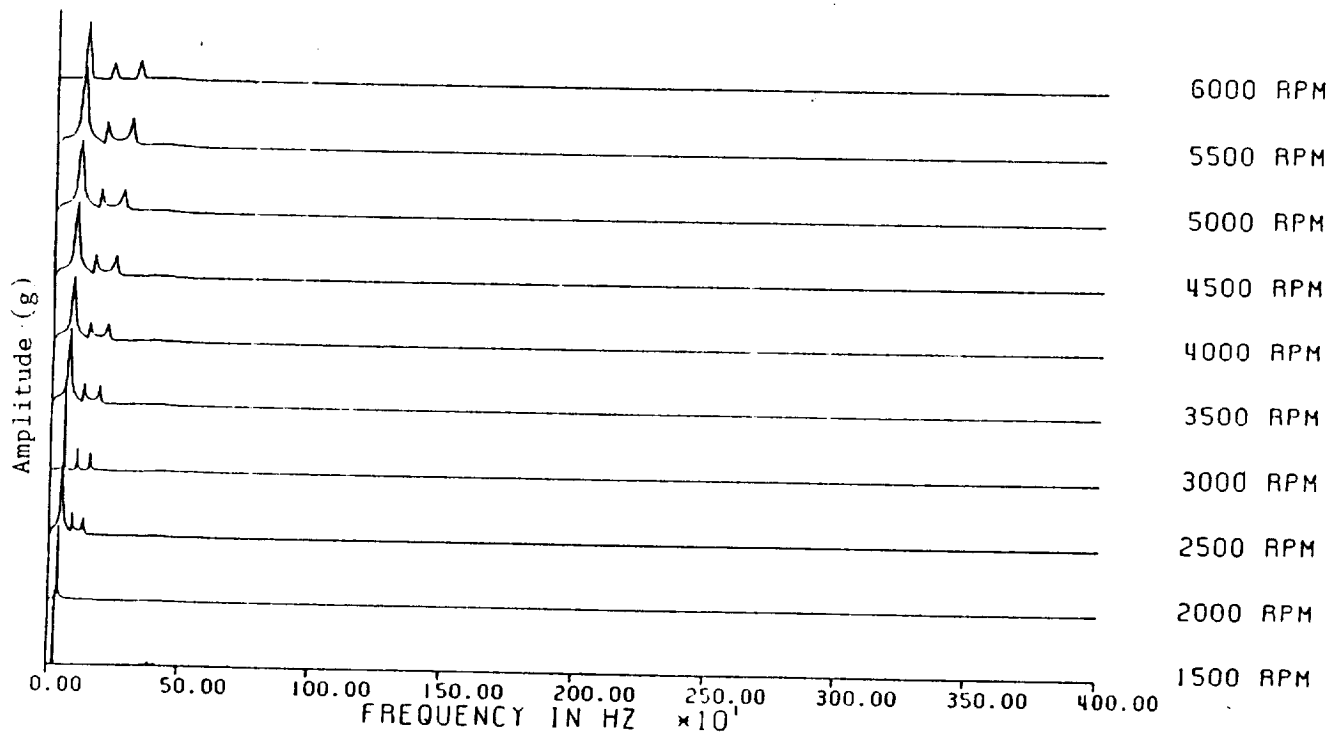


Figure 6.16B Frequency Spectra of the X-direction Vibration of the 2nd Rotor from Numerical Simulation

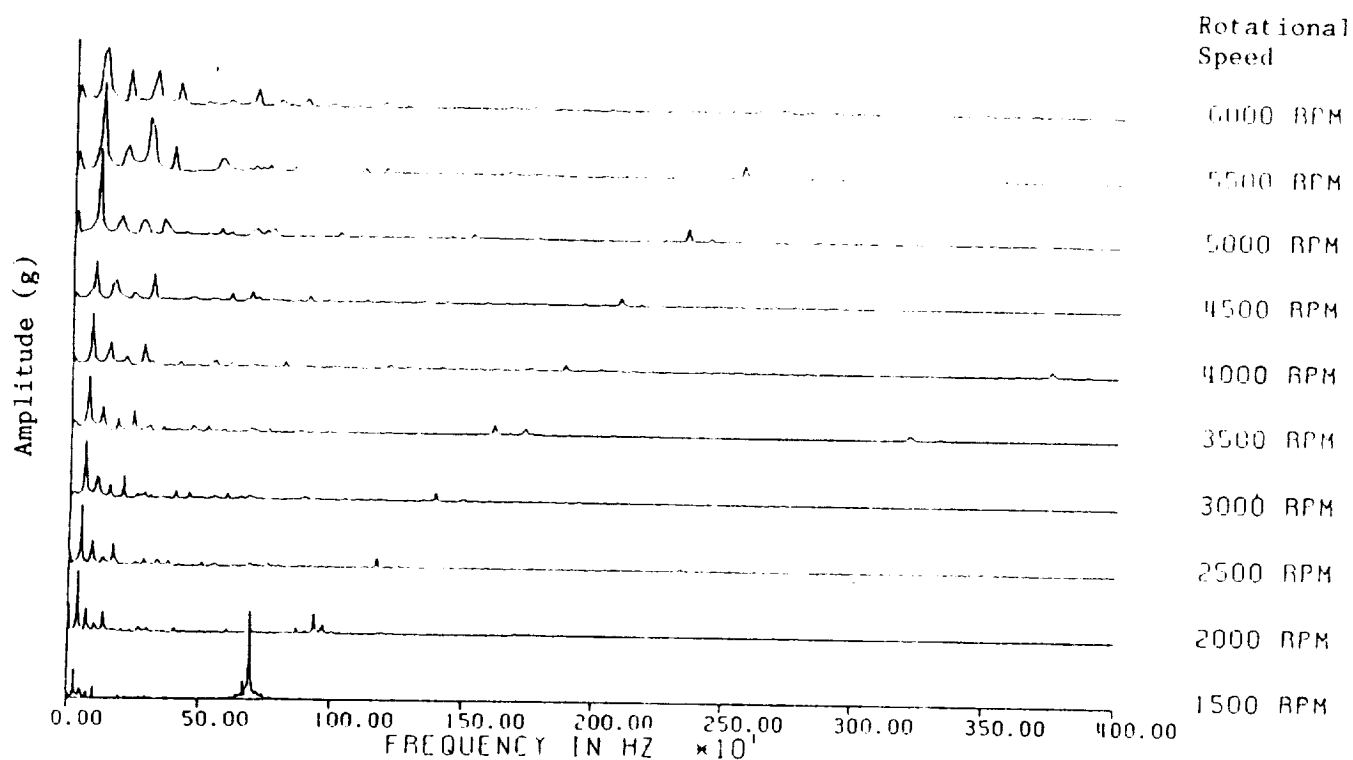


Figure 6.16C Frequency Spectra of the Y-direction Vibration of the 2nd Rotor from Experimental Study

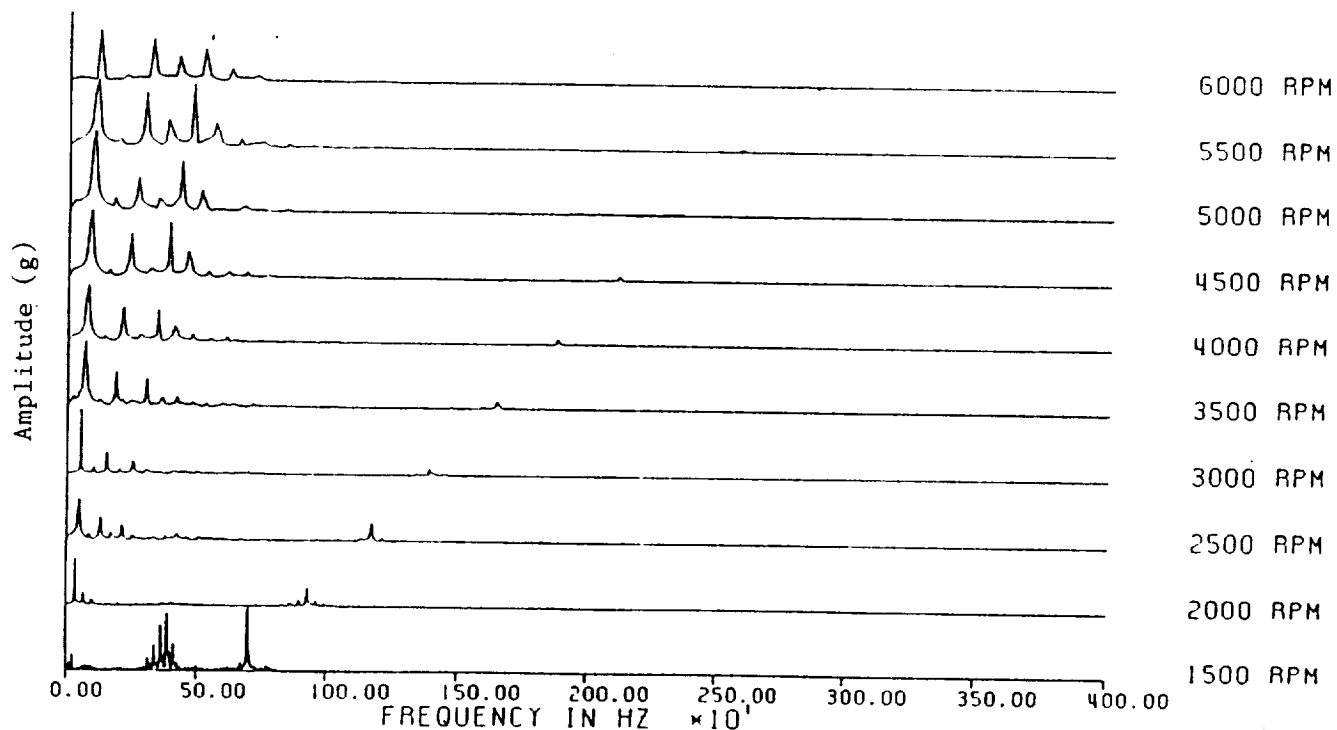


Figure 6.16D Frequency Spectra of the Y-direction Vibration of the 2nd Rotor from Numerical Simulation

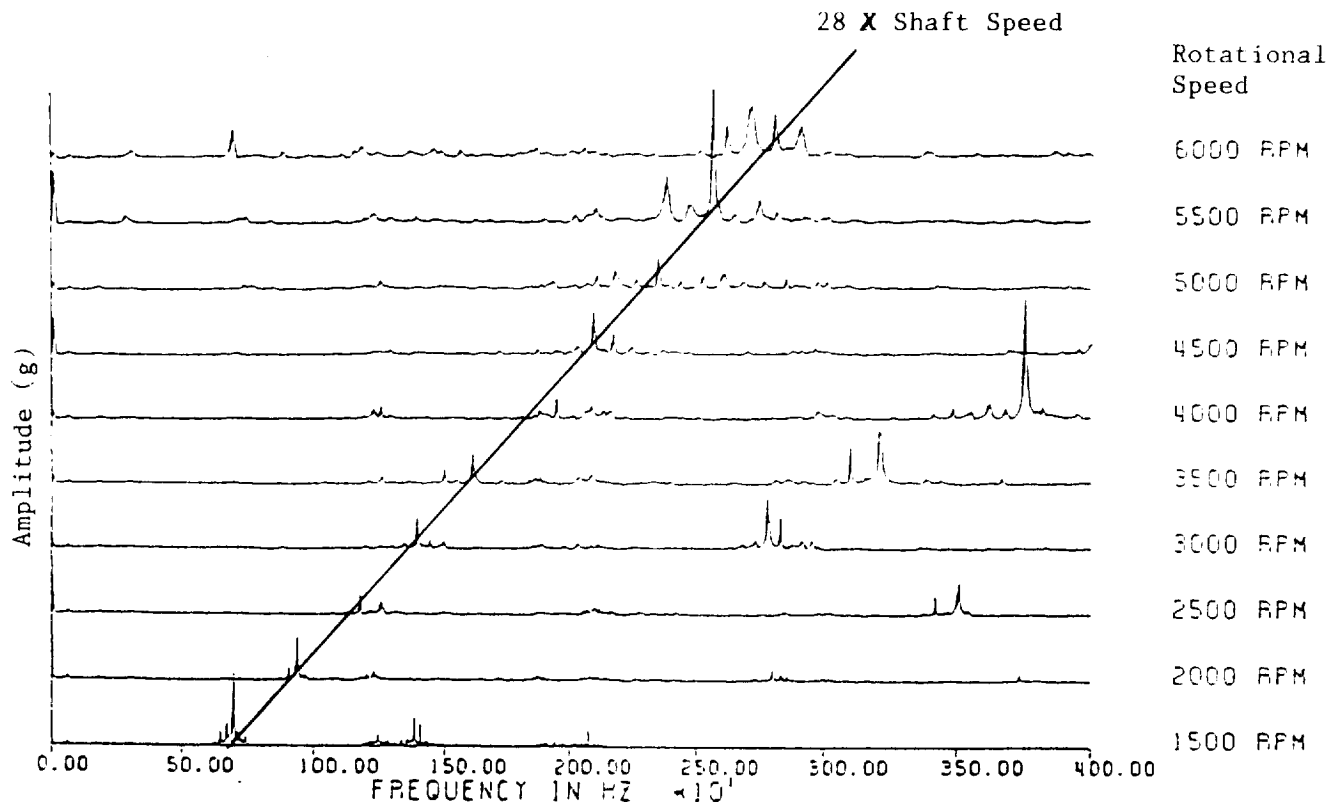


Figure 6.17A Frequency Spectra of the X-direction Vibration of the Gear Box from Experimental Study

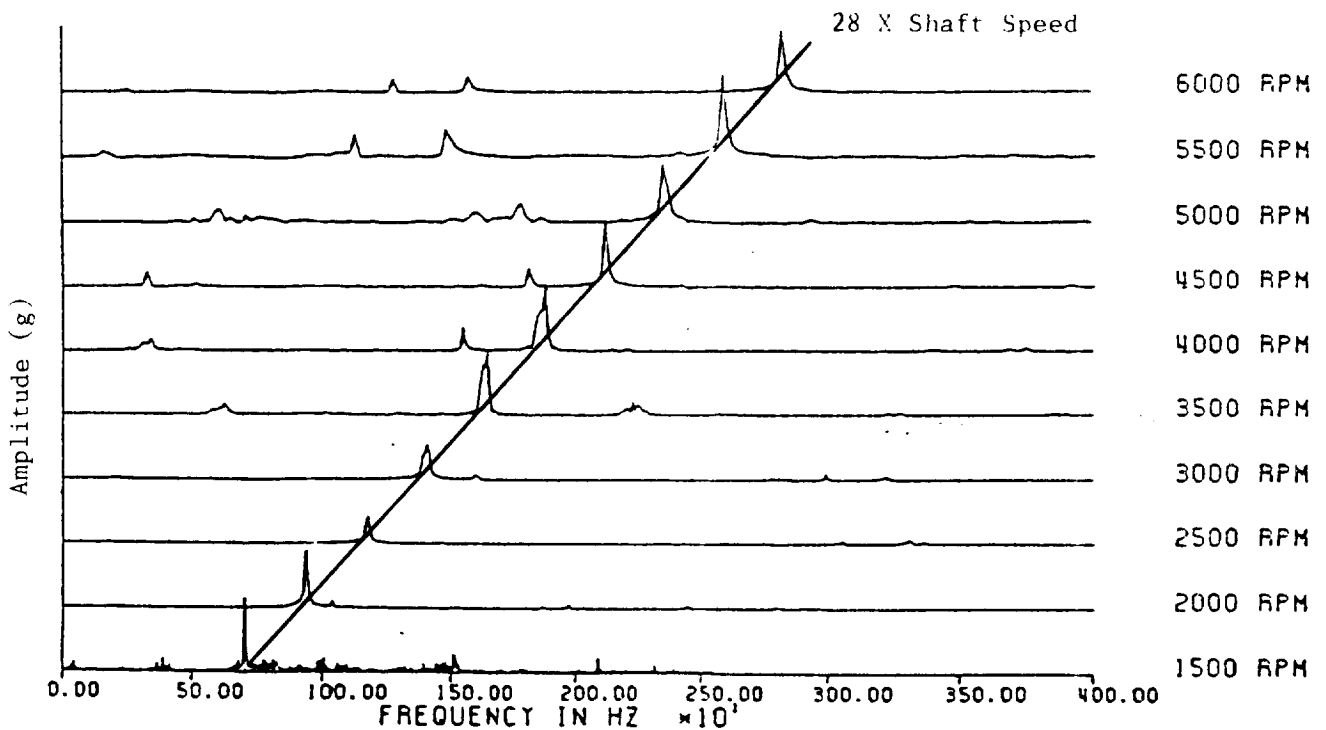


Figure 6.17B Frequency Spectra of the X-direction Vibration of the Gear Box from Numerical Simulations

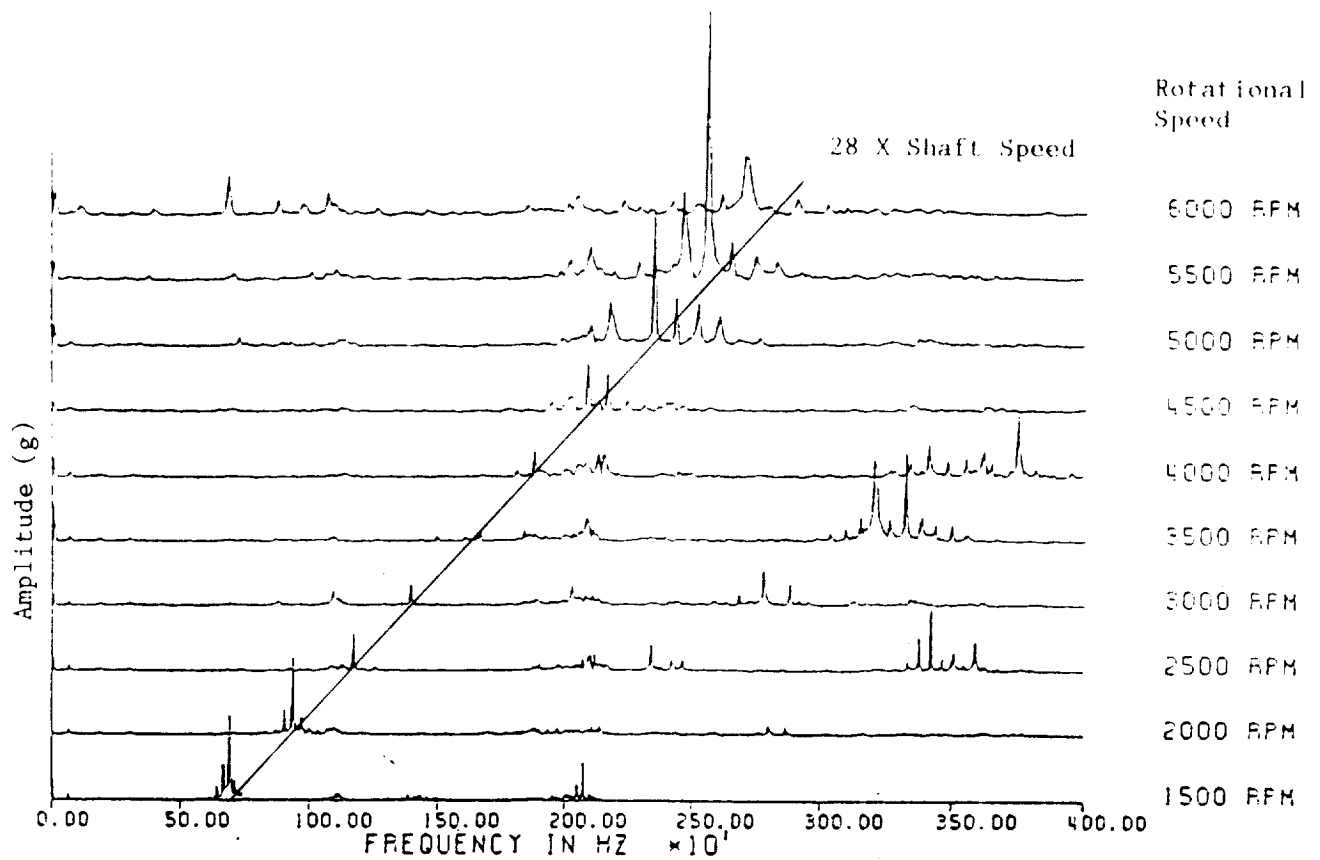


Figure 6.18A Frequency Spectra of the Y-direction Vibration of the Gear Box from Experimental Study

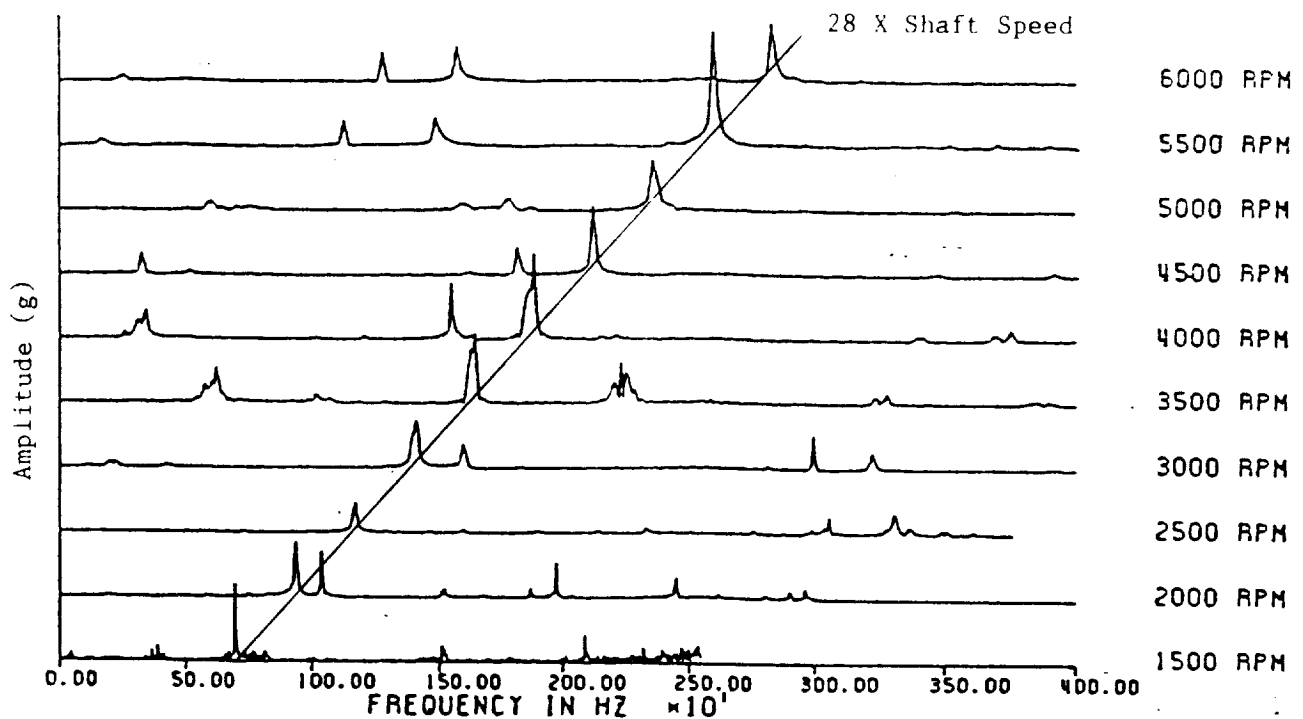


Figure 6.18B Frequency Spectra of the Y-direction Vibration of the Gear Box from Numerical Simulations

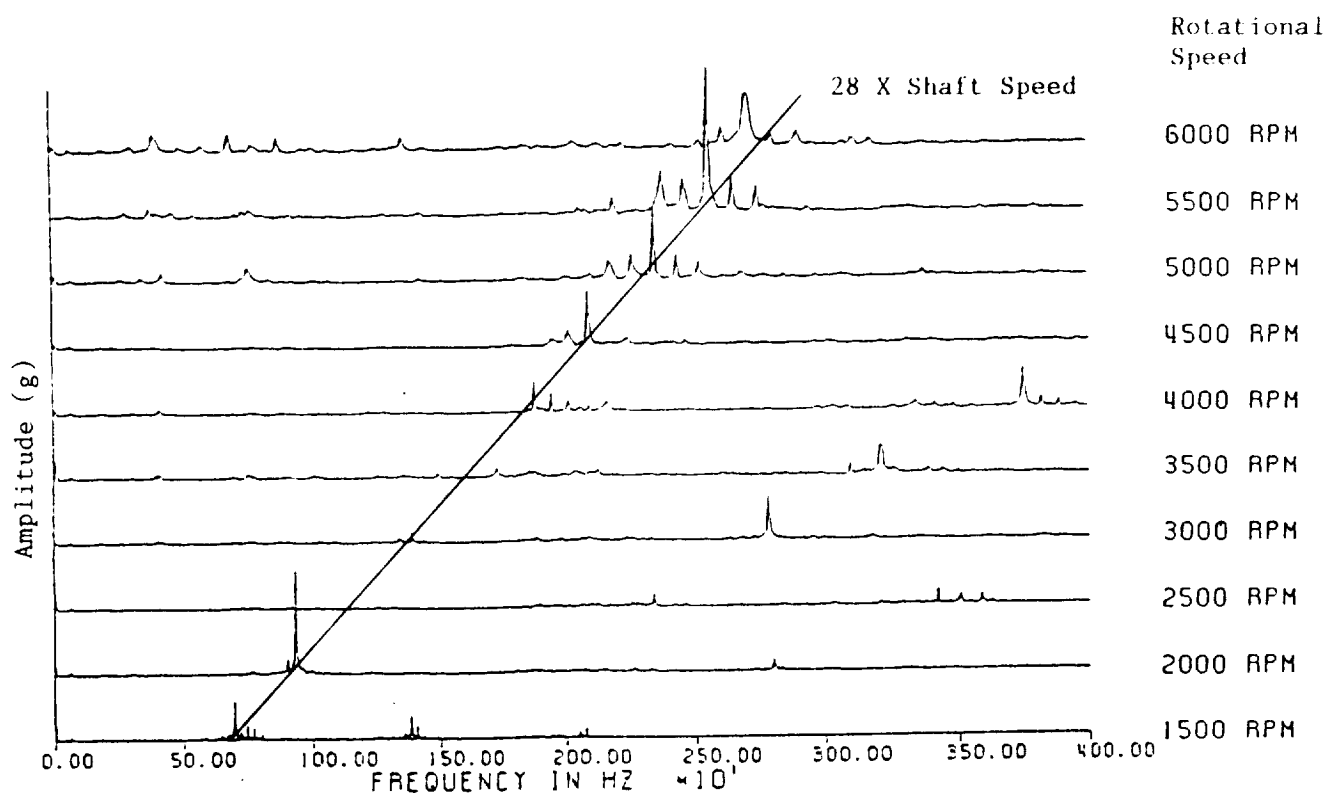


Figure 6.19A Frequency Spectra of the Z-direction Vibration of the Gear Box from Experimental Study

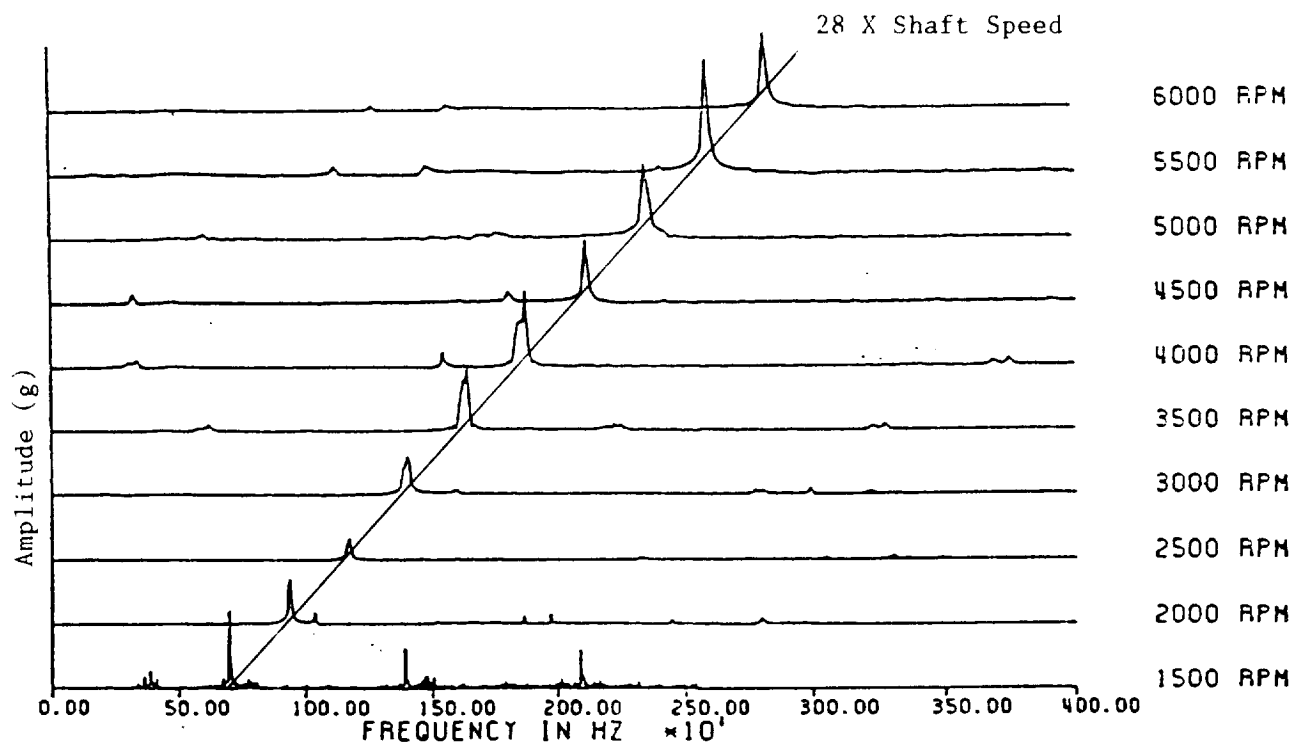


Figure 6.19B Frequency Spectra of the Z-direction Vibration of the Gear Box from Numerical Simulations

occur at the running speeds of 1500 rpm, at the tooth pass frequency of 700 Hz, and at 5500 rpm, at the tooth pass frequency of 2560 Hz. These peaks are a result of the tooth pass frequency exciting two of the major natural frequencies of the housing, namely the 658 Hz and 2536 Hz modes. The presence of other modes can be seen, however, the 658 and 2536 Hz modes, when excited by the gear mesh frequency, dominate the spectra.

When comparing the predicted vibration spectra with the measured spectra, it was found that although the actual amplitude values did not always agree, the general trends of the spectra were very similar. The predicted vibration spectra of the housing in the x-direction is given in Figure 6.17B. In comparing Figures 6.17A and 6.17B, the predicted amplitude at the gear mesh frequency at 1500 rpm is only 3% above the measured value. The comparison at 5500 rpm is not that close, where the predicted amplitude is 38% below the measured value. In comparing trends, the predicted spectra show the same gear mesh frequency induced excitation of the 658 Hz and 2536 Hz modes, as found in the measured spectra, at the running speeds of 1500 and 5500 rpm, respectively.

Figures 6.18A and 6.18B, and Figures 6.19A and 6.19B present the comparison of predicted and measured housing vibration spectra in the y and z directions, respectively. The results of the comparison are the same as those presented for the housing vibration in the x-direction (Figure 6.17A and 6.17B). Actual values of the components in the spectra were not always in good agreement, however, the general trends between the predicted and measured housing vibration spectra were very similar. Also, as seen in Figure 6.19B, at the 1500 rpm speed, the model predicts the second and third harmonic of the gear mesh frequency. As shown in Figure 6.19A, the measured vibration confirms the presence of these two harmonics at the 1500 rpm running speed.

7. CORRELATION OF NOISE AND VIBRATION

In order to predict the noise generated in a gear transmission system, a two-phase procedure was developed to correlate the noise and vibration data obtained during experimental studies; namely, i) linear correlation through transfer functions, and ii) nonlinear correlation through hypercoherence functions. The relationships derived in this study are used to predict gear box noise from the numerical simulations of the gear box vibrations. A detailed description of the procedures used are presented in the following sections.

7.1 Correlation of Experimental Noise and Vibration Data

In this experiment, a new set of gears consisting of two identical 25-tooth gears were installed in the gear box shown in Fig. 5.2. While the vibration of the gear box surfaces was monitored by accelerometers, as described in section 6.2, the noise data was obtained by microphones, as described in section 6.3. The vibration data for the top surface of the gear box for operating speeds of 3000, 4000, and 5000 rpm are shown in Fig. 7.1, with the corresponding noise data given in Fig. 7.2.A and 7.2.B. Figure 7.3 presents the frequency and power spectra of both the vibration and noise signals at 3000 rpm running speed. Note that in the vibration spectrum, a small frequency component exists at the mesh frequency of 1250 Hz with two very large components at 3-times the mesh frequency (3750 Hz), and 4-times mesh frequency (5000 Hz). In the noise spectrum, while frequency components of considerable magnitudes are observed at the mesh frequency of 1250 Hz, and at 2 and 3-times mesh frequency (2500 and 3750 Hz), a large amplitude frequency component is also noticed at 400 Hz. This 400 Hz frequency component does not coincide with any of the major vibration frequencies at the top surface of the gear box. A closer examination of the

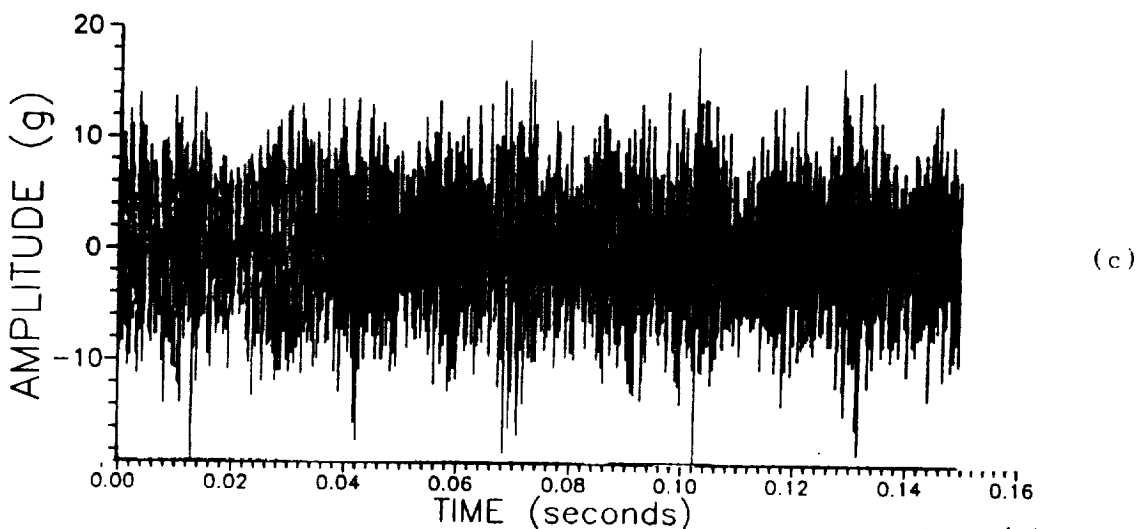
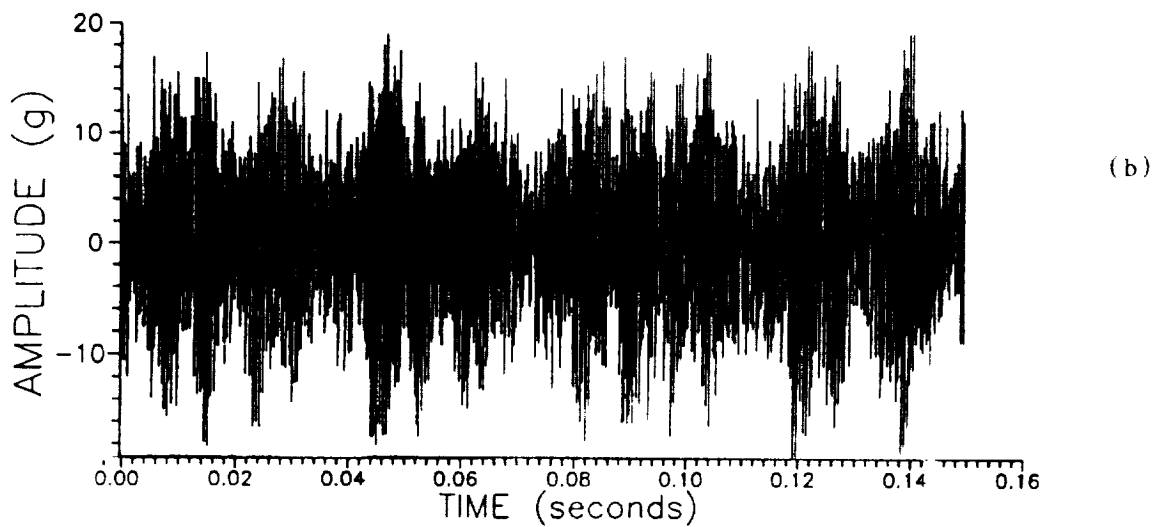
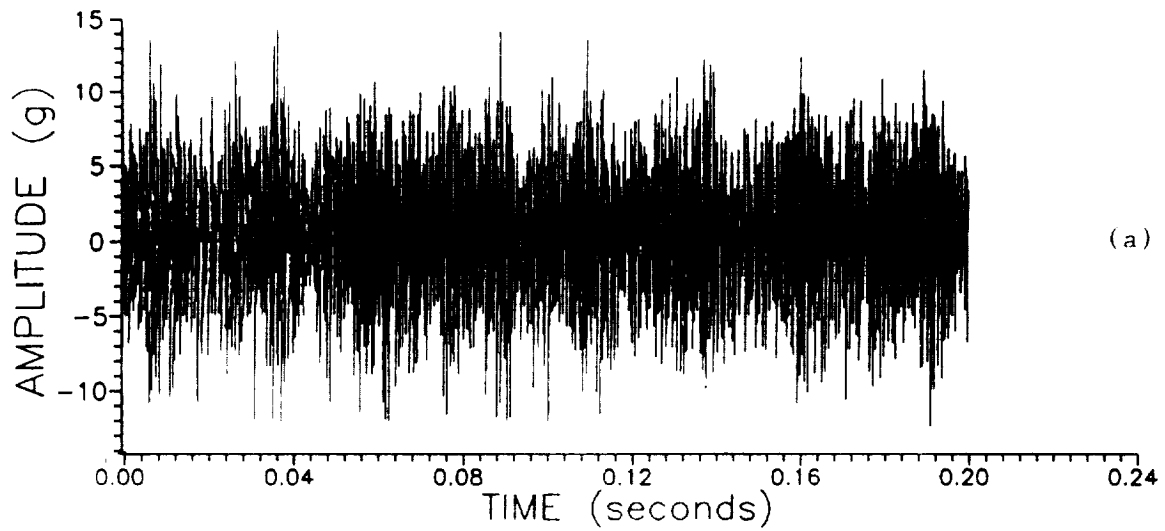


Figure 7.1 Time vibration signal at top cover of the gear box with rotor operating speed
 (a) at 3,000 rpm, (b) at 4,000 rpm, and (c) 5,000 rpm

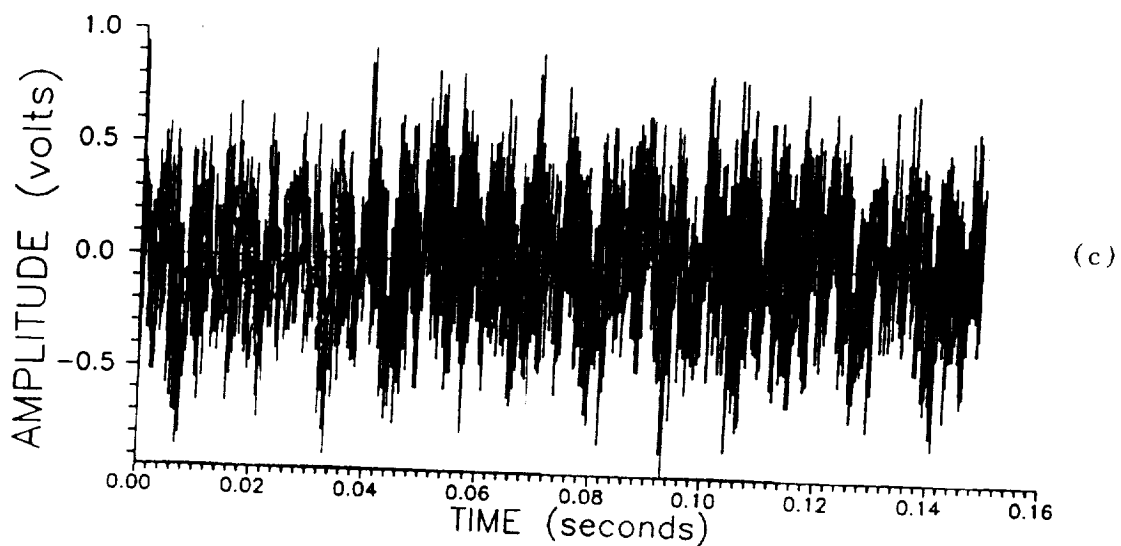
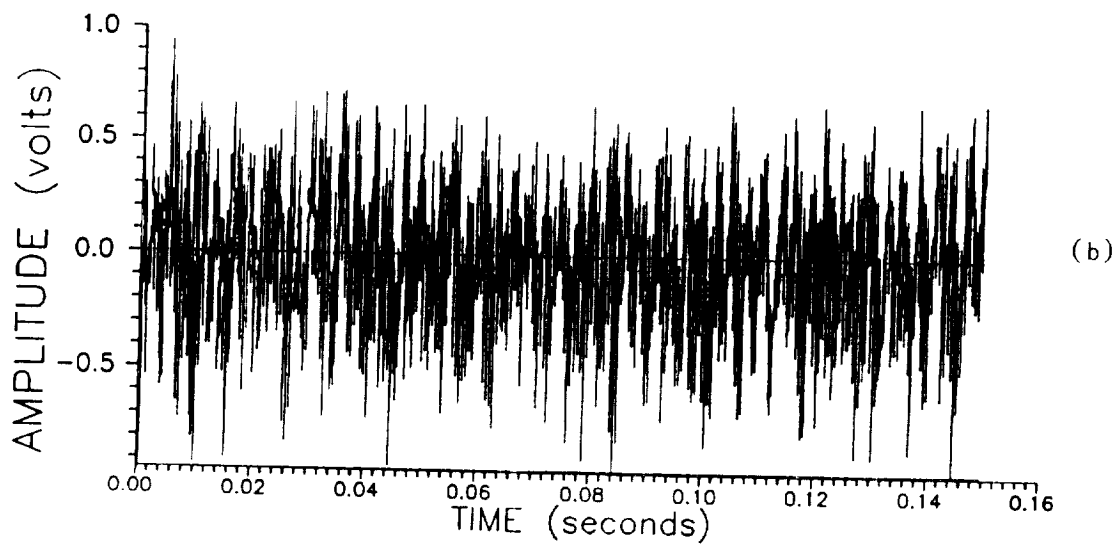
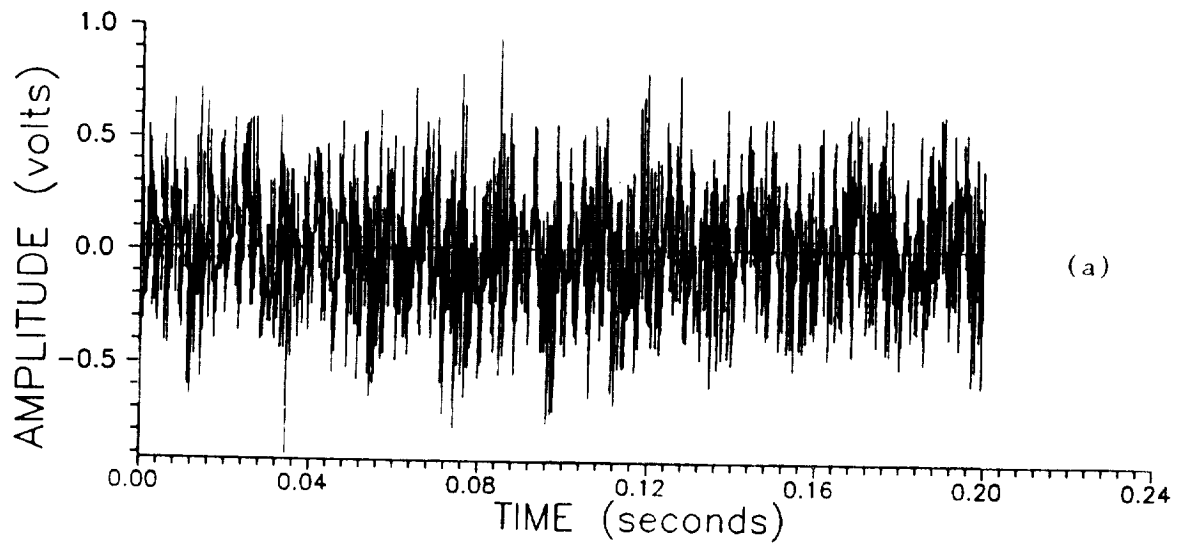


Figure 7.2 A Time noise signal from microphone no. 1 located vertically at top cover of the gear box with rotor operating speed (a) at 3,000 rpm, (b) at 4,000 rpm, and (c) at 5 000 rpm

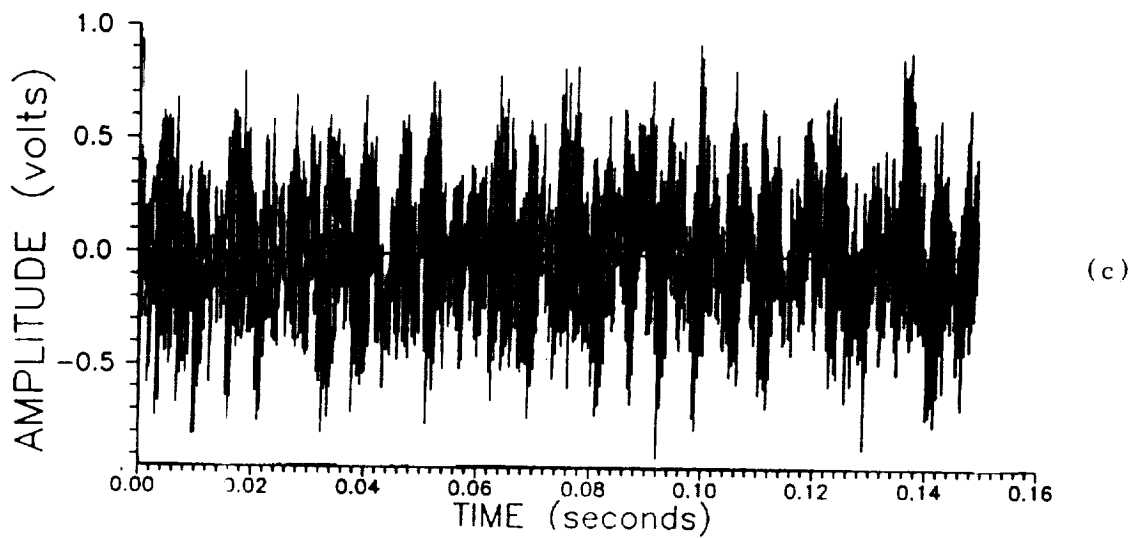
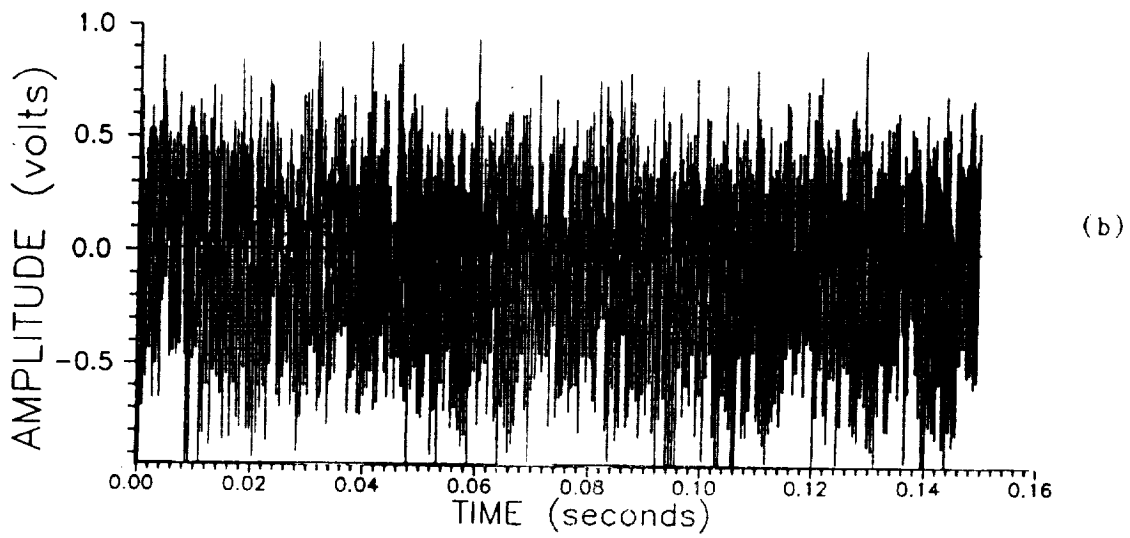
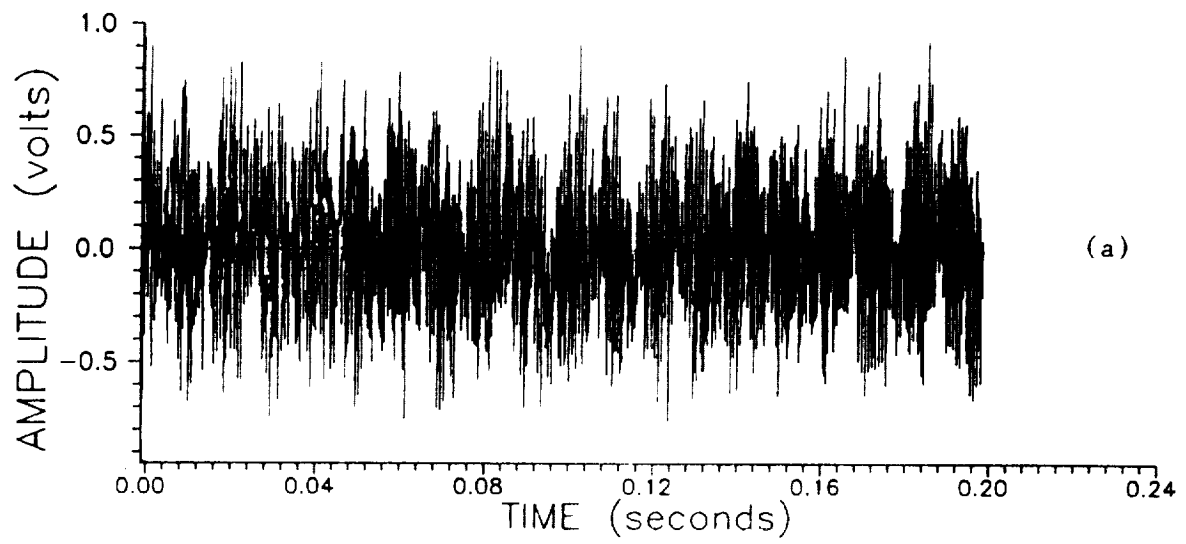


Figure 7.2B Time noise signal from microphone no. 2 located 45-degrees at top cover of the gear box with rotor operating speed (a) at 3,000 rpm, (b) at 4,000 rpm, (c) at 5,000 rpm

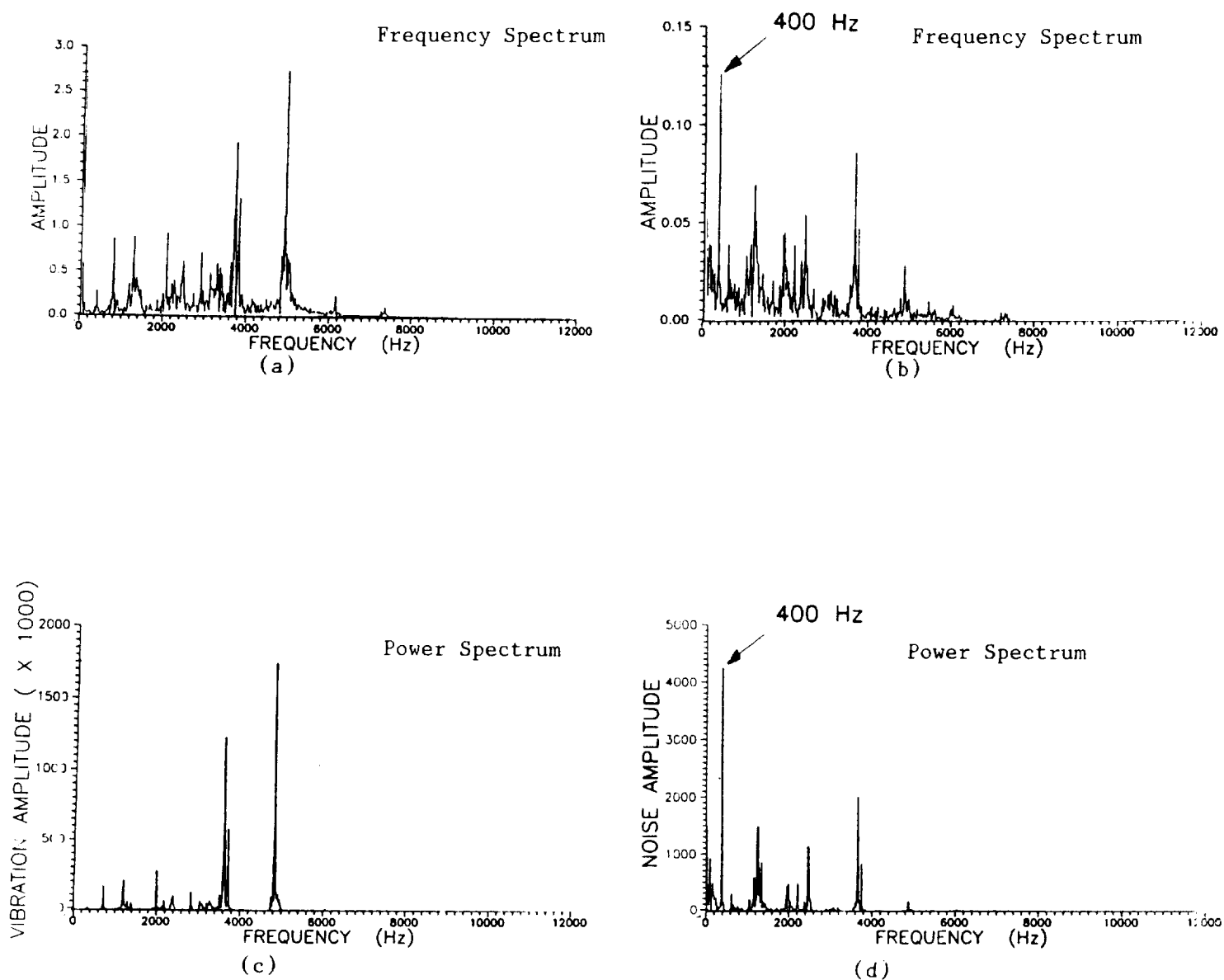


Figure 7.3 Frequency spectrum for (a) vibration, (b) noise from microphone no. 1, and power spectrum for (c) vibration, (d) noise from microphone no. 1, at the operating speed of 3,000 rpm.

system dynamic characteristics reveals that the 400 Hz frequency is an excitation of one of the natural frequencies of the rotor system, which has a very small amplitude in the gear box vibration spectrum. A logical explanation is that noise is being produced at the rotor-gear system at 400 Hz and is not being transferred to the vibration of the gear box surface. This phenomenon is further verified by the very large amplitude of the vibration-to-noise transfer function at 400 Hz as given in Fig. 7.4A. A linear coherence function between the noise and vibration signals is also given in Fig. 7.4B.

Figure 7.5 shows the comparison of the frequency and power spectra between the results of the gear box vibrations with the noise signal from microphone No. 2 (45 degrees from vertical). Note that in this case, the two signals are much better correlated. In Fig. 7.5B, the noise spectrum shows the largest component at 3-times mesh frequency (3750 Hz) and two other major components at mesh frequency (1250 Hz) and 4-times mesh frequency (5000 Hz). Although a sizable component still exists at 400 Hz, it is relatively small compared with those of the multiples of the mesh frequency. Again, the logical explanation for this phenomenon is due to the fact that the 400 Hz frequency component produced by the rotor will not radiate through the gear box surface and cannot be picked up by the 45 degree microphone. The vibration-to-noise transfer and coherence functions for the second microphone are given in Fig. 7.6.

Figures 7.7 and 7.8 present respectively the frequency and power spectra, and the transfer and coherence functions of the gear box system at the rotor running speed of 4000 rpm. The frequency spectra in Fig. 7.7 shows a significant frequency component at the 3-times mesh frequency (5000 Hz) while major noise components are noted at the rotor natural frequency of 400 Hz and the primary mesh frequency (1667 Hz). The results are attributed

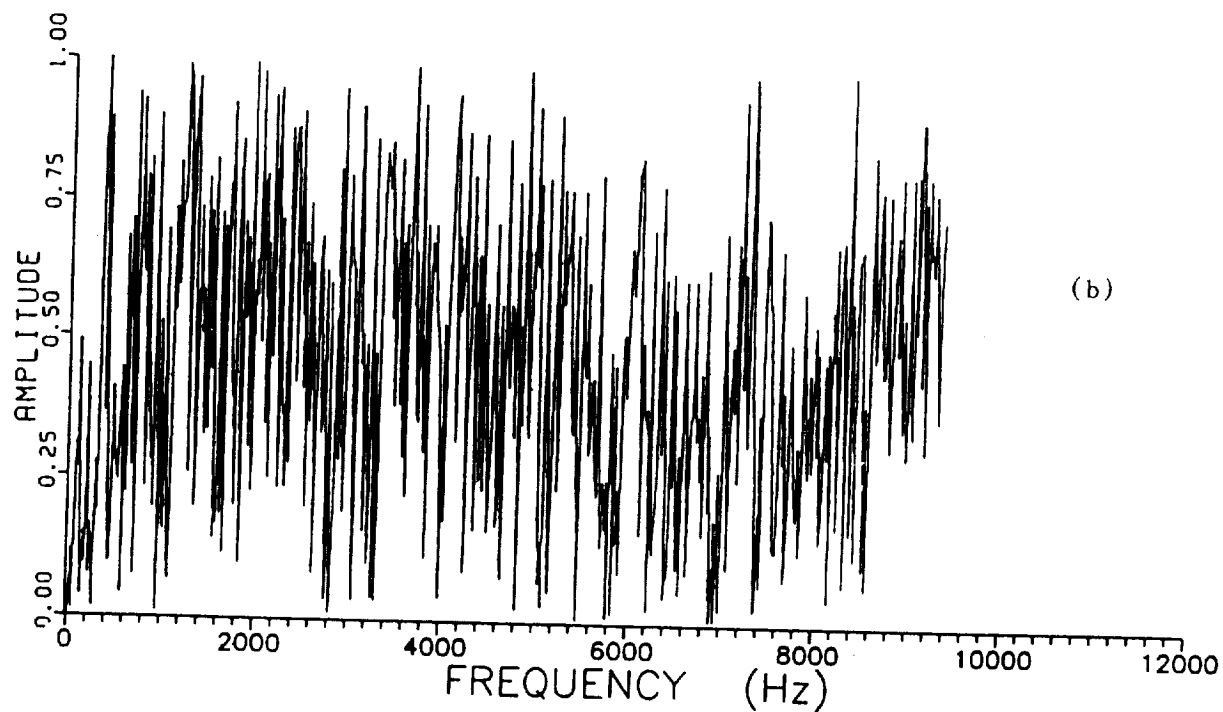
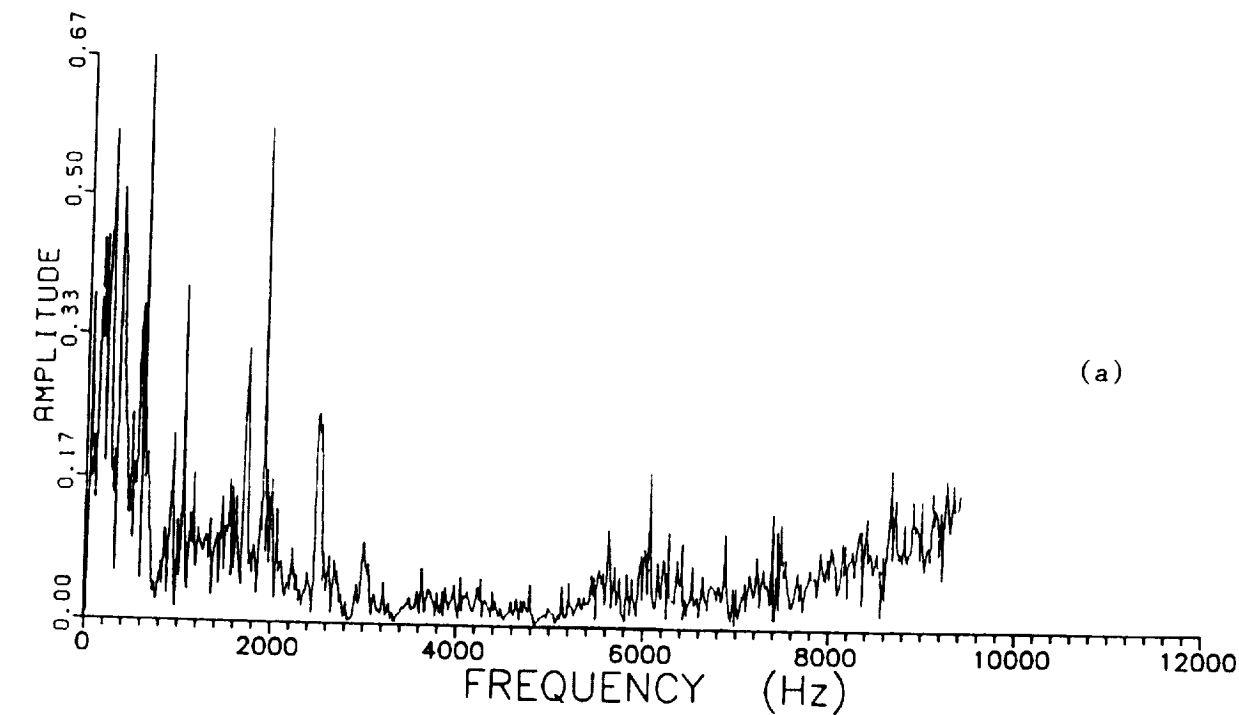


Figure 7.4 (a) Transfer function and (b) coherence function, between noise (microphone no. 1) and vibration at the operating speed of 3,000 rpm

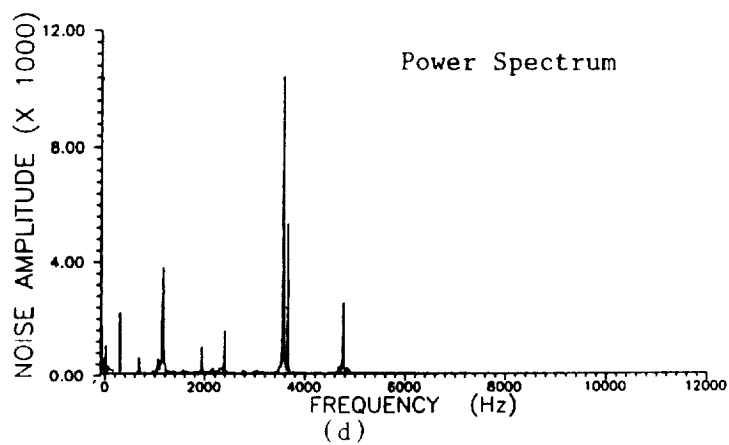
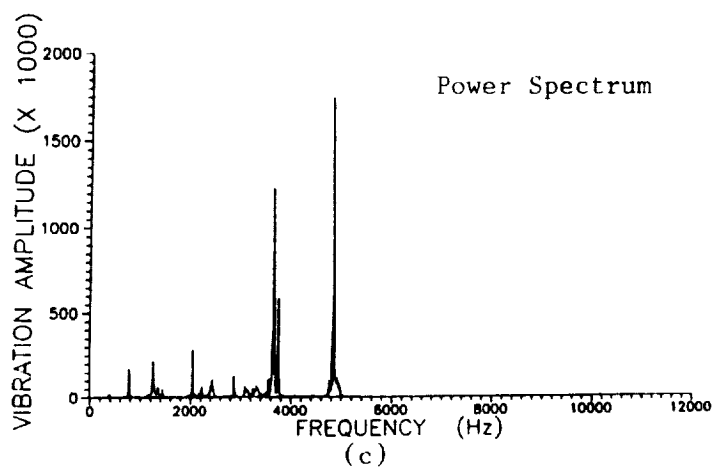
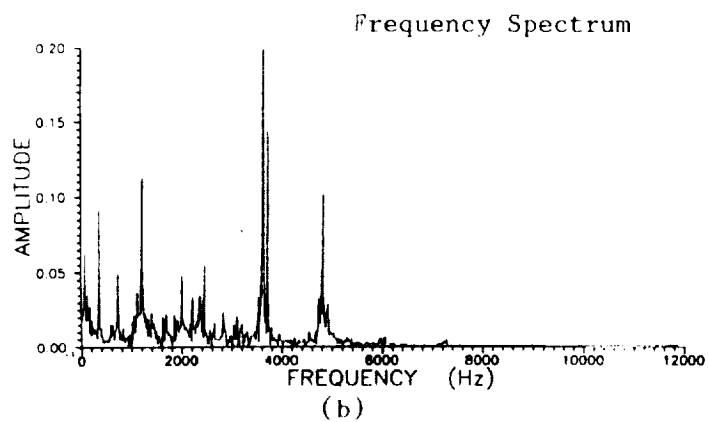
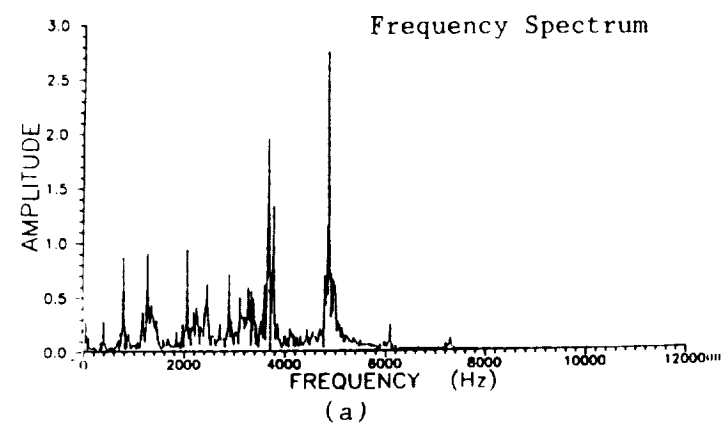


Figure 7.5 Frequency spectrum for (a) vibration, (b) noise from microphone no. 2, and power spectrum for (c) vibration, (d) noise from microphone no. 2, at the operating speed of 3,000 rpm.

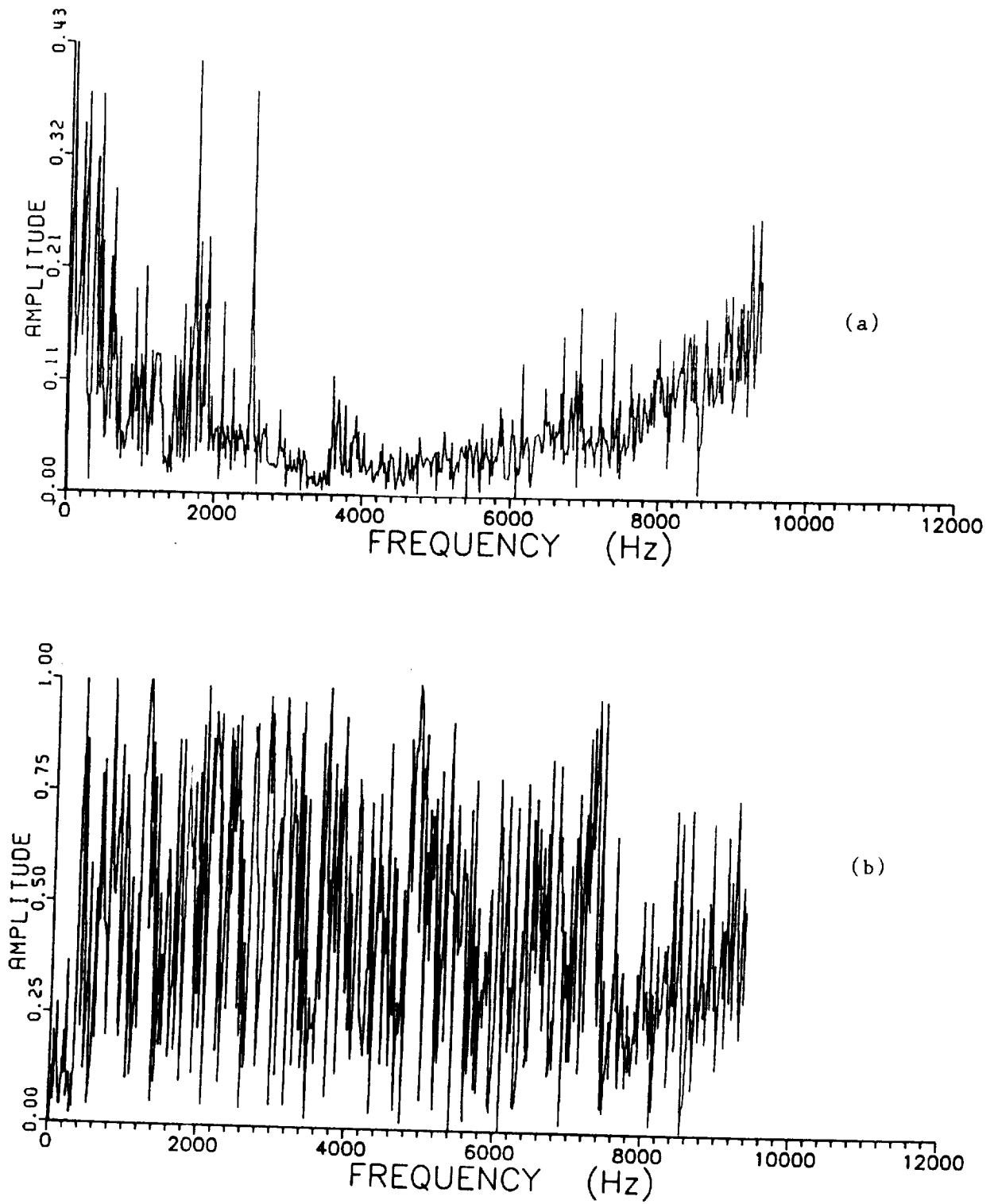


Figure 7.6 (a) Transfer function and (b) coherence function, between noise (microphone no. 2) and vibration at the operating speed of 3,000 rpm

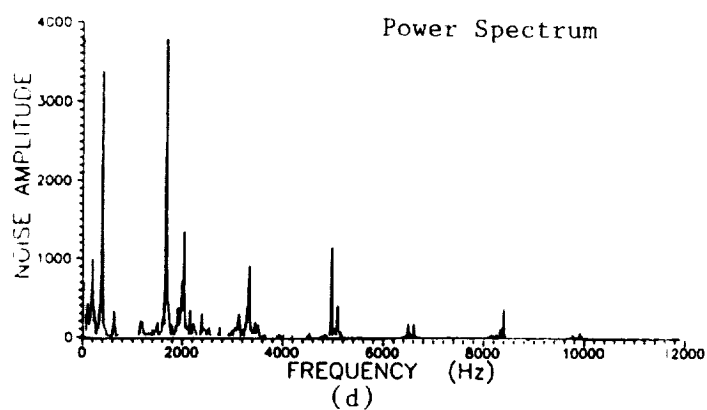
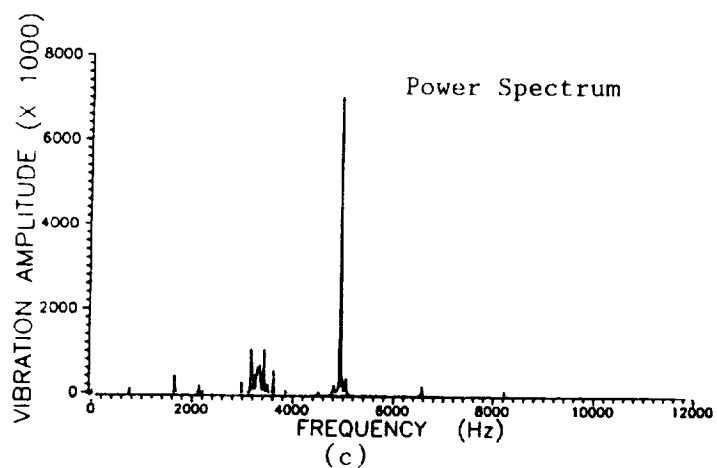
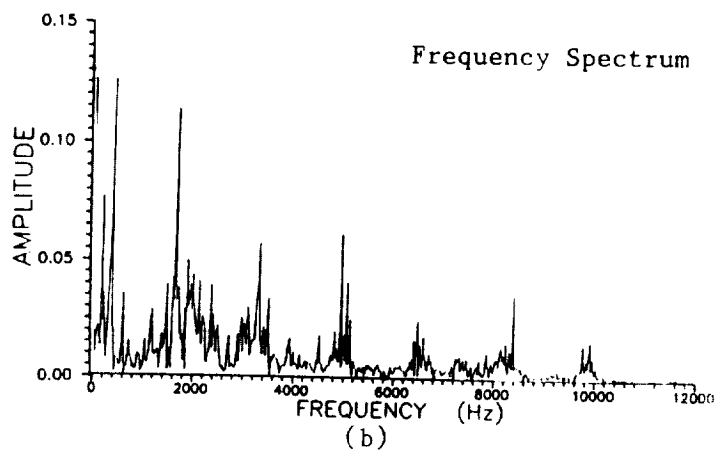
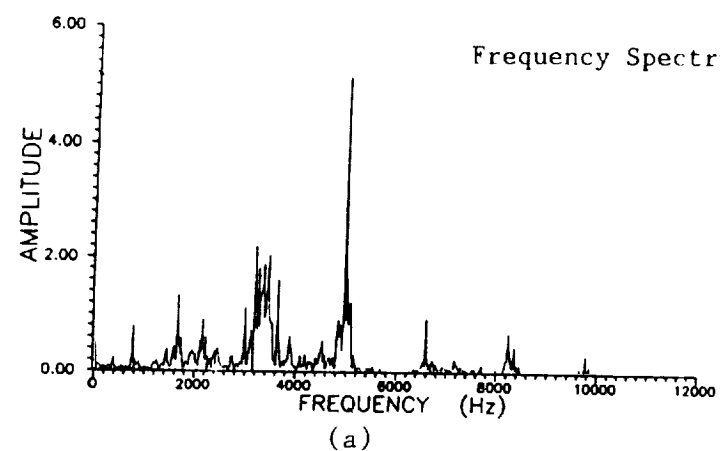


Figure 7.7 Frequency spectrum for (a) vibration, (b) noise from microphone no. 1, and power spectrum for (c) vibration, (d) noise from microphone no. 2, at the operating speed of 4,000 rpm.

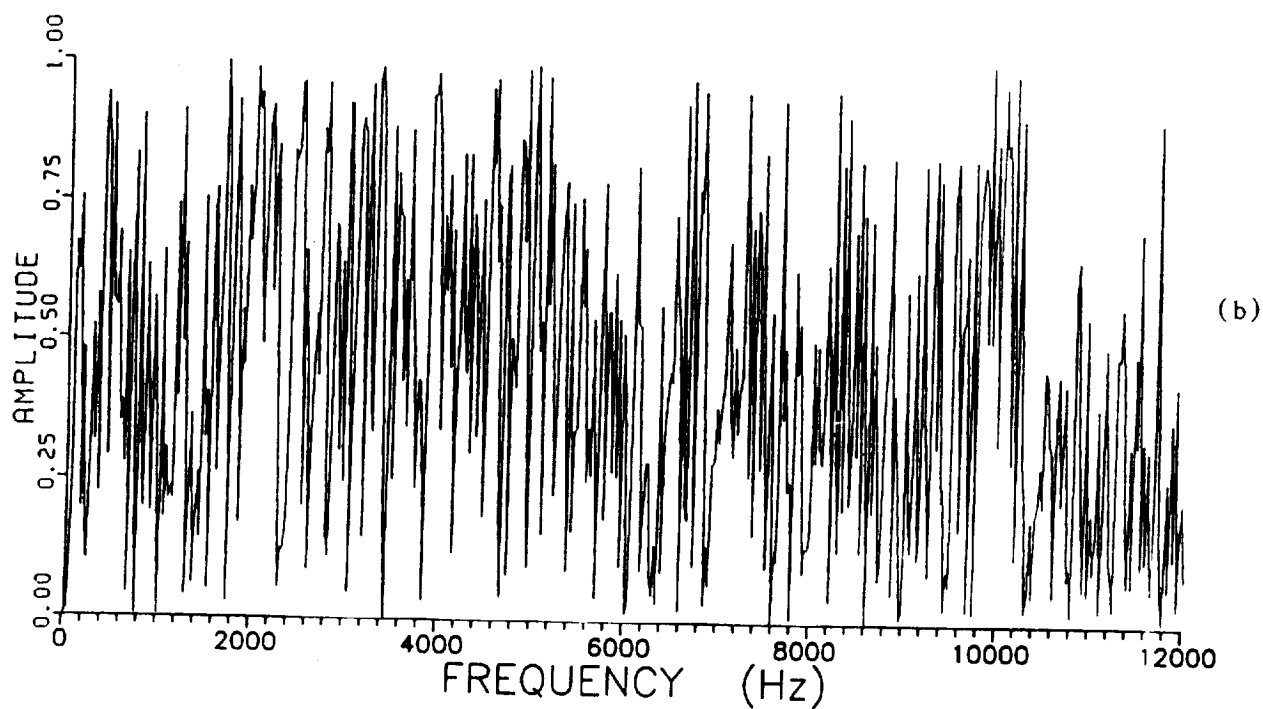
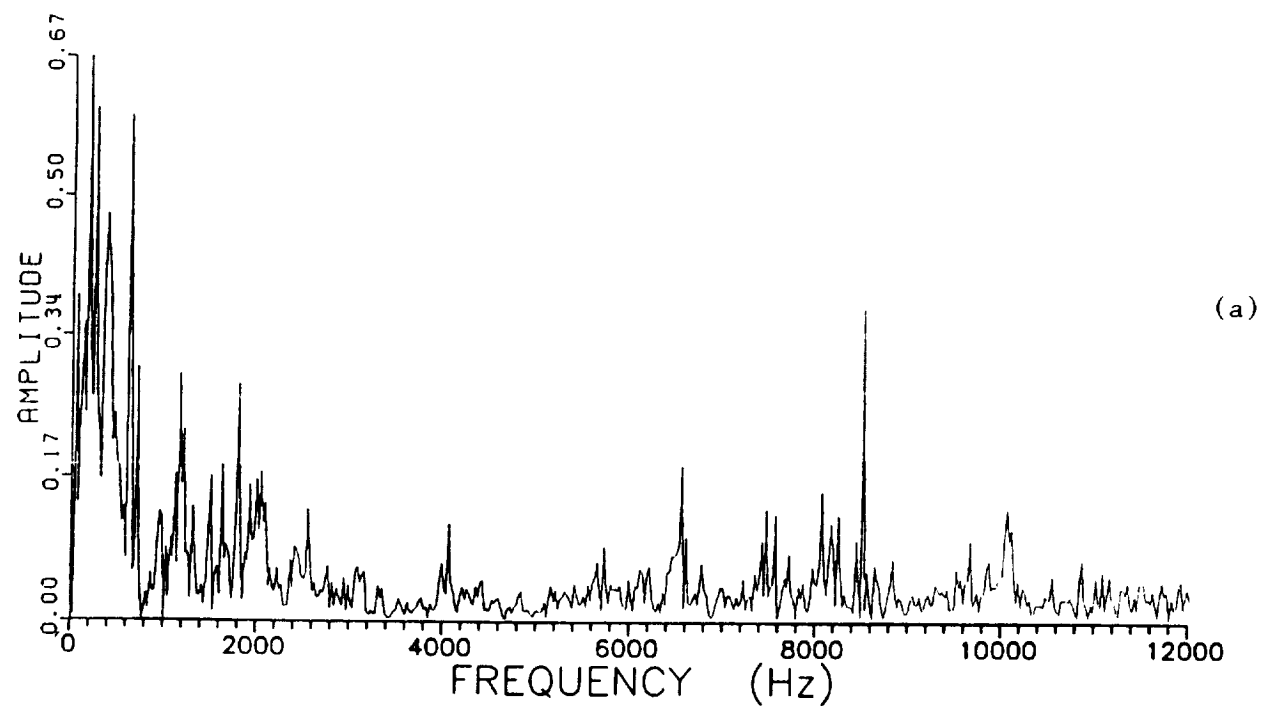


Figure 7.8 (a) Transfer function and (b) coherence function, between noise (microphone no. 1) and vibration at the operating speed of 4,000 rpm

to the fact that the noise due to the natural frequencies of the rotor system do not effectively contribute to the vibration of the gear box. The significant amplitudes in the vibration spectrum, other than the original mesh frequency, is due to the excitation of the natural frequencies of the gear box at the multiples of the mesh frequency. In the case of the 3000 rpm running speed, natural frequencies of 3750 rpm (3-times mesh frequency) and 5000 rpm (4-times) are excited. Figure 7.9 shows the comparison of the frequency spectra of the second microphone. Note again, that the 400 Hz component diminishes while the noise frequency components of the basic mesh frequency and its multiples are the major contributors. The transfer and coherence functions for this case is given in Fig. 7.10.

For the case of a rotor running speed of 5000 rpm, the frequency and power spectra of the gear box vibration and noise are given in Fig. 7.11. Note that the major vibration frequencies excited are the basic mesh frequency at 2083 Hz, 2-times at 4166 Hz, and 3-times at 6250 Hz. The magnitudes of these components are relatively lower than those at the 4000 rpm running speed. This is due to the fact that these frequencies are not close to any of the major vibration modes of the gear box. Even though at this running speed the noise frequency spectrum shows a more consistent trend with the vibration spectrum, a strong frequency component still exists at 400 Hz, which is not detected in the vibration spectrum. The transfer and coherence spectra for this case is given in fig. 7.12. For the second microphone, the noise signal spectrum, Fig. 7.13, shows a similar trend as those of microphone No. 1, with a considerably smaller 400 Hz component. The transfer and coherence function for this case is given in Fig. 7.14.

From the above discussion, it can be concluded that in the frequency domain, most of the noise components, other than the 400 Hz contributions, exist at multiples of the mesh

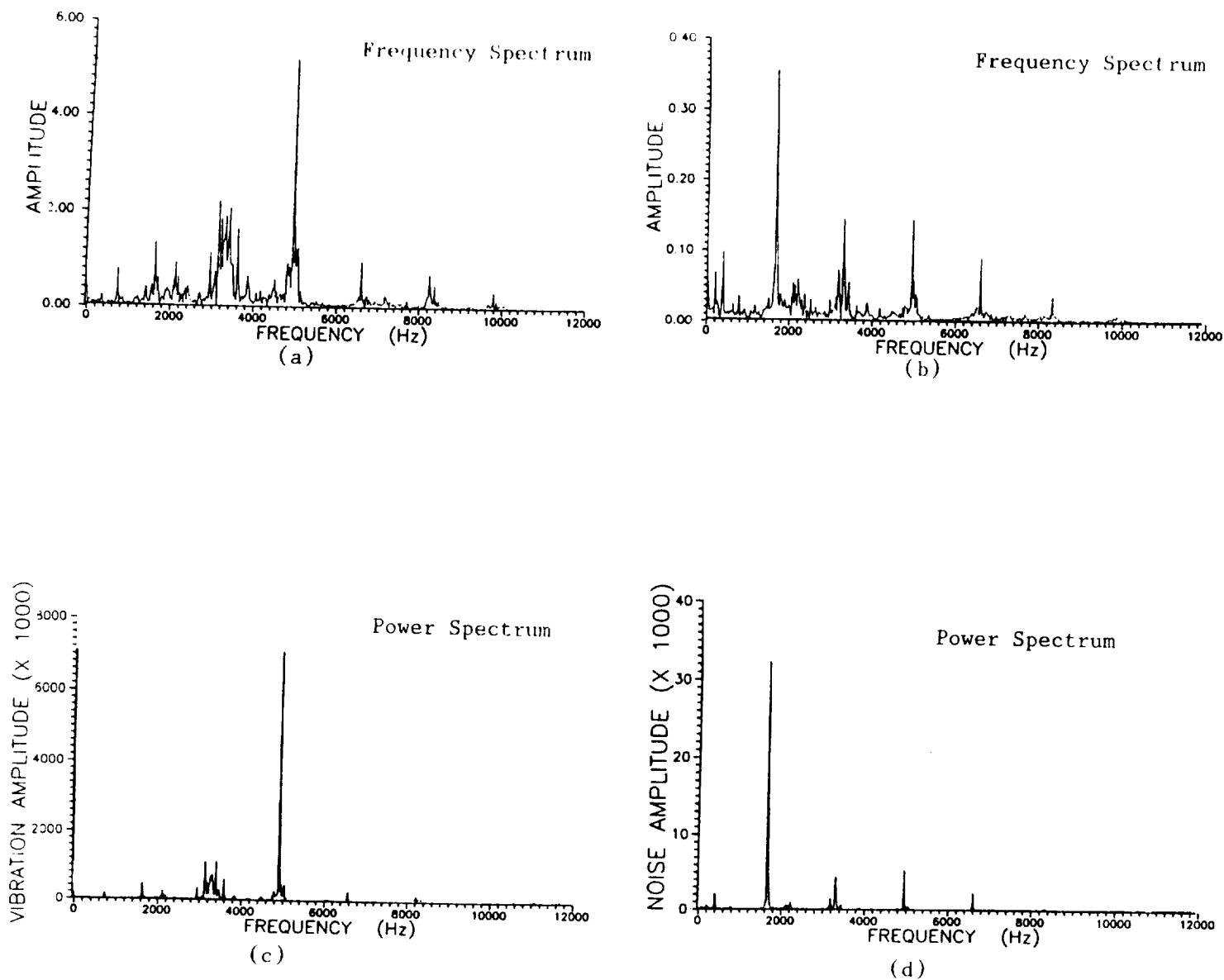


Figure 7.9 Frequency spectrum for (a) vibration, (b) noise from microphone no. 2, and power spectrum for (c) vibration, (d) noise from microphone no. 2, at the operating speed of 4,000 rpm.

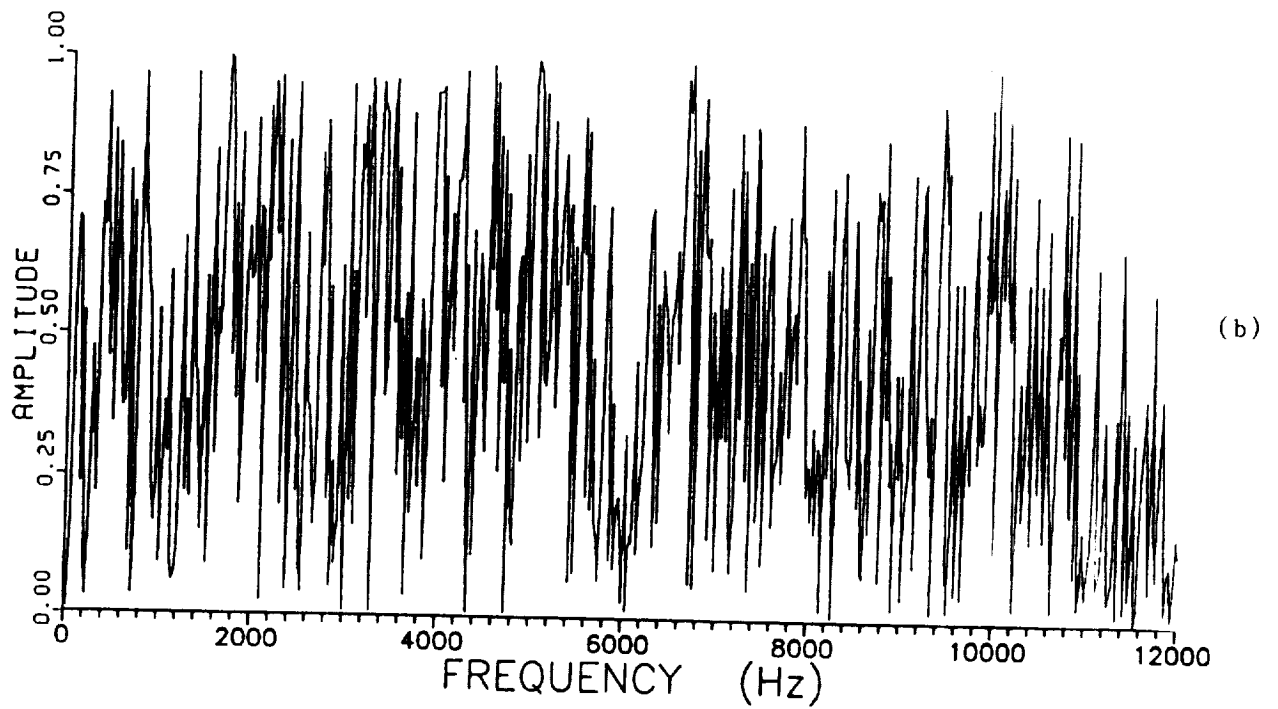
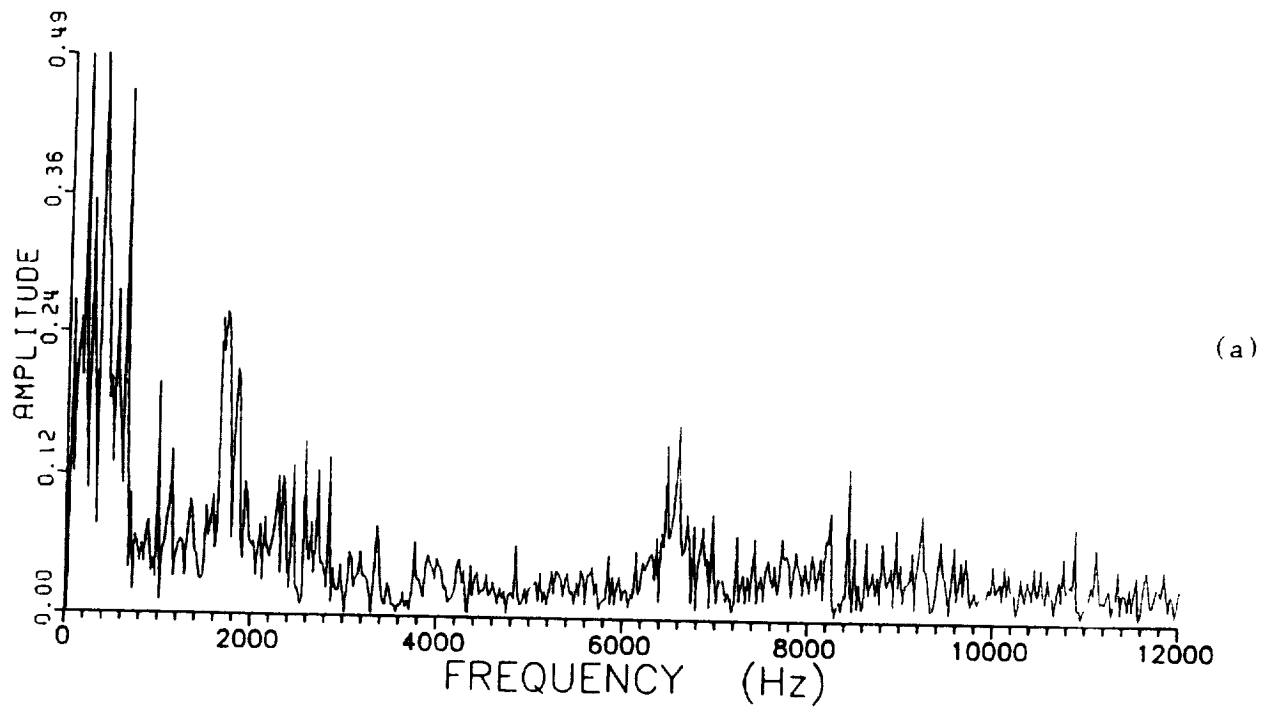


Figure 7.10 (a) Transfer function and (b) coherence function, between noise (microphone no. 2) and vibration at the operating speed of 4,000 rpm

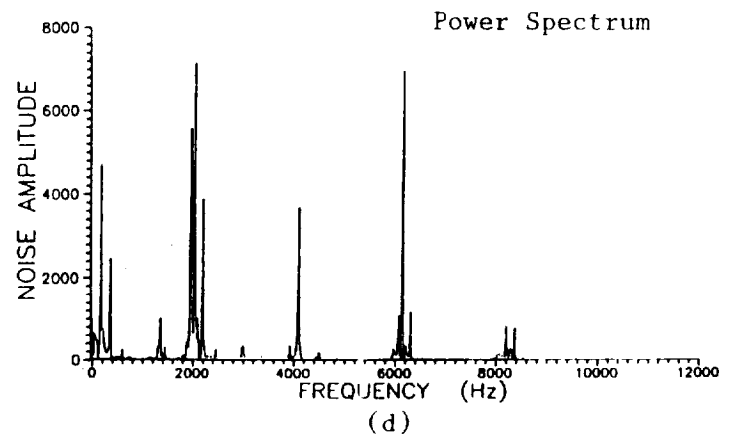
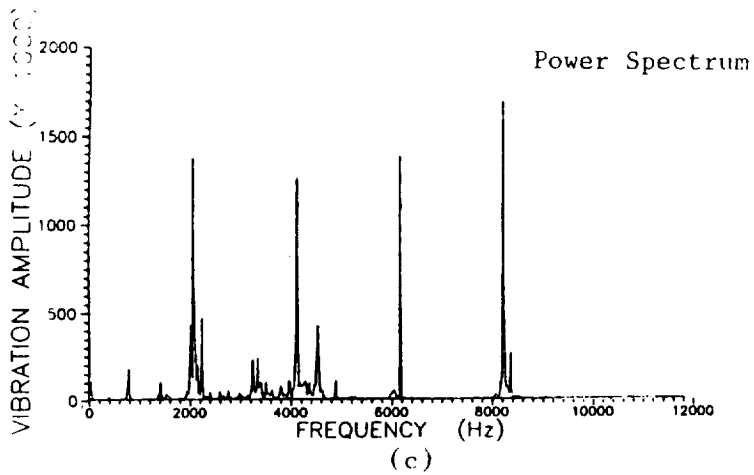
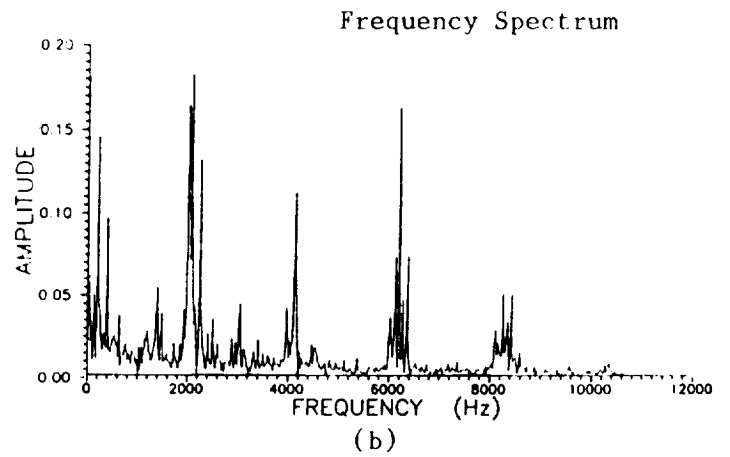
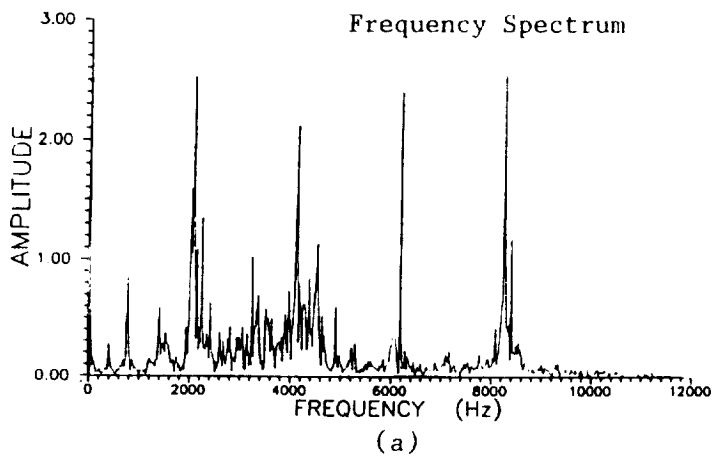


Figure 7.11 Frequency spectrum for (a) vibration, (b) noise from microphone no. 1, and spectrum for (c) vibration, (d) noise from microphone no. 1, at the operating speed of 5,000 rpm.

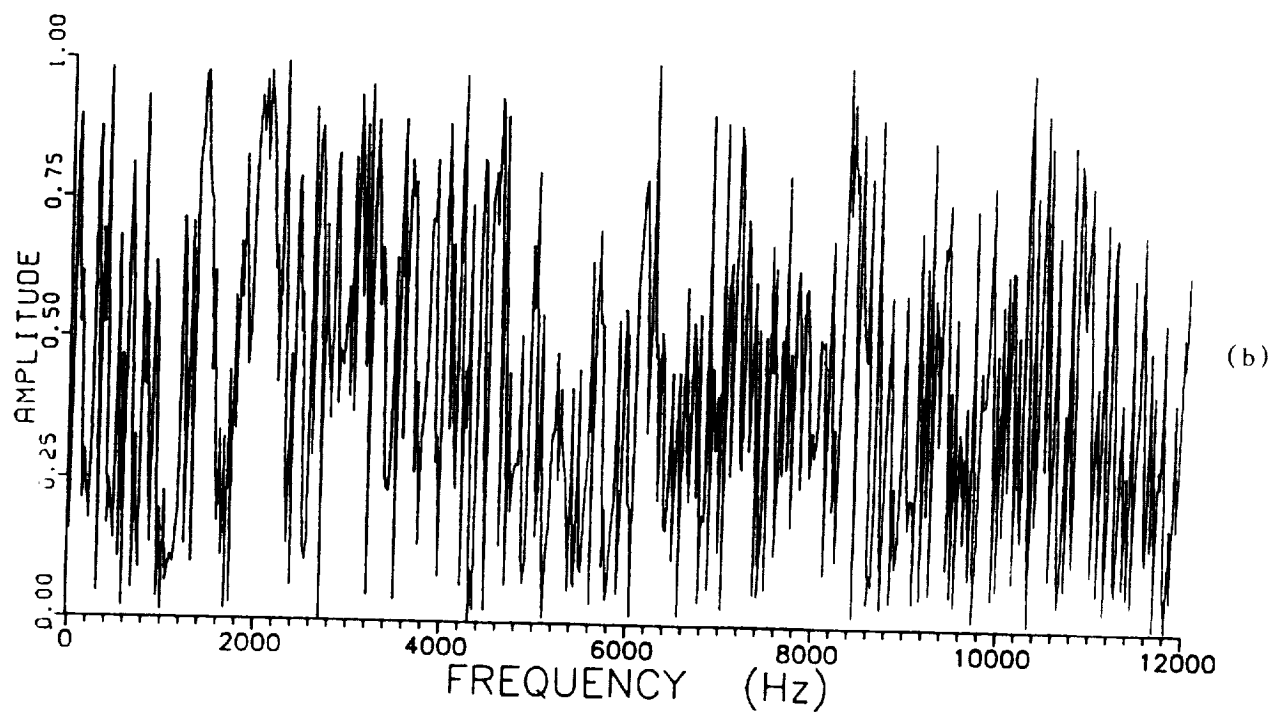
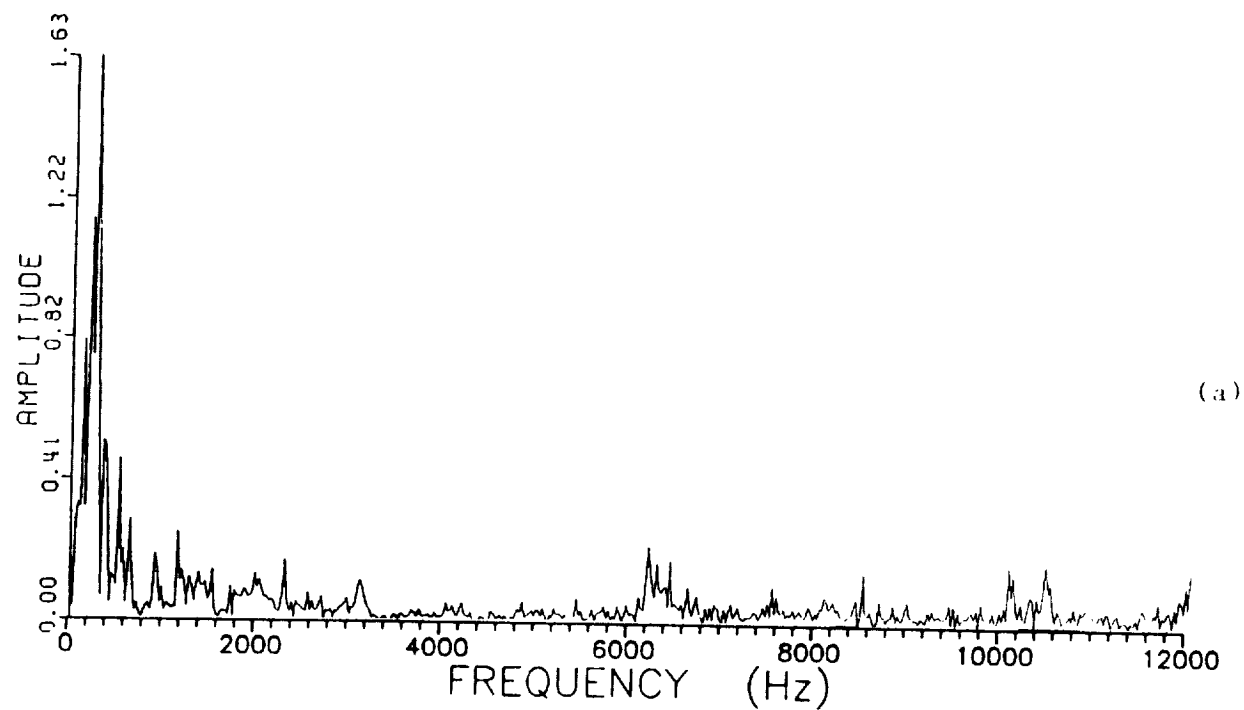


Figure 7.12 (a) Transfer function and (b) coherence function, between noise (microphone no. 1) and vibration at the operating speed of 5,000 rpm

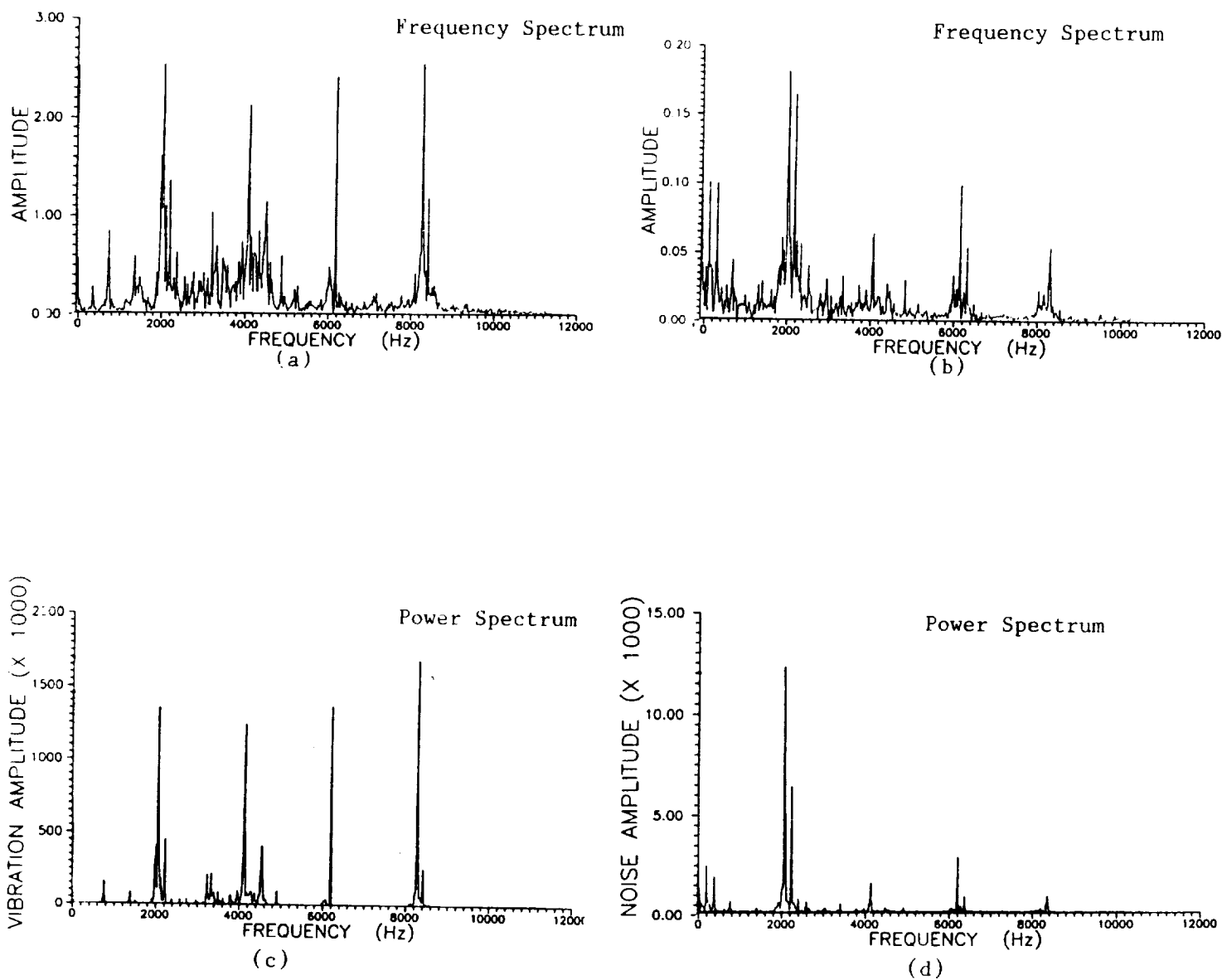


Figure 7.13 Frequency spectrum for (a) vibration, (b) noise from microphone no. 2, and power spectrum for (c) vibration, (d) noise from microphone no. 2, at the operating speed of 5,000 rpm.

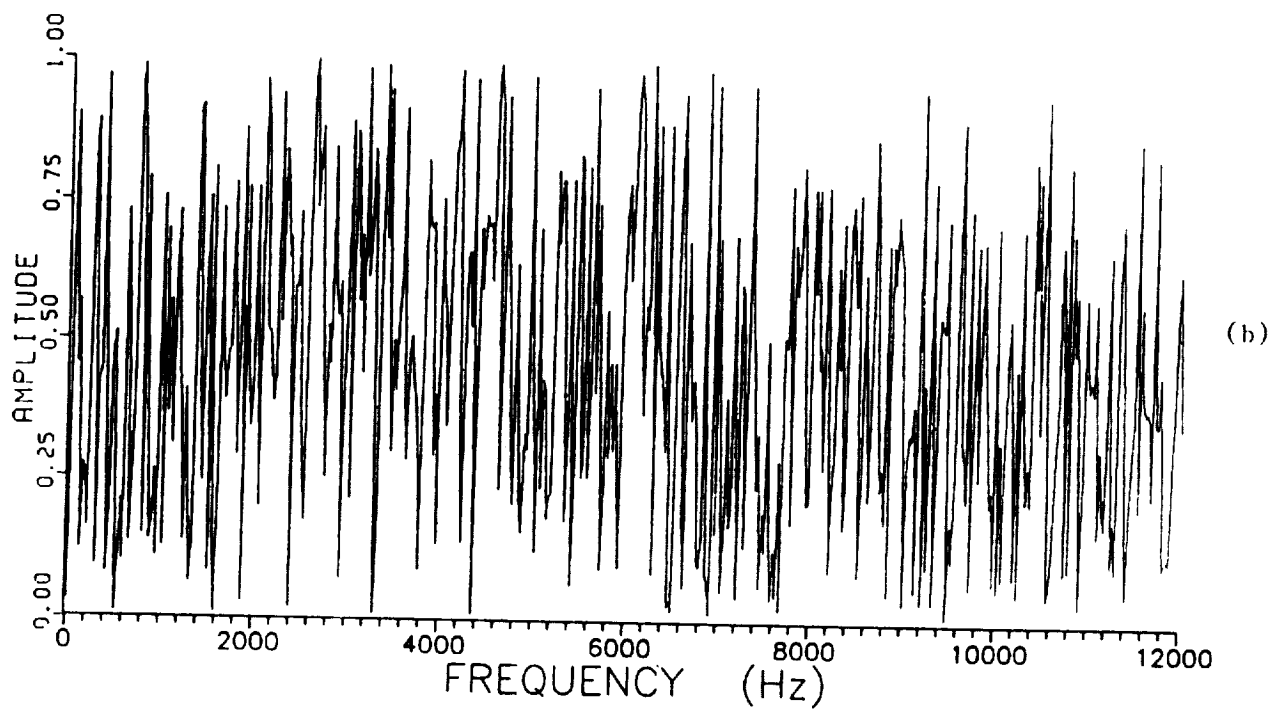
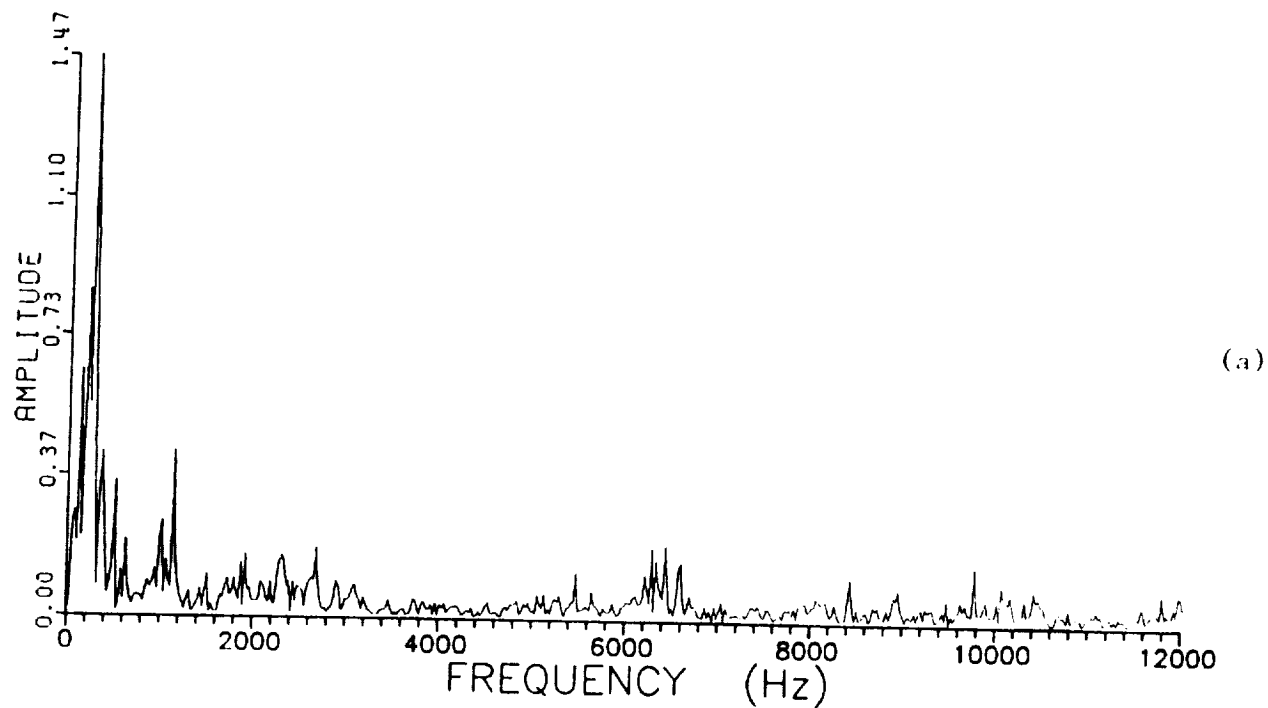


Figure 7.14 (a) Transfer function and (b) coherence function, between noise (microphone no. 2) and vibration at the operating speed of 5,000 rpm

frequency. **The Nonlinear Hypercoherence Function**, developed by NASA Marshall Space Flight Center for the Space Shuttle Noise Test Program, is used for the second phase of this study. The Hypercoherence Function [Jong 1986] will establish a nonlinear relationship between the basic frequency component with its multiple harmonics. Figure 7.15 shows the Hypercoherence functions of the noise signals for the 3000, 4000, and 5000 rpm cases. The magnitudes of the components in the harmonics are the nonlinear relationship of that component with the basic harmonic frequency. These relationships provide a picture of the relative contribution of the higher harmonics with respect to the basic frequency. Note that as the running speed increases, the magnitudes of the higher harmonics also increase. This is very similar to the conclusions drawn from the linear study discussed in the last paragraph. In the next section, this Hypercoherence function will be used on the numerical simulation data to examine the accuracy of the noise prediction.

7.2 Predictions of Noise by Numerical Simulations and Correlation with Experimental Results

In order to predict the noise level of the transmission system during operation, the vibrations of the gear box structure are simulated using the modal synthesis approach discussed in the previous chapters. Figure 7.16B shows the analytically predicted time vibration signal (acceleration) at the top of the casing structure at an operating speed of 3000 rpm while the corresponding experimental results are given in Fig. 7.16A. Note that the amplitudes and general shapes of the two time signals are very similar. The comparison of their frequency contents are given by the frequency spectra in Fig. 7.17. Figure 7.17A shows the frequency components of the measured vibration at the top of the gear box. Note that the major vibration components occur at the mesh frequency of 1250 Hz and at 3-times

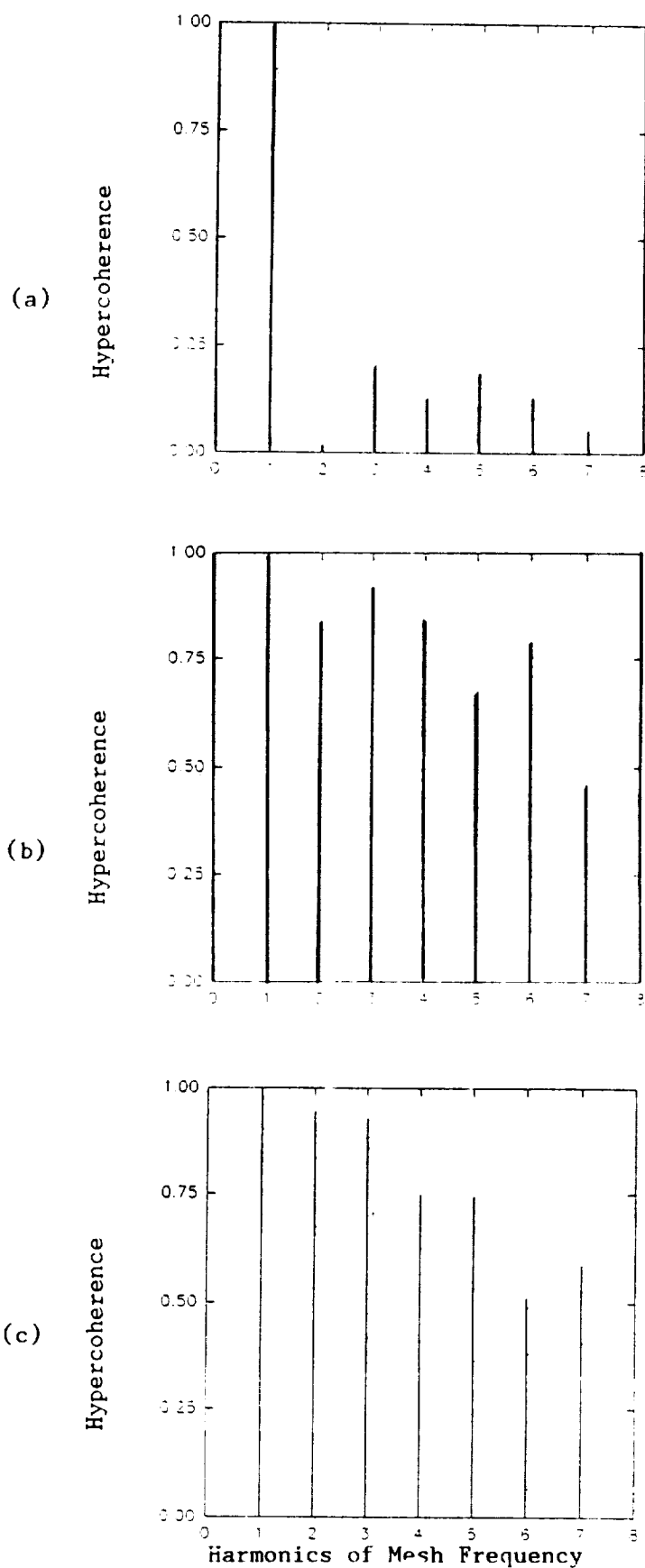


Figure 7.15 Hypercoherence function for the noise signal from microphone no. 1 (a) at 3,000 rpm, (b) at 4,000 rpm, (c) at 5,000 rpm

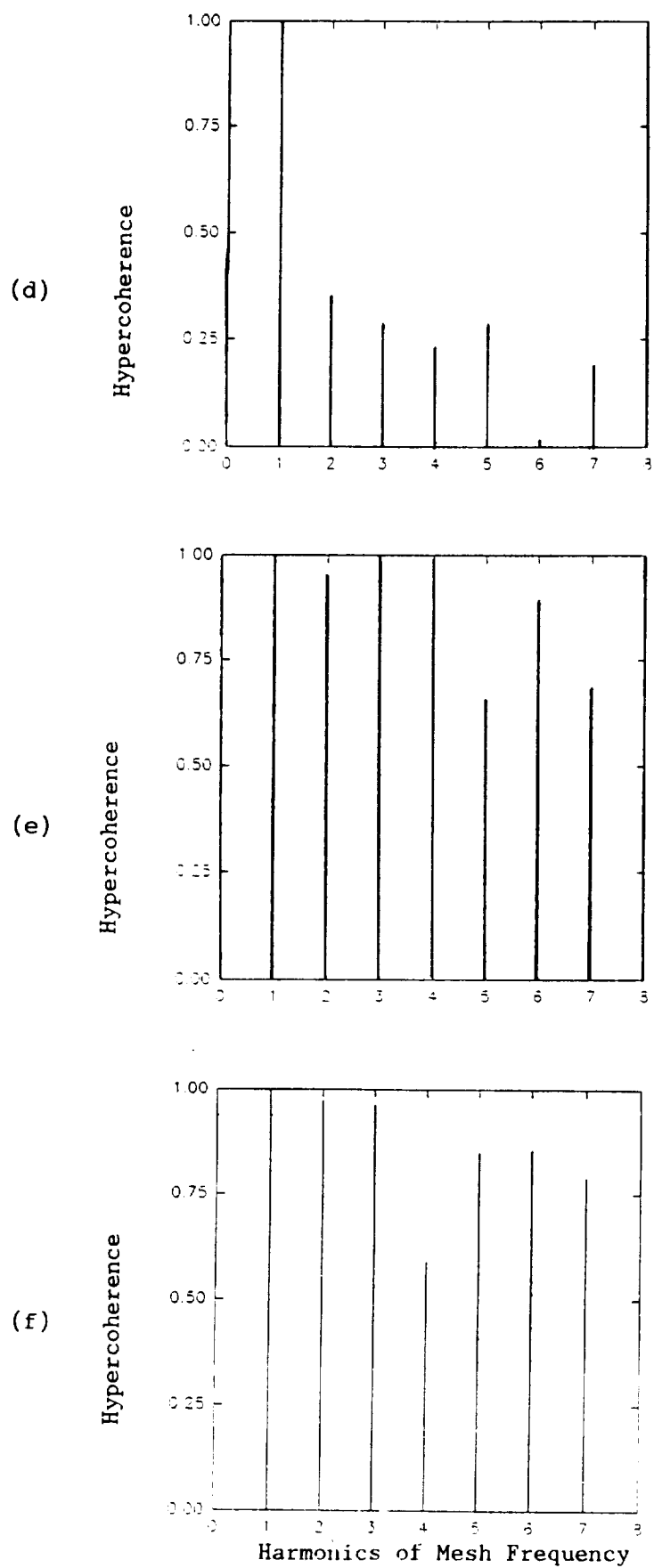


Figure 7.15 Hypercoherence function for the noise signal from microphone no. 2 (d) at 3,000 rpm, (e) at 4,000 rpm, and (f) at 5,000 rpm

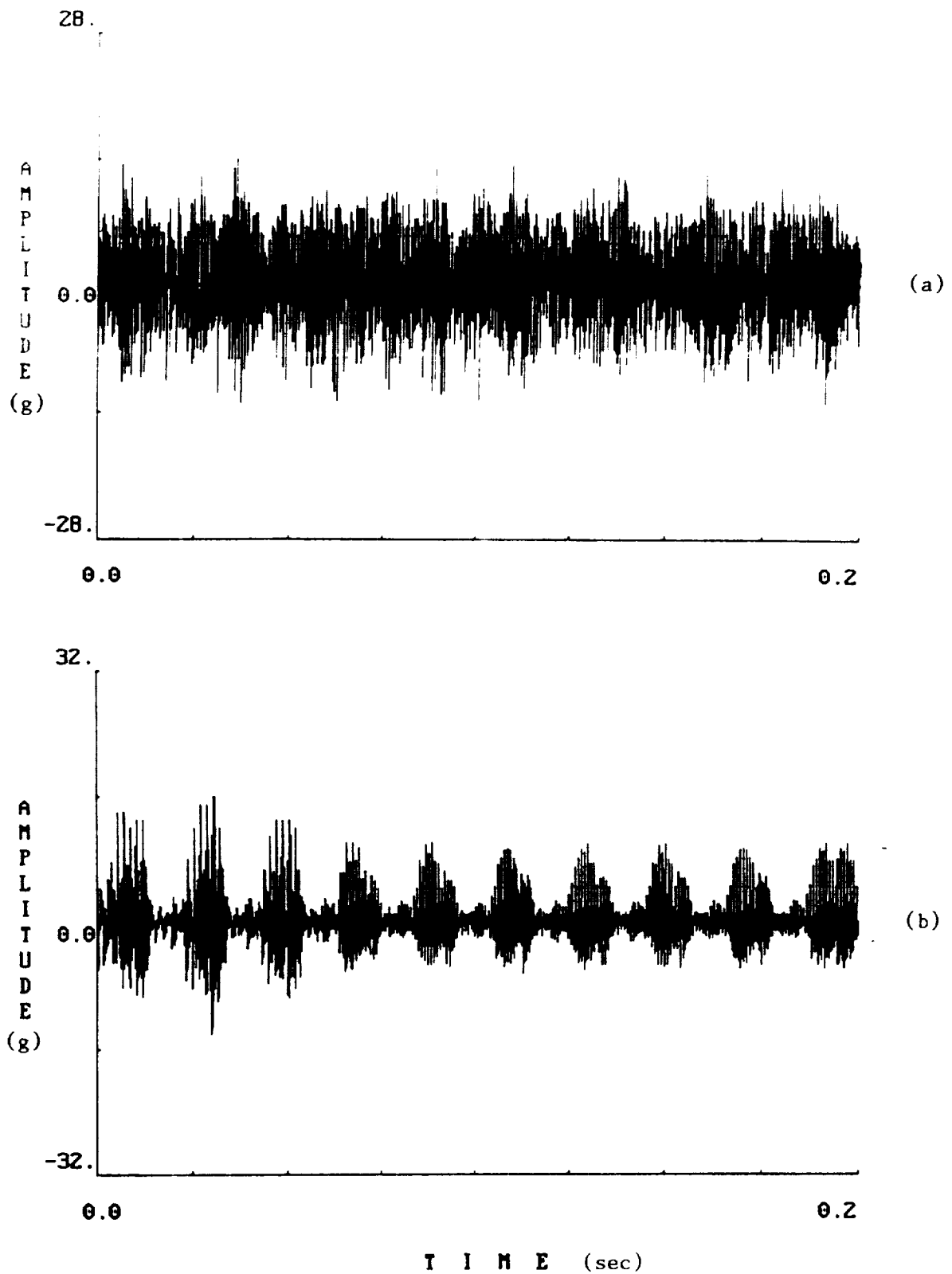


Figure 7.16 Time vibration signal at top of gear box for operating speed of 3,000 rpm from (a) experimental data, and (b) numerical simulations

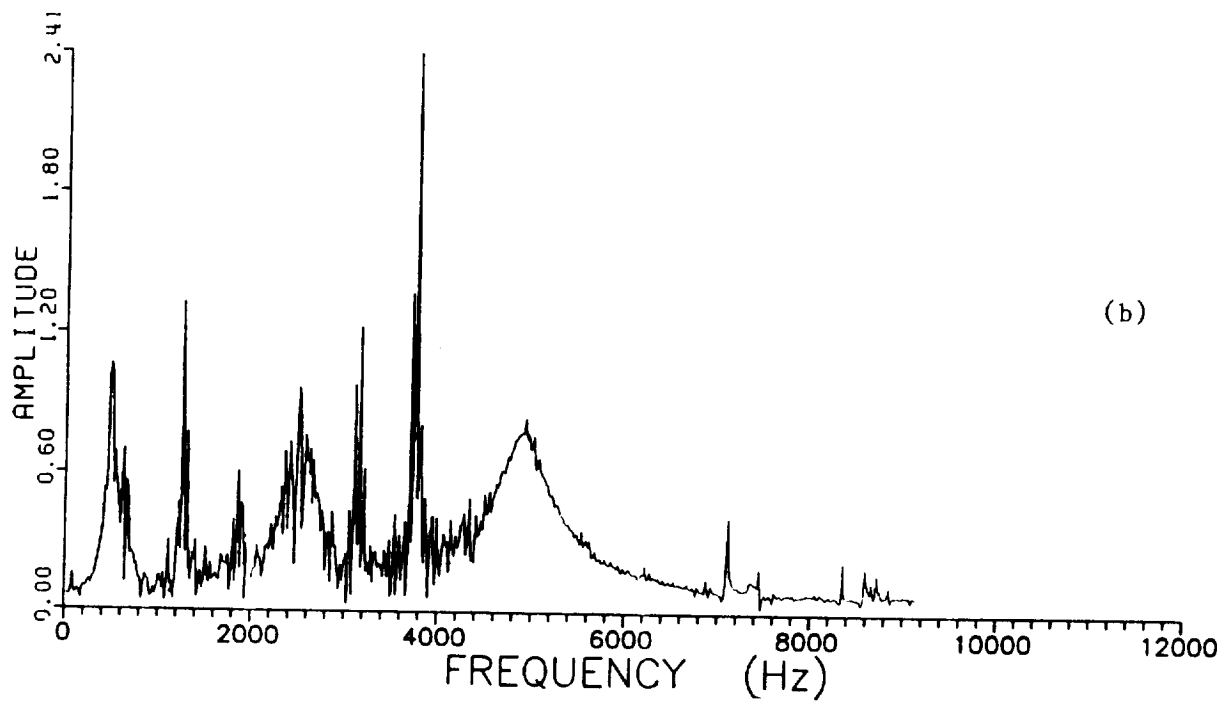
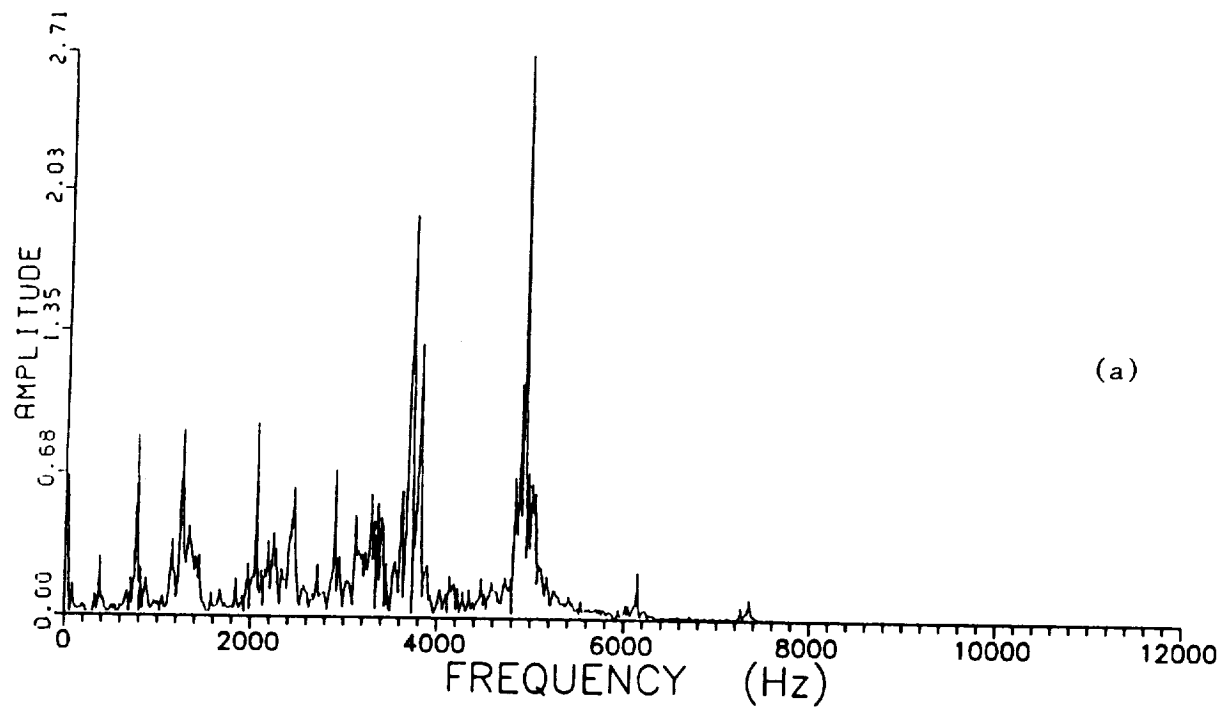


Figure 7.17 Vibration frequency spectra at top of gear box for operating speed of 3,000 rpm from (a) experimental data, and (b) numerical simulations.

(3750 Hz) and 4-times (5000 Hz) the mesh frequency. The very large amplitude in the frequency components at 3750 Hz and 5000 Hz are due to the excitation of the gear box natural frequencies near the 3-times and 4-times multiples of the mesh frequency. The fundamental and the 2-times mesh frequency component are substantially smaller due to the lack of any gear box natural frequencies near 1250 Hz and 2500 Hz. In addition, frequency components of substantial magnitude are also noticed at 700 Hz and 2900 Hz, which are also close to the natural frequencies of the gear box. Figure 7.17B depicts the results from the numerical simulations of the system. The numerical results correspond closely to those from the experimental study with the exception of the 4-times mesh frequency component. The magnitude and the general distribution of the frequency content of the spectrum is very similar to the experimental results.

To develop a predictive algorithm for the noise level in the gear box, the experimental transfer function developed with noise/vibration data is used in this study. The transfer function for Microphone No. 1 (vertical to the plate) is given in Fig. 7.18A and for microphone No. 2 (45 degrees with the plate) is given in Fig. 7.18B. By taking the product of the transfer functions with the vibration frequency spectrum, the frequency spectra for both the microphone cases can be evaluated. Figure 7.19 shows the comparison of the results of the experimental noise, Fig. 7.19A, with the predicted noise, Fig. 7.19B, for the vertical microphone. Although all the major frequency components excited in both cases are very similar, one can see that the predicted noise spectrum, Fig. 7.19B, has a much higher amplitude at mesh frequency and a very small 4-times mesh frequency component as in the vibration spectrum. Comparing the results for the 45-degree microphone, Fig. 7.20, a

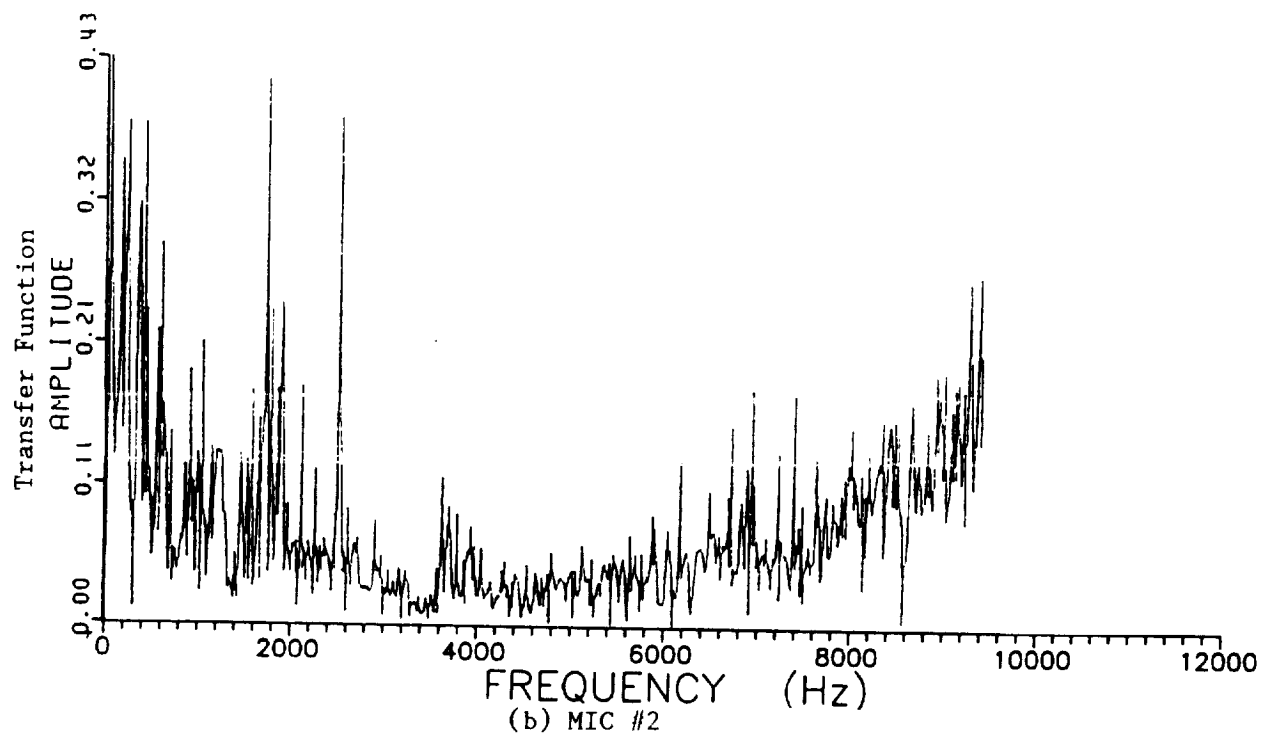
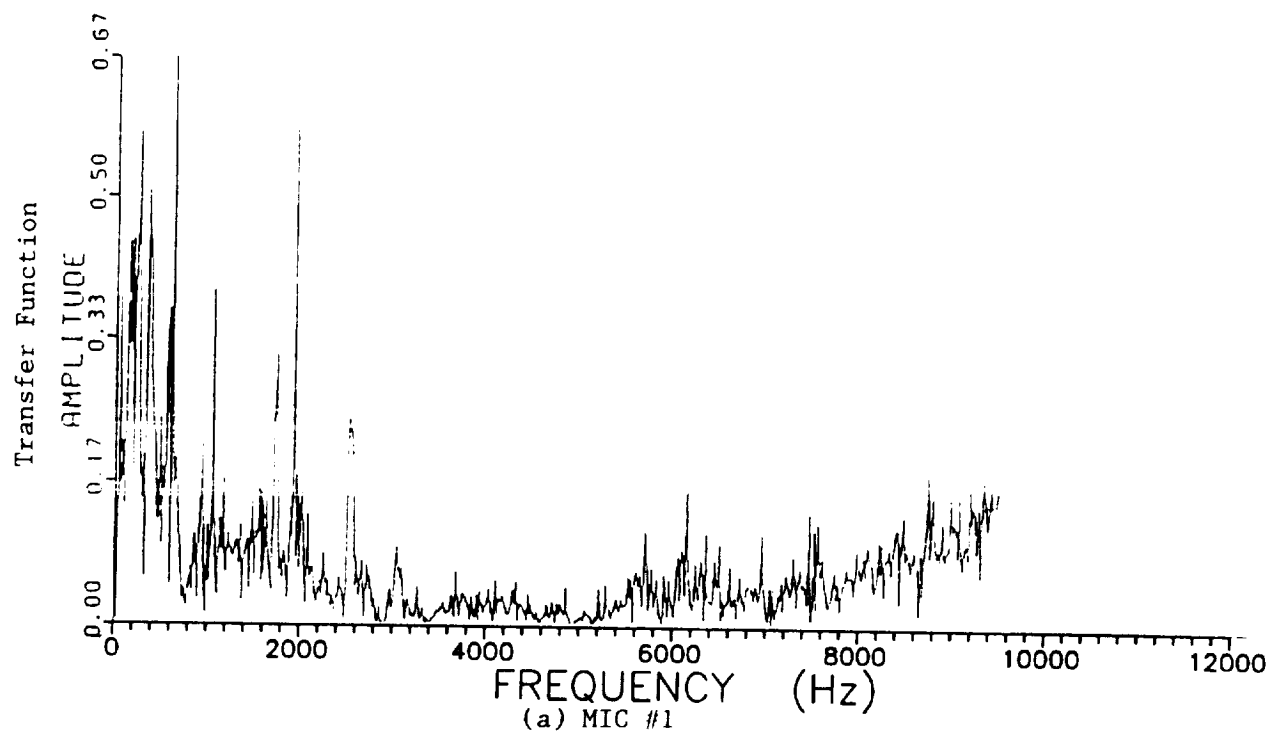


Figure 7.18 Transfer function for noise (a) microphone no. 1, and (b) microphone no. 2, with vibration at operating speed of 3,000 rpm.

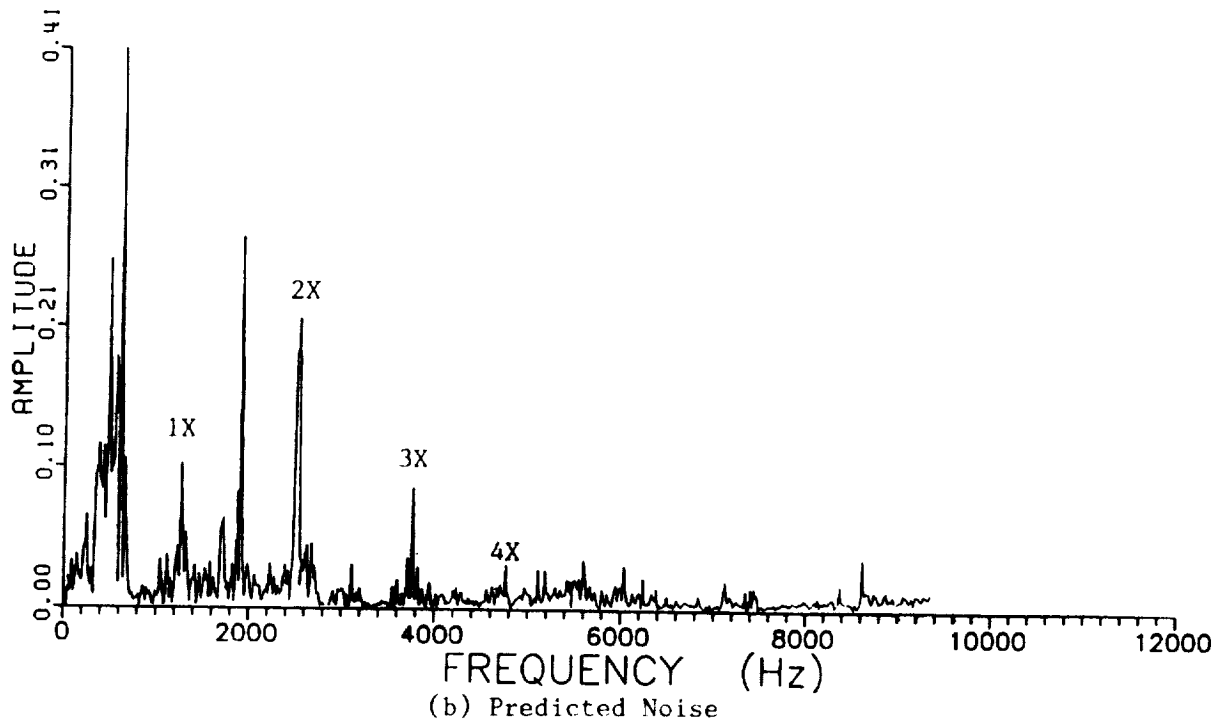
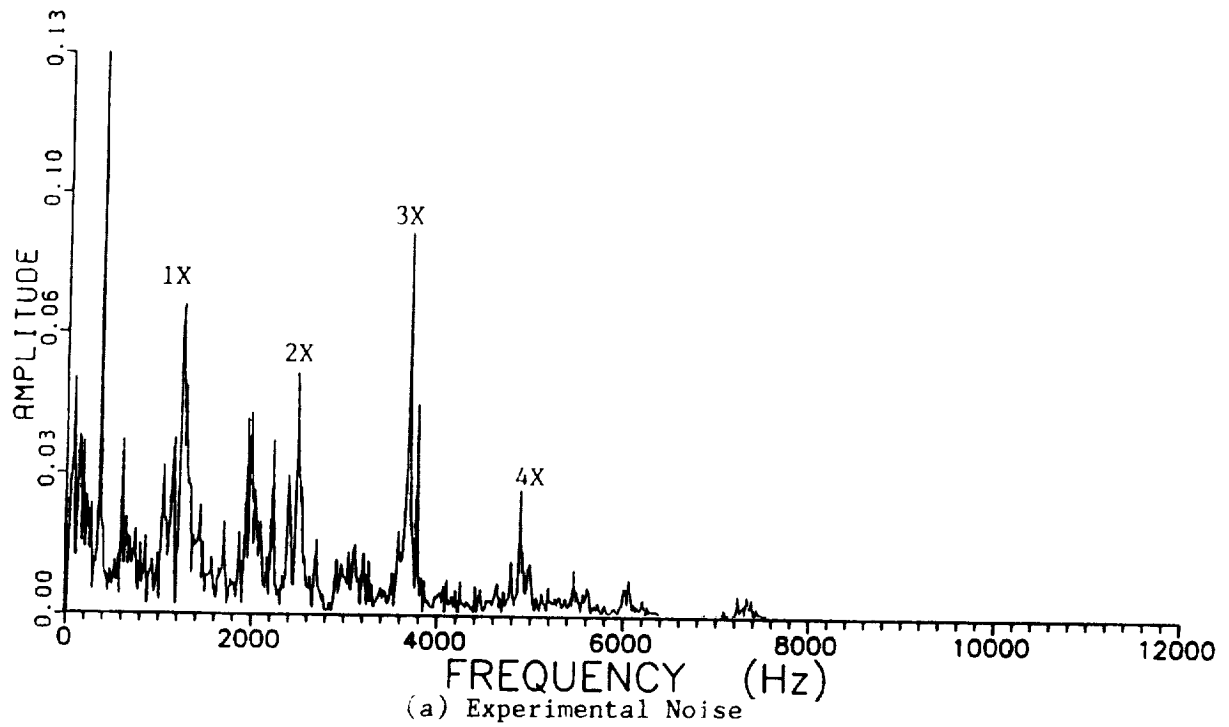


Figure 7.19 Frequency spectra of (a) experimental noise data, and (b) predicted noise results from microphone no. 1 at the operating speed of 3,000 rpm.

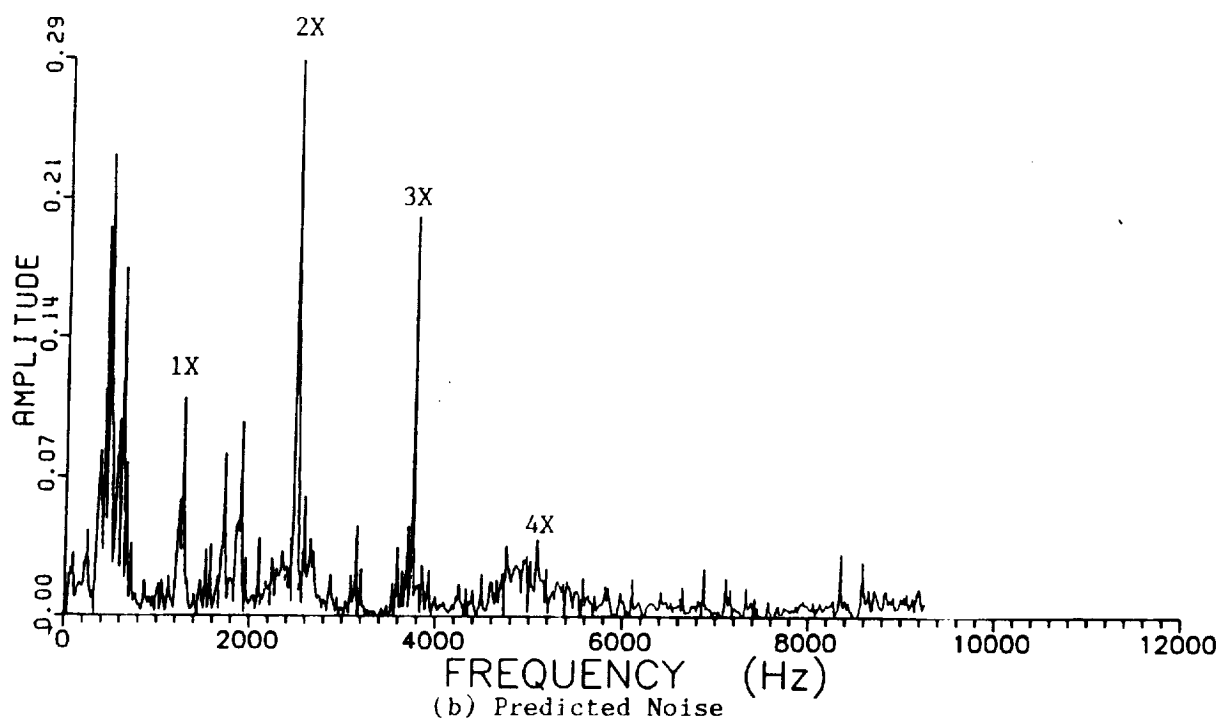
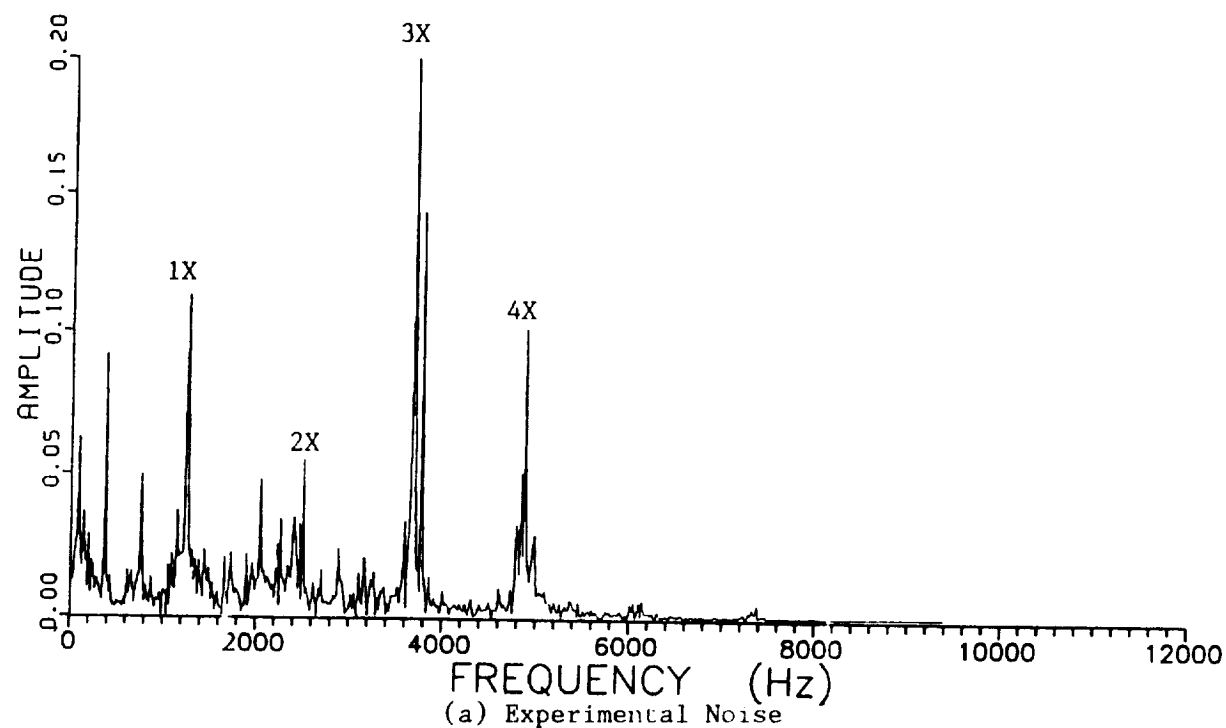


Figure 7.20 Frequency spectra of (a) experimental noise data, and (b) predicted noise results from microphone no. 2 at the operating speed of 3,000 rpm.

similar conclusion can be drawn for the predicted noise (larger amplitudes in most of the frequency components).

Another way of examining the validity of the predicted noise signal is through the nonlinear relationships derived by the Hypercoherence Function. The Hypercoherence function developed by NASA Marshall Space Flight Center is used primarily for the space shuttle noise program to generate nonlinear relationships between the fundamental frequency component and the integer multiples of the fundamental. A time signal for the gear box noise is required for this analysis. Figure 7.21 depicts the time signal for the gear box noise, from experimental study, (Fig. 7.21A), and from numerical simulations (Fig. 7.21B), for microphone No. 1. A set of the experimental and numerical noise data for microphone No. 2 is also given in Fig. 7.22. Figures 7.23 and 7.24 show the comparison of the hypercoherence functions from both experimental and numerical solutions correspondingly for microphone No. 1 and No. 2. For microphone No. 1, both the experimental and numerical results show a very small 2-times component, with a substantial amplitude at 3, 4, and 5 times fundamental frequency. However, a 50% coherence is found in the 3, 4, and 5 times components from numerical predictions, Fig. 7.23B, while only about a 25% coherence is seen from the experimental results, Fig. 7.23A. A similar conclusion can also be drawn from the results of microphone No. 2, Fig. 7.24. The difference in the numerical solution results from the experimental results are possibly due to the limitation of the numerical model in simulating various details and imperfections in the gear box transmission system. A logical explanation of the much higher (nearly double) coherence amplitudes in the numerical study is that only the major frequency-related vibration contributing factors

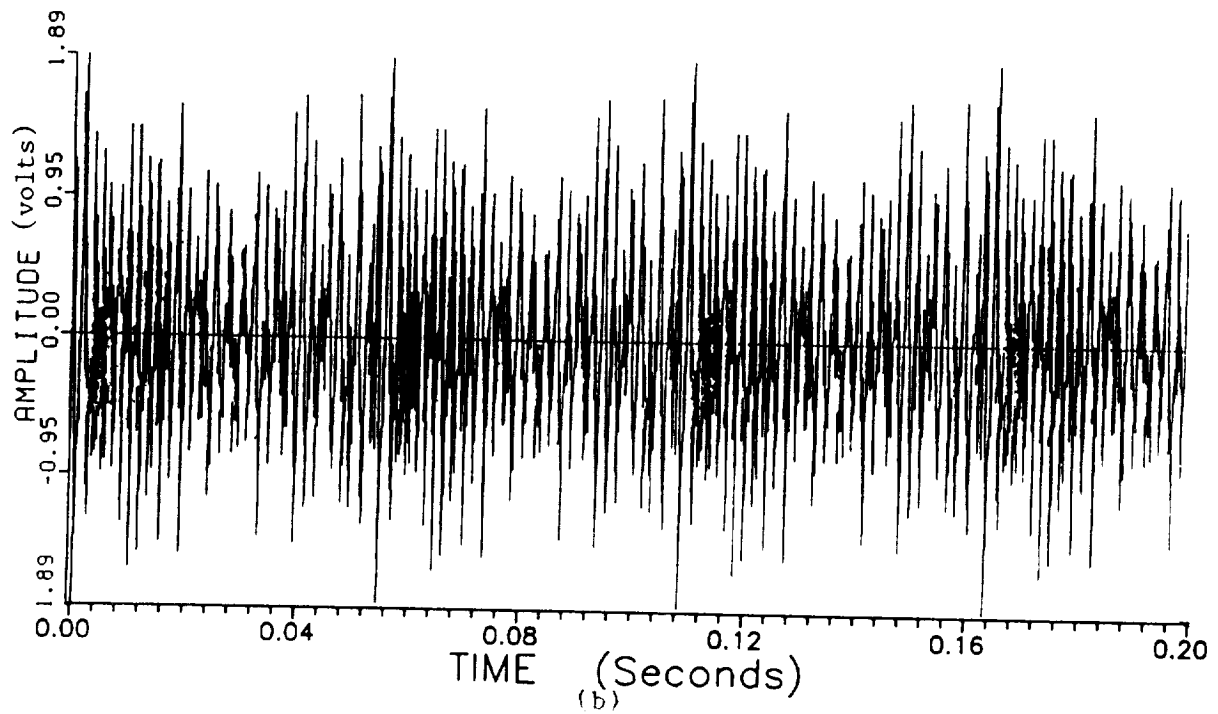
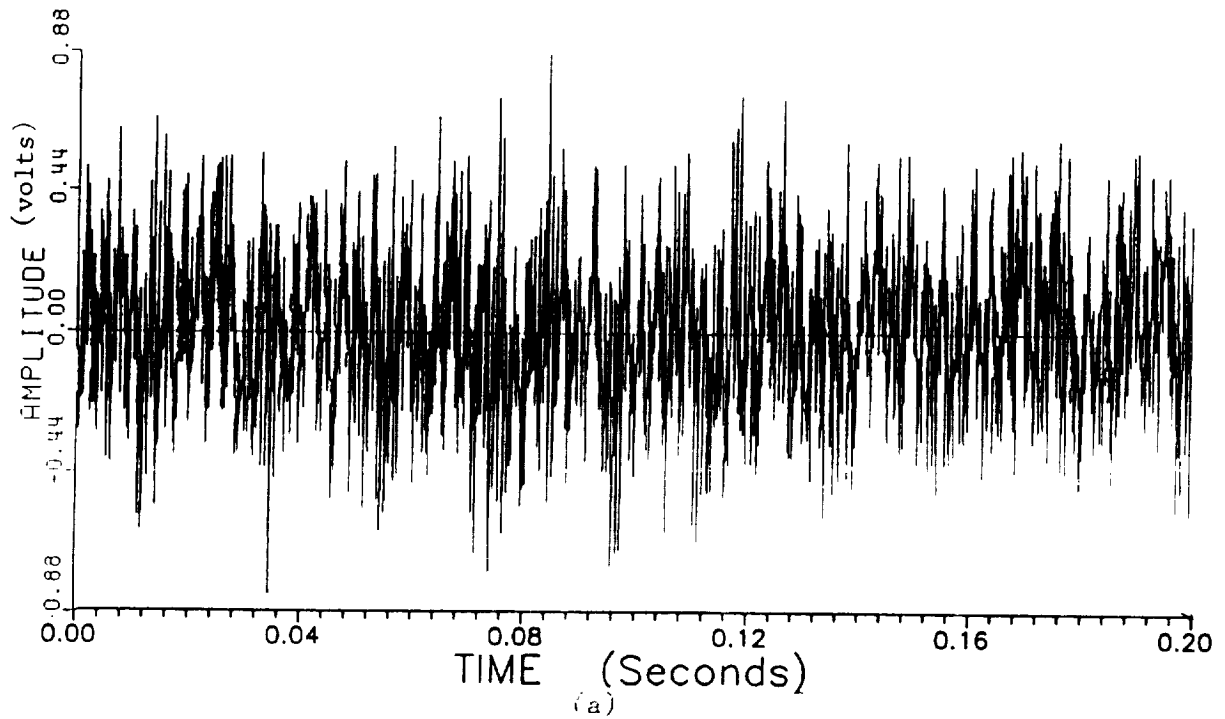


Figure 7.21 Time noise signal from (a) experimental noise data, and (b) predicted noise results from microphone no. 1 at the operating speed of 3,000 rpm.

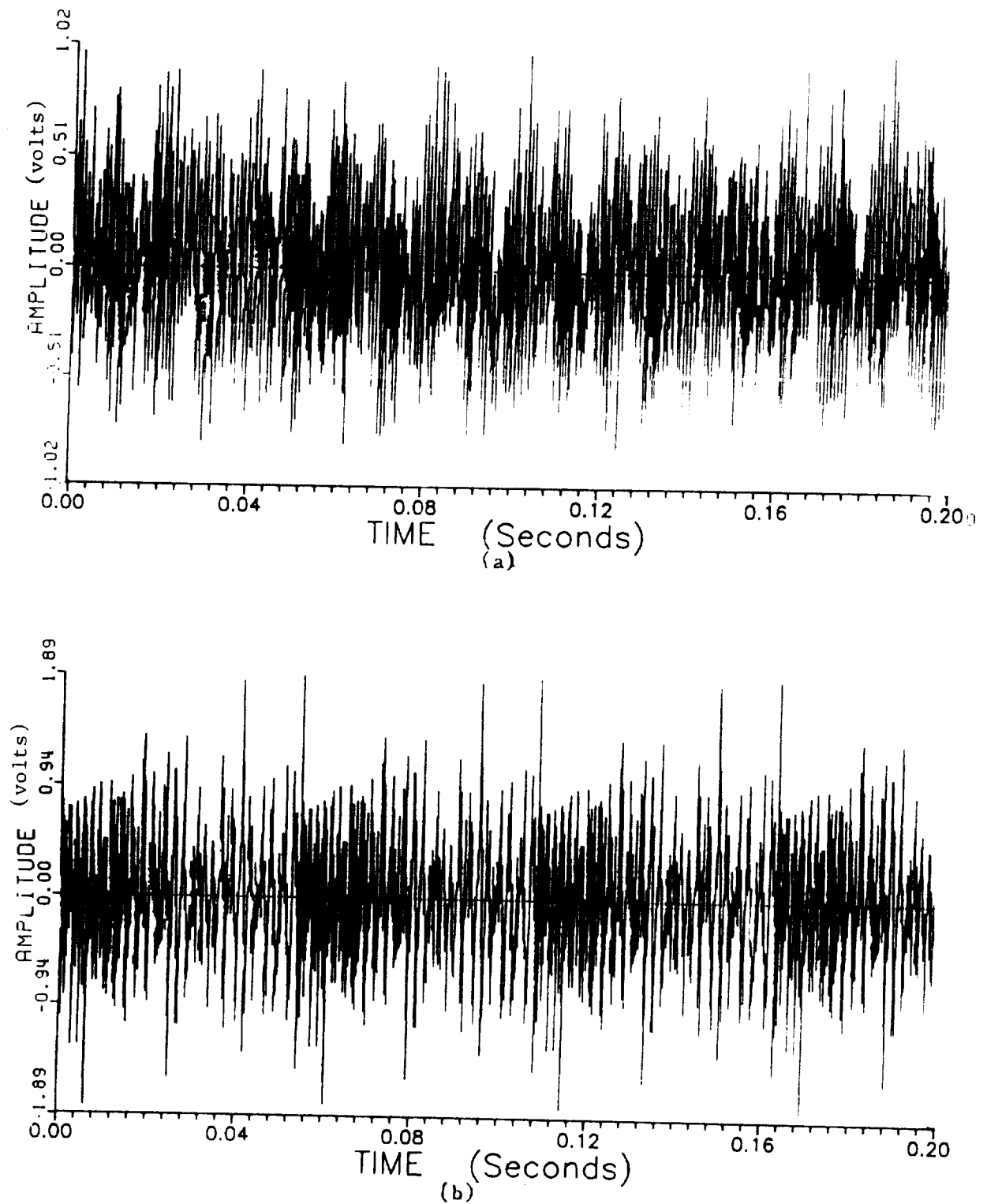


Figure 7.22 Time noise signal from (a) experimental noise data, and (b) predicted noise results from microphone no. 2 at the operating speed of 3,000 rpm.

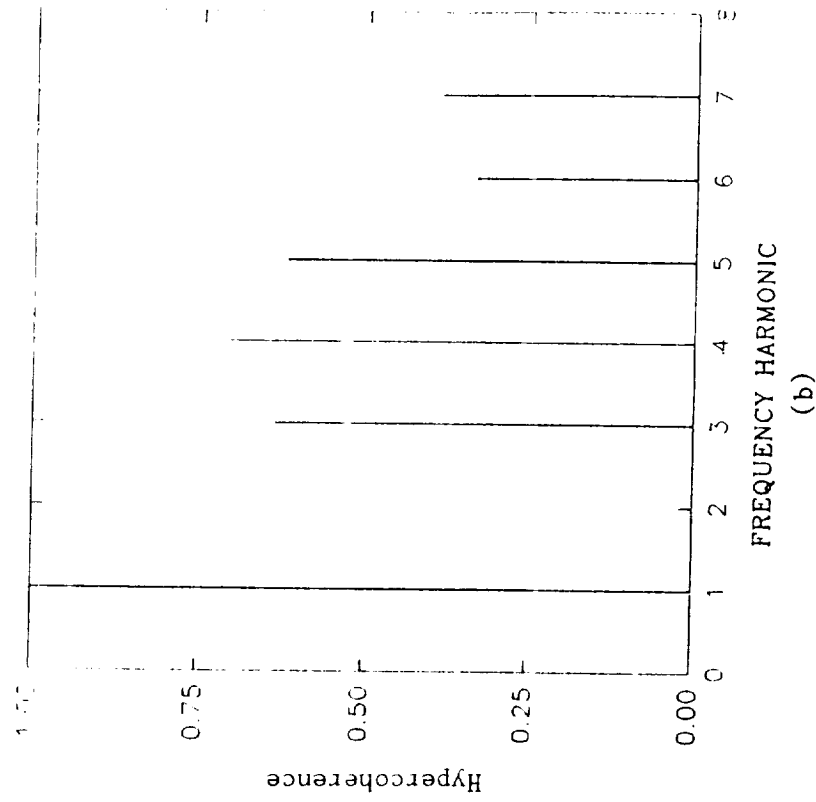
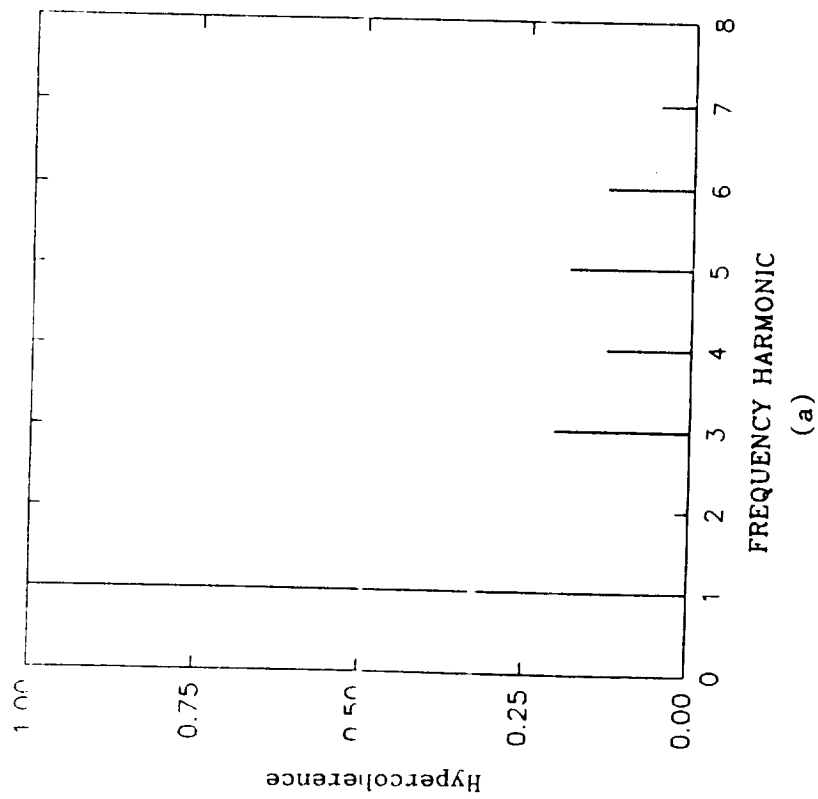


Figure 7.23 Hypercoherence function of the noise signal from (a) experimental data, and (b) from numerical predictions, for microphone no. 1 at the operating speed of 3,000 rpm

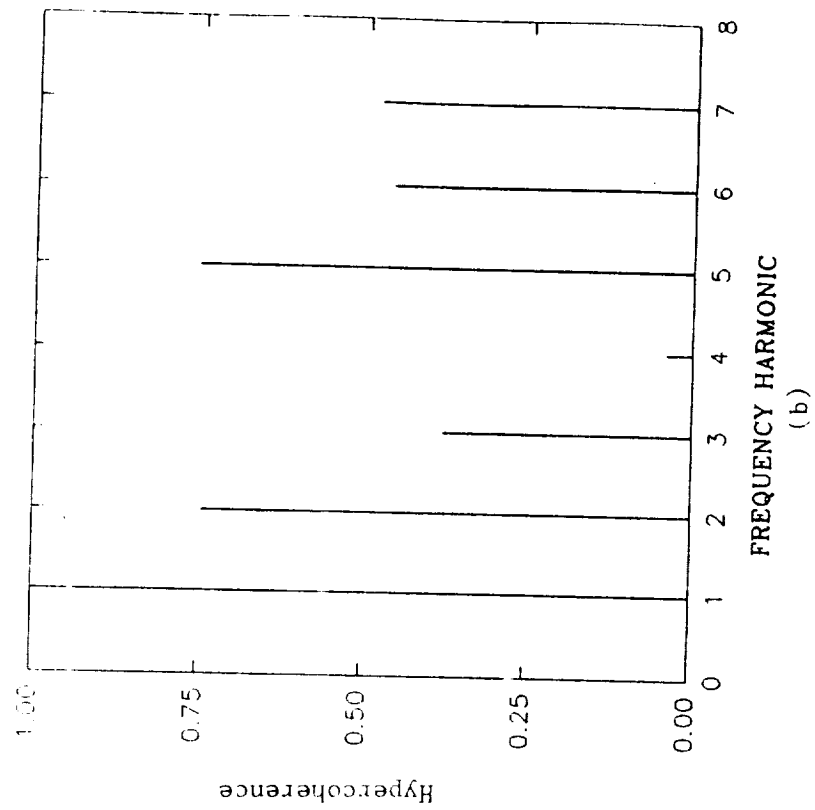
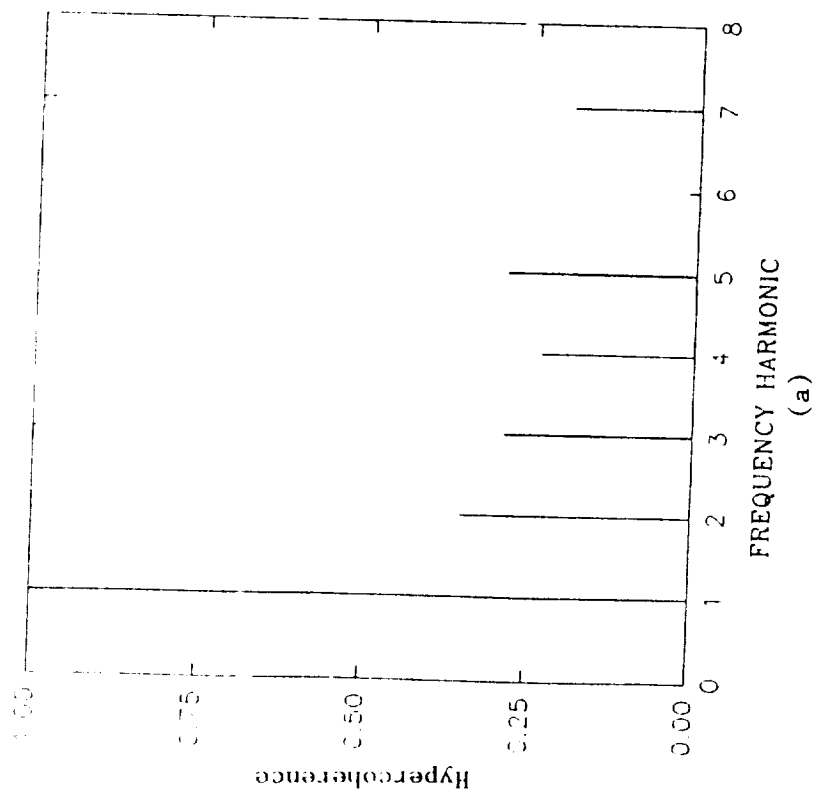


Figure 7.24 Hypercoherence function of the noise signal from (a) experimental data, and (b) from numerical predictions, for microphone no. 2 at the operating speed of 3,000 rpm

are included in the model, which results in a predicted vibration signal consisting mostly of frequency components which are closely related to the fundamental frequency.

8. CONCLUSIONS AND SUMMARY

A methodology has been developed using the modal synthesis technique to simulate the global dynamics of a gear transmission system. Excellent correlation has been obtained using results from the global dynamic model and measured dynamic characteristics from the NASA gear noise test rig. A numerical relationship was also developed from the experimental data to correlate noise and vibrations in the frequency domain. The developed noise\ vibration relationships are applied to the vibration simulations to predict the noise of the gear box. Results of the predicted noise are compared to the experimentally measured data linearly using the frequency spectra and nonlinearly using the hypercoherence function. The major accomplishments/conclusions of this study can be summarized as follows:

1. The dynamics of a gear transmission system coupled with the vibrations of the gear box structure during operation can be simulated accurately using the modal synthesis technique.
2. Gear system dynamic characteristics such as imbalance, shaft residual bow, gear mesh nonlinear stiffness, gear tooth friction, coupled axial and lateral bearing stiffness, and gyroscopic effects are also incorporated into the global dynamic model.
3. Experimental results of both gear vibration and noise are obtained using the NASA gear noise test rig for benchmarking and correlating with the numerical predictions.

4. The accuracy of the rotor and the gear box model can be improved by matching the modal characteristics calculated numerically with those obtained through experimental testing.
5. The choice and the number of vibratory modes selected to simulated the gear box vibration can be selected according to those excited experimentally by the impulse response technique. Such selection not only will reduce the number of modes used, which can significantly improve computational efficiency, it also will provide an accurate simulation of the dynamics of the system.
6. Predicted vibrations at the housing surface using the global dynamic model are in good agreement with measured values.
7. A set of linear relationships are developed between the gear box noise and vibration using transfer functions and both experimental noise and vibration spectra.
8. The developed transfer functions are applied to the numerically simulated gear box vibrations to predict noise generated from the transmission system. Both the frequencies and magnitudes of the predicted noise components are very similar to those obtained from experimental study.
9. An examination of the nonlinear relationships of the noise components with the fundamental frequency (gear mesh frequency) is performed using the hypercoherence function. A comparison of these relationships between the predicted noise and the measured noise is also presented.

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APPENDIX A

For the massless beam element shown in Fig. A1-a, the dynamic characteristics of the element can be represented as (16-18):

$$\begin{Bmatrix} Y \\ \phi \\ M \\ V \end{Bmatrix}_i^L = [S_i] \begin{Bmatrix} Y \\ \phi \\ M \\ V \end{Bmatrix}_{i-1}^R \quad \text{A.1}$$

where

$$[S_i] = \begin{bmatrix} 1 & L & L^2/2EI & -L^3/6EI \\ 0 & 1 & L/EI & -L^2/2EI \\ 0 & 0 & 1 & -L \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \text{A.2}$$

The subscript i in the matrix equations designates the nodal number of the element and the superscripts L and R designate the left- and right-hand side location at the concentrated mass station. With the inertia model shown in Fig. A1-b the dynamic effects between the mass stations can be expressed in matrix form as

$$\begin{Bmatrix} Y \\ \phi \\ M \\ V \end{Bmatrix}_i^R = [P_i] \begin{Bmatrix} Y \\ \phi \\ M \\ V \end{Bmatrix}_i^L \quad \text{A.3}$$

where

$$[P_i] = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ K_i - M_i - \omega^2 & 0 & 0 & 1 \end{bmatrix} \quad \text{A.4}$$

where K_i is the stiffness of the i^{th} spring.

Using the beam element model developed with the matrix transfer technique, the dynamics of the beam structure can be related from the left end to the right end by multiplying the series of matrices as

$$\begin{Bmatrix} Y \\ \phi \\ M \\ V \end{Bmatrix}_R = \begin{bmatrix} T_{11} & T_{12} & T_{13} & T_{14} \\ T_{21} & T_{22} & T_{23} & T_{24} \\ T_{31} & T_{32} & T_{33} & T_{34} \\ T_{41} & T_{42} & T_{43} & T_{44} \end{bmatrix} \begin{Bmatrix} Y \\ \phi \\ M \\ V \end{Bmatrix}_L \quad A.5$$

where

$$\begin{bmatrix} T_{11} & T_{12} & T_{13} & T_{14} \\ T_{21} & T_{22} & T_{23} & T_{24} \\ T_{31} & T_{32} & T_{33} & T_{34} \\ T_{41} & T_{42} & T_{43} & T_{44} \end{bmatrix} = [P_n] [S_n] [P_{n-1}] [S_{n-1}] \dots [P_1] [S_1] \quad A.6$$

Using a simple support boundary condition such that the displacements and moments at the ends vanish, the overall global matrix can be written as

$$\begin{Bmatrix} 0 \\ \phi \\ 0 \\ V \end{Bmatrix}_R = \begin{bmatrix} T_{11} & T_{12} & T_{13} & T_{14} \\ T_{21} & T_{22} & T_{23} & T_{24} \\ T_{31} & T_{32} & T_{33} & T_{34} \\ T_{41} & T_{42} & T_{43} & T_{44} \end{bmatrix} \begin{Bmatrix} 0 \\ \phi \\ 0 \\ V \end{Bmatrix}_L \quad A.7$$

where

$$[D] = \begin{bmatrix} T_{12} & T_{14} \\ T_{32} & T_{34} \end{bmatrix} = 0 \quad A.8$$

such that the determinant of the matrix will vanish at the natural frequencies of the system. A marching technique can be used to determine the fundamental frequencies of the system by searching for the zeros of the determinant at a given range of frequencies.

APPENDIX B
(INPUT INSTRUCTIONS)

1. COM1, COM2, COM3 -- COMMENT CARD
2. NSTA, NKTB, NSK
 - NSTA -- NO. OF TOTAL ROTORS
 - NKTB -- NO. OF CONNECTING GEARS STIFFNESS
 - NSK -- NO. OF SLANTED ROTORS
3. INSK(I), I=1, NSK
 - LOCATION NO. OF SLANTED ROTOR
4. ANGL(INSK (I), J), J=1, 3; I=1, NSK
 - ANGLE OF SLANTED ROTOR
5. JST(I), I=1, NSTA
 - THE LOCATION NO. OF GEAR OF iTH ROTOR
6. ALPH(I, J), I=1, NSTA; J=1, NSTA
 - ANGLE BETWEEN GEARS
7. RCC(I), I=1, NSTA
 - RADIUS OF GEARS
8. TOUT(I) , I=1, NSTA
 - INPUT EXTERNAL TORSIONAL TORQUE OF ROTORS
9. FORCEZ(I), I=1, NSTA
 - INPUT EXTERNAL AXIAL FORCE OF ROTORS
10. NP1(I), XG1(I), XMAX1(I), PS11(I), I=1, NKTB
 - NP1 -- NO. OF SPUR'S POINTS OF GEAR
 - XG1 -- ANGLE BETWEEN THE SPURS OF A PAIR OF GEAR
 - XMAX1 -- ANGLE DURING TOUCH PERIOD
 - PS11 -- PHASE ANGLE OF A PAIR OF GEARS
11. XK(K, I), YK(K, I), I=1, NP1(K); K=1, NKTB
 - XK -- ANGLE OF iTH POINT OF kTH GEAR
 - YK -- STIFFNESS OF iTH POINT kTH GEAR
12. NTTD(I), I=1, NSTA
 - NO. OF GEARS FOR EACH ROTOR
13. LLTD(I, J), I=1, NTTD(J); J=1, NSTA
 - LOCATION NO. OF GEARS
14. TTCC(I, J), I=1, NTTD(J); J=1, NSTA
 - GEAR DAMPING

15. AB, OMEGA, FAB

AB -- AMPLITUDE IF BASE MOTION
OMEGA -- ROTATION SPEED OF BASE MOTION (RAD/SEC)
FAB -- PHASE ANGLE OF BASE MOTION

16. NMODE

MODES NO. OF ROTORS

17. N, NB, NNLIN, NMB, NF, NU, NS, NBOW, ISTAB, IMODE, ISKU, NCT,
NUFPT

N -- NO. OF MASS STAGE OF ROTOR
NB -- NO. OF REGULAR LINEAR BEARINGS OF ROTOR
NNLIN -- NO. OF NONLINEAR BEARINGS OF ROTOR
NMB -- NO. OF MOMENT RESISTING BEARINGS
NF -- NO. OF EXTERNAL FORCE
NU -- NO. OF UNBALANCE
NS -- NO. OF SKEW DISK
NBOW = 1 -- WITH BOW SHAFT
= 0 -- NO BOW SHAFT
ISTAB = 1 -- NO STABILITY CALCULATION
= 0 -- WITH STABILITY CALCULATION
IMODE -- NO. OF DAMPED MODAL SHAPES DESIRED,
IF IMODE = 0, NO MODAL SHAPE CALCULATION
ISKU -- NO. OF SKEW STAGES
NCT -- NO. USED IN MODES CALCULATION
NUFPT -- NO. OF STAGE NEEDED TO PRINTOUT FOR UNBALANCE

18. ISKIP, NSTEP, NSYSLE, NITP, NINT, NPLLOT, NORBIT, NTIME, NSPEED,
NINC, NOPT, NT

ISKIP = 1 -- NO CALCULATION
= 0 -- CALCULATE TRANSIENT ORBIT
NSTEP -- NO. OF STEPS OF INTERGRATION PER CYCLE
NCYCLE -- NO. OF CYCLES
NITP -- NO. OF STEPS PER PRINTOUT
NINT = 1 -- NEWARK BETA METHOD
NPLLOT = 1 -- NO PLOT
= 0 -- WITH PLOT
NORBIT -- NO. OF TRANSIENT ORBIT STAGES DESIRED

NTIME -- NO. OF STAGES TO BE PLOTTED IN RESPONSE VS TIME
 CURVE
 NSPEED = 0
 NINC = 0 -- INPUT INITIAL CONDITION
 = 1 -- INITIAL CONDITION FROM STEADY STATE ORBIT
 (WITH SMALL PERTUBATION)
 = 2 -- INPUT MODAL INITIAL DATA
 NOPT = 0
 NT -- NO. OF STAGES FOR TRANSIENT PRINTOUT
 19. LLBD(J) , J=1, NB
 LOCATION NO. OF BEARINGS
 20. KXX, KXY, KYX, KYY, KXA, KAX, KAA, KXB, KBX, KBB,
 KXZ, KYZ, KZY, KZA, KAZ, KZB, KBZ, KZZ
 BEARING STIFFNESS
 21 CXX, CXY, CYX, CYY, CXA, CAX, CAA, CXB, CBX, CBB,
 CZX, CZY, CZA,
 BEARING DAMPING
 AND:
 X -- DIRECTION OF X
 Y -- DIRECTION OF Y
 A -- DIRECTION OF X ROTATION
 B -- DIRECTION OF Y ROTATION
 Z -- DIRECTION OF Z
 22. LLNB(J) , NLB(J) , VIS(J) , ANR(J) , ANL(J) , ANC(J) , J=1,NNLIN
 LLNB -- LOCATION NO. OF NONLINER BEARINGS
 NLB -- BEARING NO. OF NONLINEAR BEATINGS
 VIS -- VISCUSITY OF LUBRICATE (LB/IN**2)
 ANR -- RADIUS OF BEARING (IN)
 ANL -- LENGTH OF BEARINGS (IN)
 ANC -- CLEARANCE OF BEARING (IN)
 23. LLNMB(J) , J=1,NMB
 LOCATION NO. OF MOMENT RESISTING BEARING
 24. SLNMB(I,J,K) , CLNMB(I,J,K) , I=1,NMB; J=1,4; K=1,4
 NMB SETS, EACH SET 4 CARDS. THESE ARE THE
 BEARING STIFFNESS AND DAMPING COEFFICIENTS FOR
 MOMENT RESISTING BEARING

25. NGYR -- NO. OF GYROSCOPIC ROTOR
 E -- SECTION YOUNG'S MODULUS
 SPEED1 -- ROTOR'S OPERATING SPEED (RPM)
 SPEED2 -- ROTOR'S INITIAL OPERATING SPEED (RPM)
 ANGACL -- ANGULAR ACCERATION OF ROTOR
 BETA -- BETA PARAMETER USED FOR NEWMARK BETA METHOD
26. EXTW(J) , DX(J) , DDXT(J) , DDNT(J) , RP(J) , RT(J) , EM6(J) ,
 RO(J) , GGO(J) , TK(J) , J=1,N
 EXTW -- INPUT EXTERNAL WIGHT PER ELEMENT OF ROTOR
 DX -- ELEMENT LENGTH OF ROTOR
 DDXT -- EXTERNAL DIAMETER PER ELEMENT OF ROTOR
 DDNT -- INTERNAL DIAMETER PER ELEMENT OF ROTOR
 RP -- POLAR INERTIA MOMENT PER ELEMENT OF ROTOR
 RT -- TRANSVERSE INERTIA MEOMET PER ELEMENT
 OF ROTOR
 EM6 -- YOUNG'S MODULUS PER ELEMENT OF ROTOR
 RO -- DENSITY PER ELEMENT OF ROTOR
 GGO -- SHEAR'S MODULUS PER ELEMENT
 TK -- TORTIONAL CONSTRAINT MOMENT PER ELEMENT
27. LLFF(J) , FX(J) , FY(J) , J=1,NF
 LLFF -- LOCATION NO. OF EXTERNAL FORCE OF ROTOR
 FX -- EXTERNAL FORCE ON X-DIRECTION
 FY -- EXTERNAL FORCE ON Y-DIRECTION
28. LLUF(J) , UX(J) , UY(J) , SUX(J) , SUY(J) , J=1,NU
 LLUF -- LOCATION NO. OF UNBALANCE OF ROTOR
 UX -- X-DIR UNBALANCE (OZ-IN)
 UY -- Y-DIR UNBALANCE (OZ-IN)
 SUX -- SUDDEN INCREASE UNBALANCE OF X-DIRECTION
 SUY -- SUDDEN INCREASE UNBALANCE OF Y-DIRECTION
29. LLSK(J) , FSK(J) , PSK(J) , J=1,NS
 LLSK -- LOCATION NO. OF SKEW DISK
 FSK -- MAX. SKEW IN RADIAN
 PSK -- ANGLE BETWEEN MAX. SKEW TO THE X AXIS
30. LLUT(J) , J=1,NUFPT
 LOCATION NO. FOR PRINTOUT OF UNBALANCE RESPONSE

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31.  LLNT(J), J=1, NT
    LOCATION NO. FOR PRINTOUT OF ROTOR IN TRANSIENT
    ANALYSIS
32.  NAB, CTIME
    SKIP IF NINC IS NOT EQUAL TO 2
    NAB      -- NO. OF MODES
    CTIME    -- FINAL TIME OF PRESENT RUN
33.  A3(1,J), B3(1,J), A2(1,J), B2(1,J), J=1, NAB
    SKIP IF NINC NOT EQUAL TO 2
    MODAL DISPLACEMENT AND VELOCITY AT FINAL STEP
    OF PRESENT RUN
34.  BOW(J), PBOW(J), XIDC(J), YIDC(J), VXIDC(J), VYIDC(J), J=1,N
    SKIP IF NBOW=0
    BOW      -- INITIAL BOW
    PBOW     -- ANGLE OF BOW
    XIDC     -- INITIAL DISPLACEMENT IN X-DIRECTION
    YIDC     -- INITIAL DISPLACEMENT IN Y-DIRECTION
    VXIDC    -- INITIAL VELOCITY IN X - DIRECTION
    VYIDC    -- INITIAL VELOCITY IN Y- DIRECTION
35.  SPI, SPL, DSP
    SPI      -- INITIAL SPEED FOR CRITICAL SPEED
    SPL      -- FINAL SPEED FOR CRITICAL SPEED
    DSP      -- SPEED INCREMENT FOR CRITICAL SPEED
36.  SPE1, SPE2, SPE3
    SPE1     -- INITIAL SPEED FOR TORTIONAL CRITICAL SPEED
    SPE2     -- FINAL SPEED FOR TORTIONAL CRITICAL SPEED
    SPE3     -- SPEED INCREMENT FOR TORTIONAL CRITICAL SPEED
37.  SPS, SPF, SPN
    SPS      -- INITIAL SPEED FOR UNBALANCE RESPONSE CAL.
    SPF      -- FINAL SPEED FOR UNBALANCE RESPONDE CAL.
    SPN      -- SPEED INCREMENT FOR UNBALANCE RESPONSE CAL.
38.  NBMOP
    BASE MOTION LOGIC, IF NBMOP = 0, SKIP
    1, A(T) = ALPHA*(E**B*T)*COS(W1*T)
    2, A(T) = ALPHA * COS(W1*T)*COS(W2*T)

```

39. ACON1(I), ACON2(I), APH1(I), APH2(I), I=1,NB
 SKIP IF NBMOP NOT EQUAL C
 EACH VARIABLE FOR ALPHA, B, W1, W2 FOR
 $A(T) = \text{ALPHA} * \cos(W1 * T) * \cos(W2 * T)$

40. NSRUB, NSEU
 SKIP IF NSRUB = 0
 NSRUB -- NO. OF RUB STAGES
 NSEU -- NO. OF SUDDEN INCREASE UNBALANCE STAGES

41. NFACT, IND, KR, ABSO
 SKIP IF NSRUB = 0
 NFACT -- STEP FACTOR OF RUB
 IND = 0 -- FOR CASING STIFFNESS
 =1 -- BLADE EQUATION
 =2 -- LINEARIZED STIFFNESS
 KR -- DIRECT CASING STIFFNESS
 ABSO -- FRICTION COEFFICIENT

42. NRUB(J), CLEAR(J), J=1, NSRUB
 SKIP IF NSRUB = 0
 NRUB -- LOCATION NO. OF RUB STAGE
 CLEAR -- CLEARANCE BETWEEN ROTOR AND CASING

43. ABL1, ABL2, ABL3
 THREE TITLE CARDS OFR LABEL IN PLOTS

44. NMBB, NDB, NODEB
 NMBB -- MODES NO. OF BOX
 NDB -- NO. OF NODES OF BOX
 NODEB -- DEGREE OF FREEDOM FOR EACH NODE

45. LBLBT(I,K), I=1, NNB(K), K=1, NSTA
 LOCATION NO. OF BEARING ON BOX

46. BKZZ(I,K), I=1, NNB(K), K=1, NSTA
 Z-DIRECTION CASING STIFFNESS

47. NPT
 NO. OF BOX'S NODES FOR DEFORMATION ANALYSIS

48. NPTNO(I), I=1, NPT
 LOCATION NO. OF NODES FOR DEFORMATION ANALYSIS

49. OMEGS(IN), IN=1, NMBB
 NATURAL FREQUENCIES OF BOX

50. IA, BX1(IN, ID, IX), IX=1, 5; ID=1, NDB; IN=1, NMBB

IA -- NODE NUMBER

BX1 -- MODAL SHAPES OF BOX

AND:

IX = 1 -- MODAL SHAPES IN X-DIRECTION

= 2 -- MODAL SHAPES IN Y-DIRECTION

= 3 -- MODAL SHAPES IN Z-DIRECTION

= 4 -- MODAL SHAPES IN X-ROTATION

= 5 -- MODAL SHAPES IN Y-ROTATION

NOTE: DATA IN CARDS 49 AND 50 CAN BE OBTAINED THROUGH RUNNING
NSTRAN PROGRAM.

APPENDIX C
(COMPUTER PROGRAM LISTING)


```

C *****
C *
C * This program calculates the dynamics of a multi-stage rotor-
C * bearing-gear system coupling with the vibrations of the gear box
C * structure. The modal synthesis procedure is used in this program.
C * Undamped critical speeds and orthonormal modes of the rotor
C * bearing system is calculated by the matrix transfer method. The
C * orthonormal modes of the casing(gearbox) structure are evaluated
C * using a finite approach(NASTRAN) such that output of NASTRAN can
C * be read directly into the program as data file. Transient and
C * steady state vibrations of the system will be evaluated by solving
C * the equations of motion in the modal coordinates. In addition, the
C * program will handle other dynamic effects such as:
C *   - multi-stage rotor bearing system
C *   - mass imbalance, shaft residual bow, and disk skew
C *   - effects of base motion
C *   - input of nonlinear gear stiffness
C *   - 3-dimensional lateral-torsional coupled bearing stiffness
C *   - coupling casing vibration effects
C * The output of the program will be given in files that can be read
C * directly in any IBM compatible PC for plotting of data. The main
C * files are given as follows:
C *   - gear.dat      --- gear force
C *   - box.dat       --- deformation at top of gearbox
C *   - orbit1.dat    --- first stage orbit at gear station
C *   - orbit2.dat    --- second stage orbit at gear station
C *   - x_modal.dat   --- modal amplitude in x-dir for each stage
C *   - y_modal.dat   --- modal amplitude in y-dir for each stage
C *
C * The program is written by:
C *
C *           BY F.K. CHOY  &  W. QIAN
C *
C *           DEPARTMENT OF MECHANICAL ENGINEERING
C *
C *           UNIVERSITY OF AKRON, AKRON, OH 44325
C *
C *           NOV. 10,1992
C *****

```

```

C ----- THERE ARE THREE PARTS:
C           1. PROGRAM
C           2. SAMPLING DATA
C           3. INPUT DATA INSTRUCTION ( APPENDIX )

```

```

C           * * * * *
C PART1. * PROGRAM *
C           * * * * *
C           IMPLICIT REAL(A-H,O-Z)
C           REAL MFX,MFY,MUY,MUX,KMX,KMY,MBX,MBY,KR
C           REAL KXX,KXY,KXA,KXB,KXZ
C           REAL KYX,KYY,KYA,KYB,KYZ
C           REAL KAX,KAY,KAA,KAB,KAZ
C           REAL KBX,KBY,KBA,KBB,KBZ
C           REAL KZX,KZY,KZA,KZB,KZZ

```

```

C ----- BEARING STIFFNESS
C           X -- DIRECTION OF X
C           A -- DIRECTION OF X ROTATION
C           Y -- DIRECTION OF Y
C           B -- DIRECTION OF Y ROTATION

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```

C          Z -- DIRECTION OF Z
CHARACTER COM1(80),COM2(80),COM3(80)
CHARACTER ABL1(80),ABL2(80),ABL3(80)
DIMENSION KXX(30),KXY(30),KXA(30),KXB(30),KXZ(30)
DIMENSION CXX(30),CXY(30),CXA(30),CXB(30),CXZ(30)
DIMENSION KYX(30),KYY(30),KYA(30),KYB(30),KYZ(30)
DIMENSION CYX(30),CYY(30),CYA(30),CYB(30),CYZ(30)
DIMENSION KAX(30),KAY(30),KAA(30),KAB(30),KAZ(30)
DIMENSION CAX(30),CAY(30),CAA(30),CAB(30),CAZ(30)
DIMENSION KBX(30),KBY(30),KBA(30),KBB(30),KBZ(30)
DIMENSION CBX(30),CBY(30),CBA(30),CBB(30),CBZ(30)
DIMENSION KZX(30),KZY(30),KZA(30),KZB(30),KZZ(30)
DIMENSION CZX(30),CZY(30),CZA(30),CZB(30),CZZ(30)
C ----- BEARING STIFFNESS K**
C ----- BEARING DAMPING C**
C          X -- DIRECTION OF X
C          A -- DIRECTION OF X ROTATION
C          Y -- DIRECTION OF Y
C          B -- DIRECTION OF Y ROTATION
C          Z -- DIRECTION OF Z
DIMENSION ENER(100), EY1(100), EY2(100), DPC(100)
DIMENSION DEFL(100), LB(100), SK(100), WA(50)
DIMENSION SW1(100), EI(100)
DIMENSION WMOD(50)
DIMENSION EAN1(100), EAN2(100), EYTH(100), TMX(10,10)
DIMENSION NORUB(100), GAP(100), APH1(10), APH2(10), SNLB(5,8,3)

COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10
1      ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1      ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1      ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10
1      ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1      ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)
C ----- BEARING STIFFNESS TK**
C ----- BEARING DAMPING TC**
C          X -- DIRECTION OF X
C          A -- DIRECTION OF X ROTATION
C          Y -- DIRECTION OF Y
C          B -- DIRECTION OF Y ROTATION
C          Z -- DIRECTION OF Z

COMMON /ADD6/ TOC(16),TOD(16),TOE(16)
C          TOC -- BOX'S Z-DIRECTION DEFORMATION
C          TOD -- BOX'S X-ROTATION DEFORMATION
C          TOE -- BOX'S Y-ROTATION DEFORMATION

COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NCT,NU
1      FPT
C          N -- NO. OF MASS STAGE OF ROTOR
C          NB -- NO. OF REGULAR LINEAR BEARINGS OF ROTOR
C          NNLIN -- NO. OF NONLINEAR BEARINGS OF ROTOR
C          NMB -- NO. OF MOMENT RESISTING BEARINGS
C          NF -- NO. OF EXTERNAL FORCE
C          NU -- NO. OF UNBALANCE
C          NS -- NO. OF SKEW DISK
C          NBOW = 1 -- WITH BOW SHAFT

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C          = 0      -- NO SHAFT BOW
C      ISTAB = 1      -- NO STABILITY CALCULATION
C          = 0      -- WITH STABILITY CALCULATION
C      IMODE -- NO OF DAMPED MODAL SHAPES DESIRED
C          IF = 0, NO MODAL SHAPE CALCULATION
C      ISKU -- NO. OF SKEW STAGES
C      NCT -- NO. USED TO CALCULATE MODES OF ROTOR
C      NUFPT -- NO. OF STAGE NEEDED TO PRINTOUT FOR UNBALANCE

COMMON /BLK2/ ISKIP,NSTEP,NCYCLE,NITP,NINT,NPLOT,NORBIT,NTIME,NSPE
1          ED,NINC,NOPT,NT
C      ISKIP = 1      -- NO CALCULATION
C          = 0      -- CALCULATE TRANSIENT ORBIT
C      NSTEP -- NO. OF STEPS OF INTEGRATION PER CYCLE
C      NCYCLE -- NO. OF CYCLES
C      NITP -- NO. OF STEPS PER PRINTOUT
C      NINT = 1      -- NEWARK BETA METHOD
C      NPLOT = 1      -- NO PLOT
C          = 0      -- WITH PLOT
C      NORBIT -- NO. OF TRANSIENT ORBIT STAGES DESIRED
C      NTIME -- NO. OF STAGES TO BE PLOTTED IN RESPONSE VS TIME CURVE
C      NSPEED = 0
C      NINC = 0      INPUT INITIAL CONDITION
C          = 1      -- INITIAL CONDITION FROM STEADY STATE ORBIT
C                  ( WITH SMALL PERTURBATION )
C          = 2      -- INPUT MODAL INITIAL DATA
C      NOPT = 0
C      NT -- NO. OF STAGES FOR TRANSIENT PRINTOUT

COMMON /BLK3/ CRT(10),LLBD(10),LLNB(5),LLNMB(9),LLSK(10),LLNT(10),
1          LLUF(10),LLFF(10),LLUT(10),TCRT(10,5)
C      CRT -- ROTOR LATERAL NATURAL FREQUENCY
C      LLBD -- NO. OF COUPLING BEARING STAGE OF ROTOR
C      LLNB(J) -- STAGE NO. OF JTH NONLINEAR BEARING
C      LLNMB(J) -- STAGE NO. OF THE JTH MOMENT RESISTING BEARING
C      LLSK(J) -- STAGE NO. OF JTH TOTOR SKEW DISK
C      LLNT -- PRINTOUT ROTOR STAGE NO. FOR TRANSIENT ANALYSIS
C      LLUF(J) -- STAGE NO. OF JTH ROTOR UNBALANCE
C      LLFF(J) -- STAGE NO. OF JTH ROTOR EXTERNAL FORCE
C      LLUT -- PRINTOUT STAGE NO. FOR UNBALANCE RESPONSE
C      TCRT -- ROTOR CRITICAL SPEED

COMMON /BLK4/SLNMB(9,4,4),CLNMB(9,4,4)

COMMON /BLK5/ UX(10),UY(10),FX(10),FY(10),FSK(10),PSK(10)
C      UX -- X-DIR UNBALANCE ( OZ-IN )
C      UY -- Y-DIR UNBALANCE ( OZ-IN )
C      FX -- X-DIR EXTERNAL FORCE ( LB )
C      FY -- Y-DIR EXTERNAL FORCE ( LB )
C      FSK -- MAXIMUM STEW OF THE DISK
C      PSK -- ANGLE BETWEN MAXIMUM SKEW & X-AXIS

COMMON /BLK6/ BOW(100),PBOW(100),XIDC(100),YIDC(100),VXIDC(100),VY
1IDC(100),BXA(100),BYA(100)
C      BOW -- INITIAL BOW OF ROTORS
C      PBOW -- ANGLE OF BOW
C      XIDC -- X-DIR INITIAL DISPLACEMENT
C      YIDC -- Y-DIR INITIAL DISPLACEMENT
C      VXIDC -- X-DIR INITIAL VELOCITY
C      VYIDC -- Y-DIR INITIAL VELOCITY

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COMMON /BLK7/ CMX(10,10),KMX(10,10),EMX(10,10),CMY(10,10),KMY(10,1
10),EMY(10,10)
COMMON /BLK8/ MFX(10),MFY(10),MUX(10),MUY(10),MBX(10),MBY(10)

COMMON /BLK9/ DDP(10,100),EETH(10,100)
C   DDP -- LATERAL MODAL SHAPE OF ROTOR
C   EETH -- X-DIR TORSIONAL MODAL SHAPE OF ROTOR

COMMON /BLK10/ SPS,SPF,SPN,SPEED1
C   SPS -- INITIAL SPEED FOR UNBALANCE CALCULATION ( RPM )
C   SPF -- FINAL SPEED FOR UNBALANCE CALCULATION ( RPM )
C   SPN -- SPEED INCRME FOR UNBALANCE CALCULATION ( RPM )
C   SPEED1 -- ROTOR OPERATING SPEED ( RPM )

COMMON /BLK11/ DOX(10,10),DOY(10,10),EOX(10,10),EOY(10,10)
COMMON /BLK15/ RP(100),RT(100)
C   RP -- POLAR INERTIA MOMENT OF ROTOR
C   RT -- TRANSVERSE INERTIA MOMENT OF ROTOR

COMMON /BLK16/ SPEED2,ANGSP,ANGACL,FSPEED
C   SPEED2 -- INITIAL SPEED USED IN TRANSIENT ANALYSIS
C   ANGSP -- ANGULAR VELOCITY OF ROTOR
C   ANGACL -- ANGULAR ACCELERATION OF ROTOR

COMMON /BLK18/ AKK(10),TAKK(10,5)
C   AKK -- AVERAGE BEARING STIFFNESS
C   TAKK -- AVERAGE BEARING STIFFNESS

COMMON /BLK19/ DX(100)
C   DX(J) -- LENGTH OF JTH ELEMENT OF ROTOR

COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
1 0)
C   A1,A2,A3,B1,B2,B3 -- USED FOR MATRICE CALCULATION

COMMON /BLK22/ W(100)
C   W(J) -- WEIGHT OF JTH ELEMENT OF ROTOR

COMMON /BLK24/ BB(20,21),CC(20)
COMMON /BLK25/ BETA
C   BETA -- NEWMARK BETA COEFFICIENT

COMMON /BLK29/ PASP
C   PASP -- TRANSIENT ANGLE OF CYCLE

COMMON /BLK40/ BMMFX(10),BMMFY(10),TBMMFX(10,5),TBMMFY(10,5)
COMMON /BLK41/ NBMOP,ACON1(10),ACON2(10),AOMG1(10),AOMG2(10)
C   NBMOP = 0 NO CALCULATION
C           = 1 A(T)=(E**(A(T)*T)*COS(A(T)*T))
C           = 2 A(T)=COS(A(T)*T)**2

COMMON /BLK42/ CLEAR(100),NRUB(100),KR,IND,NSRUB,ABSO,NFACT
C   CLEAR -- CLEARANCE IN RUB
C   NRUB -- LOCATION NO. OF RUB STAGE
C   KR -- DIRECT CASING STIFFNESS
C   IND = 0 FOR CASING STIFFNESS
C         = 1 BLADE EQUATION
C         = 2 LINEARIZED STIFFNESS
C   NSRUB -- NO. OF RUB STAGES

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C      ABSO -- FRICTION COEFFICIENT
C      NFACT -- STEP FACTOR

COMMON /BLK46/ NSEU,SUX(10),SUY(10)
C      NSEU -- NO. OF SUDDEN INCREASE UNBALANCE
C      SUX -- SUDDEN INCREASE UNBALANCE OF X-DIRECTION
C      SUY -- SUDDEN INCREASE UNBALANCE OF Y-DIRECTION

COMMON /BLK79/ CTIME
C      CTIME -- FINAL TIME OF RUNNING

COMMON /SPEED/ TSPEED(5)
C      TSPEED -- ROTOR OPERATING SPEED

COMMON /SHAPE/ NN(5),NNNCT(5),NNB(5)
C      NN -- NO. OF ELEMENTS OF ROTORS
C      NNNCT -- NO. OF MODES OF ROTOR
C      NNB -- NO. OF BEARING OF ROTOR

COMMON /OMG/ NNBMO(5),TACON1(10,5),TACON2(10,5),TAOMG1(10,5),
1      TAOMG2(10,5)
COMMON /BLK14/ AAA(42),UUU(42),VVV(42),HHH(42),BBB(42),CCC(42)
COMMON /BLK21/ DMX(10,10),DMY(10,10)
COMMON /BLK28/ ABL1,ABL2,ABL3
COMMON /BLK35/ WMY(10),VIS(5),ANR(5),ANL(5),ANC(5),NLB(5)

COMMON /TOU/ TOUT(5),FORCEZ(5)
C      TOUT -- INPUT EXTERNAL TORSIONAL MOMENT ON ROTOR
C      FORCEZ -- INPUT EXTERNAL AXIAL FORCE ON ROTOR

COMMON /BLK52/ EXTW(100),DLX(100),DDXT(100),DDNT(100),RO(100),GGO(
1      100)
C      EXTW(J) -- EXTERNAL WEIGHT OF JTH ELEMENT OF ROTOR
C      DLX(J) -- LENGTH OF ELEMENT OF ROTOR
C      DDXT(J) -- EXTERNAL DIAMETER OF ROTOR
C      DDNT(J) -- INTERNAL DIAMETER OF ROTOR
C      RO -- DENSITY OF ROTOR
C      GGO -- SHEAR MODULUS *1.0E-6

COMMON /BLK54/ FR(10,5),          FFV(10,100,5)
C      FR -- TORSIONAL NATURAL FREQUENCIES OF ROTOR
C      FFV -- TORSIONAL MODAL SHAPES OF ROTOR

COMMON /BLK58/ ZF(10,5),ZFV(10,100,5)
C      ZF -- Z-DIR NATURAL FREQUENCIES OF ROTOR
C      ZFV -- Z-DIR MODAL SHAPES OF ROTOR

COMMON /BLK56/ SPE1,SPE2,SPE3
C      SPE1 -- INITIAL SPEED FOR TORSIONAL CRITICAL SPEED ANALYSIS
C      SPE2 -- FINAL SPEED FOR TORSIONAL CRITICAL SPEED ANALYSIS
C      SPE3 -- SPEED INCREMENT FOR TORSIONAL CRITICAL SPEED ANALYSIS

COMMON /BLK59/ TK(100),EM6(100)
C      TK -- TORSIONAL CONSTRAINT MOMENT OF ROTOR
C      EM6 -- YOUNG'S MODULUS *1.0E-5

COMMON /JS/ JST(5)
C      JST(J) -- THE LOCATION NO. OF GEAR OF JTH ROTOR

COMMON /K123/ XK(4,100),YK(4,100)

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C      XK(K,I) -- ANGLE OF ITH POINT OF KTH GEAR
C      YK(K,I) -- STIFFNESS OF ITH POINT OF KTH GEAR

COMMON / KK13 / NP1(4),XG1(4),XMAX1(4),PS11(4)
C      NP1 -- NO. OF SPUR'S POINTS OF GEAR
C      XG1 -- ANGLE BETWEEN SPURS OF A PAIR OF GEARS
C      XMAX1 -- ANGLE DURING TOUCH PERIOD
C      PS11 -- THE PHASE ANGLE OF A PAIR OF GEARS

COMMON / RDDT / NTTD(5),LLTD(10,5),TTCC(10,5)
C      NTTD -- NO. OF DAMPING STAGE OF ROTOR
C      LLTD -- NO. OF DAMPING STAGE OF ROTOR
C      TTCC -- DAMPING COEFFICIENT OF ROTOR

COMMON / KTB13 / NKTB,NSK,INSK(5),ANGL(5,3),UANGL(5,9)
C      NKTB -- NO. OF CONNECTING GEARS
C      NSK -- NO. OF SLANTED ROTORS
C      INSK -- THE LOCATION NO. OF SLANTED ROTOR
C      ANGL(I,1) -- ANGLE TO X-AXIS OF SLANTED ROTOR
C      ANGL(I,2) -- ANGLE TO Y-AXIS OF SLANTED ROTOR
C      ANGL(I,3) -- ANGLE TO Z-AXIS OF SLANTED ROTOR

COMMON /TMU1/ TMUX(10,5),TMUY(10,5),TEXTW(100,5),TDX(100,5)
C      TMUX -- MODAL UNBALANCE FORCE OF X-DIRECTION
C      TMUY -- MODAL UNBALANCE FORCE OF Y-DIRECTION
C      TEXTW -- INPUT EXTERNAL WEIGHT PER ELEMENT OF ROTOR
C      TDX -- ELEMENT LENGTH OF ROTOR

COMMON /TD1/ TDDXT(100,5),TDDNT(100,5),TRP(100,5)
C      TDDXT -- EXTERNAL DIAMETER OF ROTOR
C      TDDNT -- INTERNAL DIAMETER OF ROTOR
C      TRP -- POLAR INERTIA MOMENT OF ROTOR

COMMON /TR1/ TRT(100,5),TEM6(100,5),TRO(100,5),TGGO(100,5)
C      TRT -- TRANSVERSE INERTIA MOMENT OF ROTOR
C      TEM6 -- YOUNG'S MODULUS *1.0E-5
C      TRO -- DENSITY OF ROTOR
C      TGGO -- SHEAR MODULUS *1.0E-6

COMMON /MF1/ LTLFF(10,5),TSFX(10,5),TSFY(10,5),TMFX(10,5)
C      LTLFF -- ROTOR STAGE NO. OF EXTERNAL FORCE
C      TSFX -- EXTERNAL FORCE OF X-DIRECTION
C      TSFY -- EXTERNAL FORCE OF Y-DIRECTION

COMMON /TU1/ LTLUF(10,5),TUX(10,5),TUY(10,5),TSUX(10,5),TSUY(10,5)
C      LTLUF(J) -- STAGE NO. OF JTH ROTOR UNBALANCE
C      TUX -- X-DIR UNBALANCE ( OZ-IN )
C      TUY -- Y-DIR UNBALANCE ( OZ-IN )
C      TSUX -- SUDDEN INCREASE UNBALANCE OF X-DIRECTION
C      TSUY -- SUDDEN INCREASE UNBALANCE OF Y-DIRECTION

COMMON /SEU1/ LTLNT(10,5),NTSRUB(5),NTSEU(5),NTFACT(5),ITND(5)
C      LTLNT -- STAGE NO. OF PRINTOUT ROTOR STAGE FOR TRANSIENT ANALYSIS
C      NTSRUB -- NO. OF RUB STAGE
C      NTSEU -- NO. OF SUDDEN INCREASE UNBALANCE STAGES
C      NTFACT -- STEP FACTOR OF RUB
C      ITND = 0 FOR CASING STIFFNESS
C           = 1 BLADE EQUATION
C           = 2 LINEARIZED STIFFNESS

```

```

COMMON /AAB1/ KTR(5),TABSO(5),AA1(2,10,5),AA2(2,10,5),AA3(2,10,5)
C   KTR -- DIRECT CASING STIFFNESS
C   TABSO -- FRICTION COEFFICIENT
C   AA1 -- MODAL ACCELERATION OF ROTOR AT X-DIRECTION
C   AA2 -- MODAL VELOCITY OF ROTOR AT X-DIRECTION
C   AA3 -- MODAL DISPLACEMENT OF ROTOR AT X-DIRECTION

COMMON /BBA1/ BB1(2,10,5),BB2(2,10,5),BB3(2,10,5),TA1(2,10,5)
C   BB1 -- MODAL ACCELERATION OF ROTOR AT Y-DIRECTION
C   BB2 -- MODAL VELOCITY OF ROTOR AT Y-DIRECTION
C   BB3 -- MODAL DISPLACEMENT OF ROTOR AT Y-DIRECTION
C   TA1 -- MODAL ACCELERATION OF ROTOR AT TORSIONAL-DIRECTION

COMMON /TKB1/ TA2(2,10,5),TA3(2,10,5),TKB(5,5),ALPH(5,5),RCC(5)
C   TA2 -- MODAL VELOCITY OF ROTOR AT TORSIONAL-DIRECTION
C   TA3 -- MODAL DISPLACEMENT OF ROTOR AT TORSIONAL-DIRECTION
C   TKB -- STIFFNESS BETWEEN GEARS
C   ALPH -- ANGLE BETWEEN GEARS
C   RCC -- RADIUS OF GEAR

COMMON /TMB1/ TMBX(10,5),TMBY(10,5),TWMY(10,5),LTLBD(10,5)
C   LTLBD -- LOCATION NO.OF BEARINGS

COMMON /TCM1/ TCMX(10,10,5),TCMY(10,10,5),TKMX(10,10,5)
COMMON /TDO1/ TDOX(10,10,5),TDOY(10,10,5),TEOX(10,10,5)
COMMON /TD/ TDDPC(10,100,5),TEMX(10,10,5),TEMY(10,10,5)
C   T*MX -- COEFFICIENT OF COMPENSATION TERM IN X-EQUATION
C   T*MY -- COEFFICIENT OF COMPENSATION TERM IN Y-EQUATION
C   TEOX -- COEFFICIENT OF COMPENSATION TERM IN TORSIONAL-EQU.
C   TEOY -- COEFFICIENT OF COMPENSATION TERM IN TORSIONAL-EQU.
C   TDDPC -- LATERAL MODAL SHAPE OF ROTOR

COMMON /TW1/ TDMY(10,10,5),TEEYTH(10,100,5),TW(100,5),TWMOD(50,5)
C   TEEYTH -- X-DIR TORSIONAL MODAL SHAPE OF ROTOR

COMMON /LAS/ TTK(100,5),TMFY(10,5),TKMY(10,10,5),TEOY(10,10,5),
1   TDMX(10,10,5)

COMMON /BASE1/ AB,OMEGA,FAB
C   AB -- AMPLITUDE OF BASE MOTION
C   OMEGA -- ROTATION SPEED OF BASE MOTION ( RAD/SEC )
C   FAB -- PHASE ANGLE OF BASE MOTION

COMMON /BOX01/ OMEGS(40),BX1(40,200,6),LBLBT(10,5),NMBB,NODEB
C   OMEGS -- NATURAL FREQUENCY OF BOX
C   BX1 -- MODAL SHAPES OF BOX
C   LBLBT -- NO. OF BEARING LOCATION IN BOX
C   NMBB -- NO. OF MODES OF BOX
C   NODEB -- NO. OF EACH NODE'S DEGREE OF FREEDOM

COMMON /BOX03/ BKZZ(10,5)
C   BKZZ -- Z-DIRECTION STIFFNESS

COMMON /BOX08/ NPT,NPTNO(16)
C   NPT -- NO. OF BOX'S NODES FOR DEFORMATION PLOT
C   NPTNO -- LOCATION NO. OF BOX FOR DEFORMATION PLOT

C   * * * * *
C   ----- * START TO INPUT DATA OF ROTOR-GEAR SYSTEM *
C   * * * * *

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```

NNPLT=0
READ (5,690) COM1
READ (5,690) COM2
READ (5,690) COM3
C   COM1,COM2,COM3 -- SPECIFICATION OF SAMPLING CASE

WRITE(6,700) COM1,COM2,COM3
WRITE (6,1080)
WRITE (6,700) COM1,COM2,COM3
WRITE (6,710)

READ (5, *) NSTA,NKTB,NSK
C   NSTA -- NO. OF TOTAL ROTORS
C   NKTB -- NO. OF CONNECTING GEARS STIFFNESS
C   NSK -- NO. OF SLANTED ROTORS
WRITE (6, *) NSTA,NKTB,NSK
IF (NSK.EQ.0) GO TO 25

READ (5,*) (INSK(I),I=1,NSK)
C   INSK -- LOCATION NO. OF SLANTED ROTOR
WRITE (6,*) (INSK(I),I=1,NSK)

READ (5,*) ((ANGL(INSK(I),J),J=1,3),I=1,NSK)
C   ANGL -- ANGLE OF SLANTED ROTOR
WRITE (6,*) ((ANGL(INSK(I),J),J=1,3),I=1,NSK)
DO 28 I=1,NSK
DO 28 J=1,4
28  ANGL(INSK(I),J)=ANGL(INSK(I),J)*3.1415926/360.0

25  READ (5,*) (JST(I),I=1,NSTA)
C   JST(J) -- THE LOCATION NO. OF GEAR OF JTH ROTOR
WRITE (6,*) (JST(I),I=1,NSTA)

READ (5,*) ((ALPH(I,J),I=1,NSTA),J=1,NSTA)
C   ALPH -- ANGLE BETWEEN GEARS
WRITE (6,*) ((ALPH(I,J),I=1,NSTA),J=1,NSTA)

READ (5,*) (RCC(I),I=1,NSTA)
C   RCC -- RADIUS OF GEARS
WRITE (6,*) (RCC(I),I=1,NSTA)

READ (5,*) (TOUT(I),I=1,NSTA)
C   TOUT -- INPUT EXTERNAL TORSIONAL TORQUE OF ROTORS
WRITE (6,*) (TOUT(I),I=1,NSTA)

READ (5,*) (FORCEZ(I),I=1,NSTA)
C   FORCEZ -- INPUT EXTERNAL AXIAL FORCE OF ROTORS
WRITE (6,*) (FORCEZ(I),I=1,NSTA)

READ (5,*) (NP1(I),XG1(I),XMAX1(I),PS11(I),I=1,NKTB)
C   NP1 -- NO. OF SPUR'S POINTS OF GEAR
C   XG1 -- ANGLE BETWEEN THE SPURS OF A PAIR OF GEARS
C   XMAX1 -- ANGLE DURING TOUCH PERIOD
C   PS11 -- PHASE ANGLE OF A PAIR OF GEARS
WRITE (6,*) (NP1(I),XG1(I),XMAX1(I),PS11(I),I=1,NKTB)

READ (5,*) ((XK(K,I),YK(K,I),I=1,NP1(K)),K=1,NKTB)
C   XK(K,I) -- ANGLE OF ITH POINT OF KTH GEAR
C   YK(K,I) -- STIFFNESS OF ITH POINT OF KTH GEAR
WRITE (6,*) ((XK(K,I),YK(K,I),I=1,NP1(K)),K=1,NKTB)

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      READ (5,*) (NTTD(I),I=1,NSTA)
C      NTTD -- NO. OF GEARS FOR EACH ROTOR
      WRITE (6,*) (NTTD(I),I=1,NSTA)

      READ (5,*) ((LLTD(I,J),I=1,NTTD(J)),J=1,NSTA)
C      LLTD -- LOCATION NO. OF GEARS
      WRITE (6,*) ((LLTD(I,J),I=1,NTTD(J)),J=1,NSTA)

      READ (5,*) ((TTCC(I,J),I=1,NTTD(J)),J=1,NSTA)
C      TTCC -- GEAR DAMPING
      WRITE (6,*) ((TTCC(I,J),I=1,NTTD(J)),J=1,NSTA)

      READ (5,*) AB,OMEGA,FAB
C      AB -- AMPLITUDE OF BASE MOTION
C      OMEGA -- ROTATION SPEED OF BASE MOTION ( RAD/SEC )
C      FAB -- PHASE ANGLE OF BASE MOTION
      WRITE(6,*) AB,OMEGA,FAB

C      * * * * *
C ----- * INPUT DATA OF ROTOR PROPERTIES *
C      * * * * *
      DO 123 K1=1,NSTA
      K=5*K1+55
      READ(5,859) NMODE
C      NMODE -- MODES NO. OF ROTORS
      WRITE(6,859) NMODE

      READ(5,720) N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NUFPT
C      N -- NO. OF MASS STAGE OF ROTOR
C      NB -- NO. OF REGULAR LINEAR BEARINGS OF ROTOR
C      NNLIN -- NO. OF NONLINEAR BEARINGS OF ROTOR
C      NMB -- NO. OF MOMENT RESISTING BEARINGS
C      NF -- NO. OF EXTERNAL FORCE
C      NU -- NO. OF UNBALANCE
C      NS -- NO. OF SKEW DISK
C      NBOW = 1 -- WITH BOW SHAFT
C      = 0 -- NO SHAFT BOW
C      ISTAB = 1 -- NO STABILITY CALCULATION
C      = 0 -- WITH STABILITY CALCULATION
C      IMODE -- NO OF DAMPED MODAL SHAPES DESIRED
C      IF = 0, NO MODAL SHAPE CALCULATION
C      ISKU -- NO. OF SKEW STAGES
C      NCT -- NO. USED IN MODES CALCULATION
C      NUFPT -- NO. OF STAGE NEEDED TO PRINTOUT FOR UNBALANCE
      WRITE(6,720) N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NUFPT
      NN(K1)=N
      NNB(K1)=NB

      READ(5,730) ISKIP,NSTEP,NCYCLE,NITP,NINT,NPLOT,NORBIT,NTIME,NSPEE
1D,NINC,NOPT,NT
C      ISKIP = 1 -- NO CALCULATION
C      = 0 -- CALCULATE TRANSIENT ORBIT
C      NSTEP -- NO. OF STEPS OF INTEGRATION PER CYCLE
C      NCYCLE -- NO. OF CYCLES
C      NITP -- NO. OF STEPS PER PRINTOUT
C      NINT = 1 -- NEWARK BETA METHOD
C      NPLOT = 1 -- NO PLOT
C      = 0 -- WITH PLOT
C      NORBIT -- NO. OF TRANSIENT ORBIT STAGES DESIRED

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C      NTIME -- NO. OF STAGES TO BE PLOTTED IN RESPONSE VS TIME CURVE
C      NSPEED = 0
C      NINC = 0 INPUT INITIAL CONDITION
C      = 1 -- INITIAL CONDITION FROM STEADY STATE ORBIT
C      ( WITH SMALL PERTURBATION )
C      = 2 -- INPUT MODAL INITIAL DATA
C      NOPT = 0
C      NT -- NO. OF STAGES FOR TRANSIENT PRINTOUT
      WRITE(6,730) ISKIP,NSTEP,NCYCLE,NITP,NINT,NPLOT,NORBIT,NTIME,NSPEE
1D,NINC,NOPT,NT
      IF (NB.EQ.0) GO TO 20

      READ (5,740) (LLBD(J),J=1,NB)
C      LLBD -- LOCATION NO. OF BEARINGS
      WRITE(6,740) (LLBD(J),J=1,NB)

      DO 19 J=1,NB
      READ (5,*) KXX(J),KXA(J),KXY(J),KXB(J),KXZ(J),CXX(J),CXA(J),CXY
1(J),CXB(J),CXZ(J)
      WRITE(6,750) KXX(J),KXA(J),KXY(J),KXB(J),KXZ(J),CXX(J),CXA(J),CXY
1(J),CXB(J),CXZ(J)
      READ (5,*) KAX(J),KAA(J),KAY(J),KAB(J),KAZ(J),CAX(J),CAA(J),CAY
1(J),CAB(J),CAZ(J)
      WRITE(6,750) KAX(J),KAA(J),KAY(J),KAB(J),KAZ(J),CAX(J),CAA(J),CAY
1(J),CAB(J),CAZ(J)
      READ (5,*) KYX(J),KYA(J),KYY(J),KYB(J),KYZ(J),CYX(J),CYA(J),CYY
1(J),CYB(J),CYZ(J)
      WRITE(6,750) KYX(J),KYA(J),KYY(J),KYB(J),KYZ(J),CYX(J),CYA(J),CYY
1(J),CYB(J),CYZ(J)
      READ (5,*) KBX(J),KBA(J),KBY(J),KBB(J),KBZ(J),CBX(J),CBA(J),CBY
1(J),CBB(J),CBZ(J)
      WRITE(6,750) KBX(J),KBA(J),KBY(J),KBB(J),KBZ(J),CBX(J),CBA(J),CBY
1(J),CBB(J),CBZ(J)
      READ (5,*) KZX(J),KZA(J),KZY(J),KZB(J),KZZ(J),CZX(J),CZA(J),CZY
1(J),CZB(J),CZZ(J)
      WRITE(6,750) KZX(J),KZA(J),KZY(J),KZB(J),KZZ(J),CZX(J),CZA(J),CZY
1(J),CZB(J),CZZ(J)
19 CONTINUE
C ----- BEARING STIFFNESS TK**
C ----- BEARING DAMPING TC**
C      X -- DIRECTION OF X
C      A -- DIRECTION OF X ROTATION
C      Y -- DIRECTION OF Y
C      B -- DIRECTION OF Y ROTATION
C      Z -- DIRECTION OF Z

      DO 20 J=1,NB
      LTLBD(J,K1)=LLBD(J)
      TKXX(J,K1)=KXX(J)
      TKXY(J,K1)=KXY(J)
      TKXA(J,K1)=KXA(J)
      TKXB(J,K1)=KXB(J)
      TKXZ(J,K1)=KXZ(J)
      TCXX(J,K1)=CXX(J)
      TCXY(J,K1)=CXY(J)
      TCXA(J,K1)=CXA(J)
      TCXB(J,K1)=CXB(J)
      TCXZ(J,K1)=CXZ(J)
      TKYX(J,K1)=KYX(J)
      TKYY(J,K1)=KYY(J)
      TKYA(J,K1)=KYA(J)

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TKYB(J,K1)=KYB(J)
TKYZ(J,K1)=KYZ(J)
TCYX(J,K1)=CYX(J)
TCYY(J,K1)=CYY(J)
TCYA(J,K1)=CYA(J)
TCYB(J,K1)=CYB(J)
TCYZ(J,K1)=CYZ(J)
TKAX(J,K1)=KAX(J)
TKAY(J,K1)=KAY(J)
TKAA(J,K1)=KAA(J)
TKAB(J,K1)=KAB(J)
TKAZ(J,K1)=KAZ(J)
TCAX(J,K1)=CAX(J)
TCAY(J,K1)=CAY(J)
TCAA(J,K1)=CAA(J)
TCAB(J,K1)=CAB(J)
TCAZ(J,K1)=CAZ(J)
TKBX(J,K1)=KBX(J)
TKBY(J,K1)=KBY(J)
TKBA(J,K1)=KBA(J)
TKBB(J,K1)=KBB(J)
TKBZ(J,K1)=KBZ(J)
TCBX(J,K1)=CBX(J)
TCBY(J,K1)=CBY(J)
TCBA(J,K1)=CBA(J)
TCBB(J,K1)=CBB(J)
TCBZ(J,K1)=CBZ(J)
TKZX(J,K1)=KZX(J)
TKZY(J,K1)=KZY(J)
TKZA(J,K1)=KZA(J)
TKZB(J,K1)=KZB(J)
TKZZ(J,K1)=KZZ(J)
TCZX(J,K1)=CZX(J)
TCZY(J,K1)=CZY(J)
TCZA(J,K1)=CZA(J)
TCZB(J,K1)=CZB(J)
TCZZ(J,K1)=CZZ(J)

```

20

CONTINUE

IF (NNLIN.EQ.0) GO TO 30

READ(5,760) (LLNB(J),NLB(J),VIS(J),ANR(J),ANL(J),ANC(J),J=1,NNLIN
1)

C LLNB -- LOCATION NO. OF NONLINEAR BEARING
C NLB -- BEARING NO. OF NONLINEAR BEARINGS
C VIS -- VISCOUSITY OF LUBRICATE (LB/IN**2)
C ANR -- RADIUS OF BEARING (IN)
C ANL -- LENGTH OF BEARING (IN)
C ANC -- CLEARANCE OF BEARING (IN)

WRITE(6,760) (LLNB(J),NLB(J),VIS(J),ANR(J),ANL(J),ANC(J),J=1,NNLIN
1)

30

CONTINUE

IF (NMB.EQ.0) GO TO 40

READ (5,770) (LLNMB(J),J=1,NMB)

C LLNMB -- LOCATION NO. OF MOMENT RESISTING BEARING
WRITE(6,770) (LLNMB(J),J=1,NMB)

DO 35 I=1,NMB

DO 35 J=1,4

READ (5,780) (SLNMB(I,J,K),K=1,4), (CLNMB(I,J,K),K=1,4)

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35      WRITE(6,780) (SLNMB(I,J,K),K=1,4),(CLNMB(I,J,K),K=1,4)
      CONTINUE

40      CONTINUE
      READ (5,*) NGYR,E,SPEED1,SPEED2,ANGACL,BETA
C      NGYR -- NO. OF GYROSCOPIC ROTOR
C      E -- SECTION YOUNG'S MODULUS *1.0E-5
C      SPEED1 -- ROTOR'S OPERATING SPEED ( RPM )
C      SPEED2 -- ROTOR'S INITIAL OPERATING SPEED ( RPM )
C      ANGACL -- ANGULAR ACCELERATION OF ROTOR
C      BETA -- BETA PARAMETER USED FOR NEWMARK BETA METHOD
      WRITE(6,790) NGYR,E,SPEED1,SPEED2,ANGACL,BETA
      TSPEED(K1)=SPEED1

      READ(5,*) (EXTW(J),DX(J),DDXT(J),DDNT(J),RP(J),RT(J),EM6(J),
1          RO(J),GGO(J),TK(J), J=1,N)
C      EXTW -- INPUT EXTERNAL WEIGHT PER ELEMENT OF ROTOR
C      DX -- ELEMENT LENGTH OF ROTOR
C      DDXT -- EXTERNAL DIAMETER PER ELEMENT OF ROTOR
C      DDNT -- INTERNAL DIAMETER PER ELEMENT OF ROTOR
C      RP -- POLAR ENERTIA MOMENT PER ELEMENT OF ROTOR ( LB*IN**2 )
C      RT -- TRANSVERS ENERTIA MOMENT PER ELEMENT OF ROTOR ( LB*IN**2 )
C      EM6 -- YOUNG'S MODULUS PER ELEMENT OF ROTOR *1.E-5
C      RO -- DENSITY PER ELEMENT OF ROTOR
C      GGO -- SHEAR'S MODULUS PER ELEMENT *1.0E-5
C      TK -- TORTIONAL CONSTRAINT MOMENT PER ELEMENT *1.0E-15
      WRITE(6,800) (EXTW(J),DX(J),DDXT(J),DDNT(J),RP(J),RT(J),EM6(J),
1          RO(J),GGO(J),TK(J), J=1,N)
      DO 33 J=1,N
      TK(J)=1.0D15*TK(J)
      TEXTW(J,K1)=EXTW(J)
      TDX(J,K1)=DX(J)
      TDDXT(J,K1)=DDXT(J)
      TDDNT(J,K1)=DDNT(J)
      TRP(J,K1)=RP(J)
      TRT(J,K1)=RT(J)
      TEM6(J,K1)=EM6(J)
      TRO(J,K1)=RO(J)
      TGGO(J,K1)=GGO(J)
      TTK(J,K1)=TK(J)
33      CONTINUE

      IF (NF.EQ.0) GO TO 50
      READ (5,810) (LLFF(J),FX(J),FY(J),J=1,NF)
C      LLFF -- LOCATION NO. OF EXTERNAL FORCE OF ROTOR
C      FX -- EXTERNAL FORCE ON X-DIRECTION
C      FY -- EXTERNAL FORCE ON Y-DIRECTION
      WRITE(6,810) (LLFF(J),FX(J),FY(J),J=1,NF)
      DO 55 I=1,NF
      LTLFF(I,K1)=LLFF(I)
      TSFX(I,K1)=FX(I)
55      TSFY(I,K1)=FY(I)
50      CONTINUE

      IF (NU.EQ.0) GO TO 60
      READ (5,*) (LLUF(J),UX(J),UY(J),SUX(J),SUY(J),J=1,NU)
C      LLUF -- LOCATION NO. OF UNBALANCE OF ROTOR
C      UX -- X-DIR UNBALANCE ( OZ-IN )
C      UY -- Y-DIR UNBALANCE ( OZ-IN )
C      SUX -- SUDDEN INCREASE UNBALANCE OF X-DIRECTION ( OZ-IN )

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C      SUY -- SUDDEN INCREASE UNBALANCE OF Y-DIRECTION ( OZ-IN )
      WRITE(6,810) (LLUF(J),UX(J),UY(J),SUX(J),SUY(J),J=1,NU)
      DO 60 J=1,NU
      LTLUF(J,K1)=LLUF(J)
      TUX(J,K1)=UX(J)
      TUY(J,K1)=UY(J)
      TSUX(J,K1)=SUX(J)
      TSUY(J,K1)=SUY(J)
60     CONTINUE

      IF (NS.EQ.0) GO TO 70
C ----- SKEW DISK IS NEGLECTED IN THIS PROGRAM
      READ (5,810) (LLSK(J),FSK(J),PSK(J),J=1,NS)
      WRITE(6,810) (LLSK(J),FSK(J),PSK(J),J=1,NS)
70     CONTINUE

      IF (NUFPT.EQ.0) GO TO 80
      READ (5,820) (LLUT(J),J=1,NUFPT)
      WRITE(6,820) (LLUT(J),J=1,NUFPT)
80     CONTINUE

      IF (NT.EQ.0) GO TO 90
      READ (5,820) (LLNT(J),J=1,NT)
C      LLNT -- LOCATION NO. FOR PRINTOUT OF ROTOR IN TRANSIENT ANALYSIS
      WRITE(6,820) (LLNT(J),J=1,NT)
      DO 90 J=1,NT
      LTLNT(J,K1)=LLNT(NT)
90     CONTINUE

      IF(NINC.NE.2)GO TO 94
      READ(5,821)NAB,CTIME
      WRITE(6,821)NAB,CTIME
      DO 92 J=1,NAB
      READ(5,822)A3(1,J),B3(1,J),A2(1,J),B2(1,J)
      WRITE(6,822)A3(1,J),B3(1,J),A2(1,J),B2(1,J)
      AA3(1,J,K)=A3(1,J)
      AA2(1,J,K)=A2(1,J)
      BB3(1,J,K)=B3(1,J)
      BB2(1,J,K)=B2(1,J)
92     CONTINUE
94     CONTINUE

      IF(NBOW.EQ.0) GO TO 95
      READ (5,830) (BOW(J),PBOW(J),XIDC(J),YIDC(J),VXIDC(J),VYIDC(J),J=1
1,N)
      WRITE(6,830) (BOW(J),PBOW(J),XIDC(J),YIDC(J),VXIDC(J),VYIDC(J),J=1
1,N)
95     CONTINUE

      READ (5,*) SPI,SPL,DSP
C      SPI --
      WRITE(6,840) SPI,SPL,DSP

      READ (5,*) SPE1, SPE2,SPE3
C      SPE1 -- INITIAL SPEED FOR TORTIONAL CRITICAL SPEED ANALYSIS
C      SPE2 -- FINAL SPEED FOR TORTIONAL CRITICAL SPEED ANALYSIS
C      SPE3 -- SPEED INCREMENT FOR TORTIONAL CRITICAL SPEED ANALYSIS
C      ( RPM )
      WRITE(6,840) SPE1,SPE2,SPE3

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      IF (ISKU.EQ.1) GO TO 100
      READ (5,*) SPS,SPF,SPN
C      SPS -- INITIAL SPEED FOR UNBALANCE RESPONSE CALCULATION
C      SPF -- FINAL SPEED FOR UNBALANCE RESPONSE CALCULATION
C      SPN -- SPEED INCREMENT FOR UNBALANCE RESPONSE CALCULATION
      WRITE(6,850) SPS,SPF,SPN
100    CONTINUE

      READ(5,851) NBMOP
C      NBMOP = 0 NO CALCULATION
C      = 1  $A(T) = (E ** (A(T) * T) * \cos(A(T) * T))$ 
C      = 2  $A(T) = \cos(A(T) * T) ** 2$ 
      WRITE (6,851) NBMOP
      IF (NBMOP.EQ.0) GO TO 103
      READ(5,852) (ACON1(I),I=1,NB)
      WRITE(6,852) (ACON1(I),I=1,NB)
      READ(5,852) (ACON2(I),I=1,NB)
      WRITE(6,852) (ACON2(I),I=1,NB)
      READ(5,853) (APH1(I),I=1,NB)
      WRITE(6,853) (APH1(I),I=1,NB)
      READ(5,853) (APH2(I),I=1,NB)
      WRITE(6,853) (APH2(I),I=1,NB)
      DO 102 J=1,NNB(K1)
      TAOMG1(J,K1)=APH1(J)*3.14159/30.0
      TAOMG2(J,K1)=APH2(J)*3.14159/30.0
      NNBMOP(J)=NBMOP
      TACON1(J,K1)=ACON1(J)
102    TACON2(J,K1)=ACON2(J)

103    CONTINUE
      READ(5,*) NSRUB,NSEU
C      NSRUB -- NO. OF RUB STAGES
C      NSEU -- NO. OF SUDDEN INCREASE UNBALANCE STAGES
      WRITE (6,854) NSRUB,NSEU

      IF(NSRUB.EQ.0) GO TO 106
      READ(5,*) NFACT,IND,KR,ABSO
C      NFACT -- STEP FACTOR OF RUB
C      IND = 0 FOR CASING STIFFNESS
C      = 1 BLADE EQUATION
C      = 2 LINEARIZED STIFFNESS
C      KR -- DIRECT CASING STIFFNESS
C      ABSO -- FRICTION COEFFICIENT
      WRITE (6,855) NFACT,IND,KR,ABSO

      READ(5,*) (NRUB(J),CLEAR(J),J=1,NSRUB)
C      NRUB -- LOCATION NO. OF RUB STAGE
C      CLEAR -- CLEARANCE OF RUB
      WRITE(6,856) (NRUB(J),CLEAR(J),J=1,NSRUB)
      NTSRUB(K1)=NSRUB
      NTSEU(K1)=NSEU
      NTFACT(K1)=NFACT
      ITND(K1)=IND
      KTR(K1)=KR
      TABSO(K1)=ABSO
106    CONTINUE

      READ(5,690) ABL1
      WRITE(6,690) ABL1
      READ (5,690) ABL2

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        WRITE(6,690) ABL2
        READ (5,690) ABL3
        WRITE(6,690) ABL3
C ----- THREE TITLE CARDS FOR LABEL IN PLOTS
        WRITE (6,860) NCYCLE,NSTEP,NINT,NINC,NOPT,SPEED2,ANGACL,BETA
        WRITE (6,870)

C      * * * * *
C      *   CALCULATE EFFECTIVE ENERTIA MOMENT OF ROTORS   *
C      * * * * *
        DO 110 I=1,N
        DLX(I)=DX(I)
        CCRI=RO(I)
        CCEI=EM6(I)
        IF (CCRI.GT.0.001) GOTO 105
        RO(I)=0.283
105     CONTINUE
        ENER(I)=3.14159*(DDXT(I)**4.-DDNT(I)**4.)/64.
        IF (CCEI.GT.0.001) GOTO 107
        EM6(I)=E
107     CONTINUE
        EI(I)=EM6(I)*ENER(I)
        DL=ABS(DX(I))
110     SW1(I)=3.14159*(DDXT(I)**2.-DDNT(I)**2.)*DL*RO(I)/4.0
        W(1)=SW1(1)/2.+EXTW(1)
        WT=W(1)
        ZLT=DX(1)
        DO 120 I=2,N
        W(I)=SW1(I-1)/2.0+SW1(I)/2.0+EXTW(I)
C      W(I) -- TOTAL EFFECTIVE SHAFT WEIGHT
        TW(I,K1)= W(I)
        WT=WT+W(I)
120     ZLT=ZLT+DX(I)
        IF (NGYR) 130,150,130
130     RP(1)=RP(1)+ENER(1)*RO(1)*DX(1)
        RT(1)=RT(1)+SW1(1)*((DDXT(1)**2.0+DDNT(1)**2.0)/16.0+((DX(1)/2.0)*
1*2.0)/3.0)/2.0
        DO 140 I=2,N
        RP(I)=RP(I)+RO(I)*ENER(I)*DX(I)+ENER(I-1)*DX(I-1)*RO(I-1)
        RT(I)=RT(I)+SW1(I)*((DDXT(I)**2.0+DDNT(I)**2.0)/16.0+((DX(I)/2.0)*
1*2.0)/3.0)/2.0+SW1(I-1)*((DDXT(I-1)**2.0+DDNT(I-1)**2.0)/16.0+((DX
2(I-1)/2.0)**2.0)/3.0)/2.0
140     CONTINUE
150     SRP=0.0
        DO 160 I=1,N
160     SRP=SRP+RP(I)
        DO 180 I=1,N
        WRITE (6,880) I,W(I),DX(I),DDXT(I),DDNT(I),ENER(I),RP(I),RT(I),
1EM6(I),EI(I)
        IF (I-50) 180,170,180
170     WRITE (6,1080)
180     CONTINUE
        WRITE (6,890) WT,ZLT
        WRITE (6,900)
        WRITE (6,910)
        WRITE (6,920) (J,LLBD(J),KXX(J),KXY(J),KYX(J),KYY(J),J=1,NB)
        WRITE (6,930)
        WRITE (6,940)
        WRITE (6,920) (J,LLBD(J),CXX(J),CXY(J),CYX(J),CYY(J),J=1,NB)
        IF (NMB.EQ.0) GO TO 200

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DO 190 I=1,NMB
WRITE (6,950) I,LLNMB(I)
DO 190 J=1,4
WRITE (6,960) (SLNMB(I,J,K),K=1,4),(CLNMB(I,J,K),K=1,4)
190 CONTINUE
200 IF (NNLIN.EQ.0) GO TO 220
WRITE (6,1170)
DO 210 J=1,NNLIN
WRITE (6,1180) J,LLNB(J),NLB(J),VIS(J),ANR(J),ANL(J),ANC(J)
210 CONTINUE
220 IF (NF.EQ.0) GO TO 230
WRITE (6,970)
WRITE (6,980) (LLFF(J),FX(J),FY(J),J=1,NF)
230 IF (NS.EQ.0) GO TO 240
WRITE (6,990)
WRITE (6,1000) (LLSK(J),FSK(J),PSK(J),J=1,NS)
240 IF (NU.EQ.0) GO TO 260
WRITE (6,1010)
WRITE (6,1020)
WRITE (6,1030) (LLUF(J),UX(J),UY(J),J=1,NU)
DO 250 J=1,NU
UX(J)=UX(J)/(16.*386.4)
250 UY(J)=UY(J)/(16.*386.4)
260 CONTINUE
IF (NBOW.EQ.0) GO TO 275
WRITE (6,1040)
DO 270 J=1,N
WRITE (6,1050) J,BOW(J),PBOW(J),XIDC(J),YIDC(J),VXIDC(J),VYIDC(J)
270 CONTINUE
275 CONTINUE
WRITE (6,1060)

C      * * * * *
C ---- *   CALCULATE ROTOR'S LATERAL MODAL SHAPE   *
C      * * * * *

DO 280 I=1,NB
AVK=(KXX(I)+KYY(I))/2.
WRITE (6,1070) I,AVK
280 CONTINUE
WRITE (6,1071) NBMOP
IF(NBMOP.EQ.0) GO TO 283
DO 282 I=1,NB
WRITE (6,1072) I,ACON1(I),ACON2(I),APH1(I),APH2(I)
282 CONTINUE
283 CONTINUE
NC=1
C   NC=LOCAL CRITICAL SPEED  NO.
WRITE (6,1080)
LN=3
C   SPI=INITIAL SPEED,SPL=FINAL SPEED,DSP=SPEED INCREMENT-RPM
SPD=SPI
DETP=0.
MA=0
MB=0
WRITE (6,1080)
WRITE (6,1090) SPI,SPL,DSP
LN=1
WRITE (6,1100)
LN=LN+3
DIN=DSP

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```

290   I=1
      J=1
      SPSQ=SPD*SPD
C     COMPUTE ANG. VELOCITY
      ANSP=SPD*0.10471976
      ANSP2=ANSP*ANSP
      VP=0.
      ZMP=0.
      EYP=0.
      ETHP=1.0
      M=1
300   I=I+1
      II=I-1
      IF (II-LLBD(J)) 330,310,330
310   AK=(KXX(J)+KYY(J))/2.
      AKK(J)=AK
      TAKK(J,K1)=AKK(J)
      IF (J-NB) 320,340,340
320   J=J+1
      GO TO 340
330   AK=0.
340   VP=VP+(W(I-1)*ANSP2/386.4-AK)*EYP
      ZMP=ZMP-ANSP2*(RT(I-1))*ETHP/386.4
      EY=EYP+DX(I-1)*ETHP+DX(I-1)**2*ZMP/(2.E6*EI(I-1))+DX(I-1)**3*VP/(6
1.E6*EI(I-1))
      ETH=ETHP+DX(I-1)*ZMP/(1.E6*EI(I-1))+DX(I-1)**2*VP/(2.E6*EI(I-1))
      ZM=ZMP+DX(I-1)*VP
      V=VP
      IF (M.EQ.2) GO TO 350
      EY1(I)=EY
      EAN1(I)=ETH
      IF (I.GT.N) GO TO 360
      ZMP=ZM
      VP=V
      EYP=EY
      ETHP=ETH
      GO TO 300
350   EY2(I)=EY
      EAN2(I)=ETH
      ZMP=ZM
      VP=V
      EYP=EY
      ETHP=ETH
      IF (I.GT.N) GO TO 370
      GO TO 300
360   M=2
      ZM1=ZM
      VR1=V
      J=1
      I=1
      EYP=1.
      ZMP=0.
      ETHP=0.
      VP=0.
      GO TO 300
370   DET=VR1*ZM-V*ZM1
      IF (ABS(DETP).LT.0.0001) GO TO 420
      IF (MA.EQ.1) GO TO 400
      IF (ABS(DET).LT.1.) GO TO 450
      IF (DETP*DET) 380,420,420

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```

380   DOLD=DETP
390   MA=1
      IF (ABS(DET).LT.1.) GO TO 450
      IF (DIN.LT.1.E-6) GO TO 450
      DIN=DIN/2.
      DETPP=DETP
      DETP=DET
      SPD=SPD-DIN
      GO TO 290
400   IF (ABS(DET).LT.1.) GO TO 450
      IF (DOLD*DET) 390,420,410
410   CONTINUE
      IF (ABS(DET).LT.1.) GO TO 450
      IF (DIN.LT.1.E-6) GO TO 450
      DIN=DIN/2.
      SPD=SPD+DIN
      DETPP=DETP
      DETP=DET
      GO TO 290
420   IF (LN-54) 440,440,430
430   WRITE (6,1080)
      LN=1
440   WRITE (6,1110) SPD,DET
      LN=LN+1
      SPD=SPD+DSP
      DIN=DSP
      IF(NC.GT.NMODE) GO TO 610
      IF (SPD.GT.SPL) GO TO 610
      DETPP=DETP
      DETP=DET
      SSPD=SPD
      GO TO 290
450   MA=0
      WRITE (6,1110) SPD,DET
      LN=LN+1
      IF (LN-50) 470,470,460
460   WRITE (6,1080)
      LN=1
470   WRITE (6,1120) NC
      WRITE (6,1130)
      WRITE (6,1110) SPD,DET
      CRT(NC)=SPD
      TCRT(NC,K1)=CRT(NC)
      NC=NC+1
      LN=LN+3
      EY1(1)=0.
      EY2(1)=1.
      DTX=0.
      I=1
      IF (LN-50) 490,490,480
480   WRITE (6,1080)
      LN=1
490   WRITE (6,1140)
      LN=LN+2
500   DEFL(I)=V*EY1(I)-VR1*EY2(I)
      IF (I.NE.1) GO TO 510
      EYTH(I)=V
      GO TO 520
510   EYTH(I)=EAN1(I)*V-EAN2(I)*VR1
520   DEFA=ABS(DEFL(I))

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        DMXA=ABS (DTX)
        I=I+1
        IF (DEFA-DMXA) 540,540,530
530     DTX=DEFL(I-1)
540     IF (I-N) 550,550,560
550     GO TO 500
560     DO 570 I=1,N
        DPC(I)=DEFL(I)/DTX
        EYTH(I)=EYTH(I)/DTX
        EEYTH(NC-1,I)=EYTH(I)
570     DDPC(NC-1,I)=DPC(I)
        DO 600 I=1,N
        LN=LN+1
        IF (LN-54) 590,590,580
580     WRITE (6,1080)
        LN=1
590     WRITE (6,1150) I,DPC(I),EYTH(I)
        LN=LN+1
600     CONTINUE
        SPD=SSPD+DSP
        DETP=0.
        GO TO 290
610     CONTINUE
        DO 620 IK=1,NB
        KXX(IK)=KXX(IK)-AKK(IK)
620     KYY(IK)=KYY(IK)-AKK(IK)
        NCS=NC-1
        DO 650 II=1,NCS
        WMOD(II)=0.
        DO 630 JJ=1,N
630     WMOD(II)=WMOD(II)+RT(JJ)*EEYTH(II,JJ)**2+W(JJ)*DDPC(II,JJ)**2
        WMOD(II)=WMOD(II)/386.4
        TWMOD(II,K1)=WMOD(II)
        DO 640 KI=1,N
        EEYTH(II,KI)=EEYTH(II,KI)/(WMOD(II)**0.5)
        DDPC(II,KI)=DDPC(II,KI)/(WMOD(II)**0.5)
        TEEYTH(II,KI,K1)=EEYTH(II,KI)
640     TDDPC(II,KI,K1)=DDPC(II,KI)
650     CONTINUE
        DO 660 II=1,NCS
        WRITE (6,1190) II,CRT(II),WMOD(II)
        DO 660 JJ=1,N
        WRITE (6,1200) JJ,DDPC(II,JJ),EEYTH(II,JJ)
660     CONTINUE
        WRITE (6,1210)
        DO 680 II=1,NCS
        DO 670 JJ=1,NCS
        TMX(II,JJ)=0.
        DO 670 KI=1,N
        TMX(II,JJ)=TMX(II,JJ)+W(KI)*DDPC(JJ,KI)*DDPC(II,KI)/386.4+RT(KI)*E
1EYTH(II,KI)*EEYTH(JJ,KI)/386.4
670     CONTINUE
        WRITE (6,1160) (TMX(II,JJ),JJ=1,NCS)
680     CONTINUE
        NCT=NCS
        NNNCT(K1)=NCT

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C      * * * * *
C ---- *   CALCULATE ROTOR'S TORTIONAL MODAL SHAPE   *
C      * * * * *

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DO 1234 I=1,2
1234 CALL TOR(N,NCS,K1,I)
123  CONTINUE

C      * * * * *
C ----- * INPUT BOX'S DATA *
C      * * * * *
      READ(5,*) NMBB,NDB,NODEB
C      NMBB -- MODES NO. OF BOX
C      NDB -- NO. OF NODES OF BOX
C      NODEB -- DEGREE OF FREEDOM FOR EACH NODE
      WRITE(6,*)NMBB,NDB,NODEB
C      WRITE(10,*)NMBB

      DO 195 K=1,NSTA
      READ (5,*) (LBLBT(I,K),I=1,NNB(K))
C      LBLBT -- LOCATION NO. OF BEARINGS ON BOX
      WRITE (6,*) (LBLBT(I,K),I=1,NNB(K))
195  CONTINUE

      DO 199 K=1,NSTA
      READ (5,*) (BKZZ(I,K),I=1,NNB(K))
C      BKZZ -- Z-DIRECTION CASING STIFFNESS
      WRITE (6,*) (BKZZ(I,K),I=1,NNB(K))
199  CONTINUE

      READ (5,*) NPT
C      NPT -- NO. OF BOX'NODES FOR DEFORMATION ANALYSIS

      READ (5,*) (NPTNO(I),I=1,NPT)
C      NPTNO -- LOCATION NO. OF NODES FOR DEFORMATION ANALYSIS ON BOX

      DO 64 IN=1,NMBB
      READ (5,1260) OMEGS(IN)
C      OMEGS -- NATURAL FREQUENCIES OF BOX
      WRITE(6,1262) OMEGS(IN)

      DO 64 ID=1,NDB
      READ(5,1265) IA,(BX1(IN,ID,IX),IX=1,5)
      READ(5,*) IA,(BX1(IN,ID,IX),IX=1,5)
C      BX1 -- MODAL SHAPES OF BOX
      WRITE(6,1265) IA,(BX1(IN,ID,IX),IX=1,5)
64  CONTINUE

      N9=NSTEP*NCYCLE
      FCYCLE=NCYCLE
C      TTIME1=60.0*FCYCLE/SPEED1
      TTIME1=60.0/(SPEED1*NSTEP)
      FSAMPLE=1.0/TTIME1
      WRITE(7,*) NSTA,N9,NNNCT(1),FSAMPLE
      WRITE(8,*) NSTA,N9,NNNCT(1),FSAMPLE
      WRITE(9,*) NSTA,N9,NNNCT(1),FSAMPLE
      WRITE(10,*)NSTA,N9,NNNCT(1),FSAMPLE
      WRITE(11,*)NSTA,N9,NNNCT(1),FSAMPLE
      WRITE(12,*)NSTA,N9,NNNCT(1),FSAMPLE
      WRITE(13,*)NSTA,N9,NNNCT(1),FSAMPLE

C      * * * * *
C ----- * CALCULATE DYNAMIC BEHAVIOR OF THE WHOLE SYSTEM *

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C      * * * * *
      CALL TMM (NSTA)

690  FORMAT (80A1)
700  FORMAT (3(80A1,/))
703  FORMAT (2X,3I6,F10.3,I4,F10.3)
710  FORMAT (/ ,20X,'MODAL ANALYSIS VERSION 3, OCT. 3,1988')
713  FORMAT ( 20X,'X---DIR. MODAL SHAPE OF ROTOR  ')
716  FORMAT ( 20X,'T---DIR. MODAL SHAPE OF ROTOR  ')
719  FORMAT ( 20X,'Z---DIR. MODAL SHAPE OF ROTOR  ')
720  FORMAT (12I5)
730  FORMAT (12I5)
740  FORMAT (3I5)
750  FORMAT (10G10.3)
760  FORMAT (2I5,4G10.2)
770  FORMAT (9I5)
780  FORMAT (8G10.3)
790  FORMAT (I5,5X,6G10.3)
800  FORMAT (10G8.3)
810  FORMAT (I5,5X,4G10.3)
820  FORMAT (I5)
821  FORMAT(I10,F10.7)
822  FORMAT(4E15.6)
830  FORMAT (6G10.3)
840  FORMAT (3G10.3)
850  FORMAT (3G10.3)
851  FORMAT(I5)
852  FORMAT (8F10.5)
853  FORMAT (8F10.3)
854  FORMAT(2I5)
855  FORMAT(2I5,2F11.1)
856  FORMAT(I5,F10.5)
859  FORMAT(I5)
860  FORMAT (//,10X,'NCYCLE=',I3,5X,'NSTEP=',I3,5X,'NINT=',I3,5X,'NINC=
1',I3,5X,'NOPT=',I3,/,10X,'SPEED2=',F10.2,5X,'ANGACL(1/SEC)=' ,F10.3
2,5X,'BETA=' ,F10.5,/)
870  FORMAT (120H STATION NO.      WEIGHT      LENGTH  SHAFT DIA.  SHAFT D
11A.      I      IP-POLAR MOM.  IT-TRANS. MOM.  EX10-6      EI
2,/120H      (LP)      (IN.)  OUTSIDE      INSIDE      (
3IN**4)      (LP-IN**2)      (LB-IN**2)      ,/)
880  FORMAT (I7,F16.3,F12.3,F10.3,F10.3,G11.4,F12.3,F16.3,F11.2,G10.3)
890  FORMAT (16X,7H-----,5X,7H-----/7X,F16.3,F12.3/)
900  FORMAT (/ ,34X,'      LINEAR SUPPORT BEARING STIFFNESS CHARACTERICS'/)
910  FORMAT (5X,16HBEARING BEARING,12X,3HKXX,16X,3HKXY,16X,3HKYX,16X,3
1HKYY,/5X,6HNUMBER,3X,8HLOCATION,8X,7H(LB/IN),11X,7H(LB/IN),11X,7H(
2LB/IN),11X,7H(LB/IN))
920  FORMAT (5X,I3,8X,I3,9X,F11.1,5X,F11.1,8X,F11.1,8X,F11.1)
930  FORMAT (/ ,35X,'      LINEAR SUPPORT BEARING DAMPING CHARACTERISTICS'/
1)
940  FORMAT (5X,16HDAMPING DAMPING,12X,3HCXX,16X,3HCXY,16X,3HCYX,16X,3
1HCYY,/5X,6HNUMBER,3X,8HLOCATION,6X,11H(LB-SEC/IN),10X,11H(LB-SEC/
2IN),10X,11H(LB-SEC/IN),10X,11H(LB-SEC/IN))
950  FORMAT (//,10X,'FULL BEARING NO.',I2,3X,'AT STATION',I3,/)
960  FORMAT (10X,'BEARING STIFFNESS LB/IN',/,4(4(5X,G15.3),/),/,10X,'
1BEARING DAMPING LB-SEC/IN',/,4(4(5X,G15.3),/))
970  FORMAT (//,20X,'EXTERNAL FORCES',/,5X,'STATION NO.',10X,'X',15X,'Y
1',/)
980  FORMAT (10X,I3,2(5X,G15.5))
990  FORMAT (//,20X,'SKEWED DISC',/,5X,'STATION NO.',10X,'SKEW(RAD)',5X
1,'PHASE ANGLE DEG.',/)

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1000  FORMAT (10X,I3,2(5X,G15.5))
1010  FORMAT (///,25X,'ROTOR UNBALANCE IN OZ-IN.',/)
1020  FORMAT (5X,'STATION',10X,'X-UNBALANCE',10X,'Y-UNBALANCE',/)
1030  FORMAT (8X,I2,12X,F10.3,11X,F10.3)
1040  FORMAT (//,20X,'SHAFT INITIAL CONDITIONS',//,5X,'STATION NO.',5X,
1'BOW-MILS',5X,'PHASE ANGLE',5X,'X-DISP',10X,'Y-DISP',10X,'X-VEL',
210X,'Y-VEL',/,34X,'(DEGREES)',6X,'(MILS)',10X,'(MILS)',10X,
3'MILS/IN',10X,'MIL/IN',/)
1050  FORMAT (5X,I3,6(5X,F10.2))
1060  FORMAT (//,10X,'AVERAGE BEARING STIFFNESS USED FOR CRITICAL SPEED
1CALCULATIONS')
1070  FORMAT (10X,'BEARING NO.',I2,5X,'STIFFNESS(LB/IN)',F12.2)
1071  FORMAT(10X,'BASE MOTION =',I5)
1072  FORMAT(10X,'BEARING',I5,'CONSTANTS ARE',2(2X,F10.5),2(2X,F10.3))
1080  FORMAT (1H1,/)
1090  FORMAT (//,5X,' INITIAL SPEED=',F10.2,5X,'FINAL SPEED=',F10.2,5X,'
1SPEED INCREMENT=',F10.2,' RPM',/)
1100  FORMAT (/13X,3HRPM,20X,5HDELTA,12X,2HK1,13X,2HK2/)
1110  FORMAT (10X,F8.1,9X,E17.9)
1120  FORMAT (//,10X,'CRITICAL SPEED NO.',I2)
1130  FORMAT (/,10X,14HCRITICAL SPEED,11X,5HDELTA,/)
1140  FORMAT (/,12X,6HSTA NO,10X,14HNET DEFLECTION,10X,5HANGLE)
1150  FORMAT (12X,I5,13X,F9.5,13X,F9.5)
1160  FORMAT (5X,10(F8.2,2X))
1170  FORMAT (//,10X,'NONLINEAR BEARING FORCES',//,5X,'BEARING NO.',4X,'
1STATION NO.',4X,'SEQUENCE ',5X,'VISCOSITY',6X,'RADIUS',9X,'LENGTH
2',9X,'CLEARANCE',/,35X,'NUMBER ',6X,'LB/IN**2',7X,'(IN.)',10X,'(
3IN.)',10X,'(IN.)',/)
1180  FORMAT (10X,I5,10X,I5,10X,I5,5X,E10.4,5X,E10.4,5X,E10.4,5X,E10.4)
1190  FORMAT (1H1,//,10X,'CRITICAL SPEED NO.',I5,15X,F10.1,'RPM',/,10X,'
1MODAL MASS=',F10.3,2X,'LB-SEC**2/IN',/,10X,'THE ORTHONORMAL MODE
2SHAPES',//,5X,'STATION',8X,'TRANSLATIONAL',7X,'ROTATIONAL')
1200  FORMAT (9X,I3,10X,F10.5,10X,F10.5)
1210  FORMAT (///,10X,'THE ORTHOGONAL CONDITIONS OF MODES',/)
1262  FORMAT (2X,(1X,E10.3))
1260  FORMAT (18X,E13.6)
1265  FORMAT (1X,I3,5(2X,E13.6))
2109  FORMAT (2X,I5,F13.5)
      END

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SUBROUTINE TMM (NSTA)

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C *****
C *   THIS SUBROUTINE USES MODAL ANALYSIS METHOD TO CALCULATE THE   *
C *   GENERAL DYNAMIC BEHAVIOR OF SYSTEM AFTER THE MODAL SHAPES OF *
C *   BOTH ROTORS & BOX HAVE BEEN OBTAINED.                       *
C *****
      IMPLICIT REAL(A-H,O-Z)
      COMPLEX B,C
      REAL MFX,MFY,MUX,MUY,KMX,KMY,KR
      DIMENSION XDTP(10),XVTP(10),XAC(10,5),XLAC(50,5)
      DIMENSION TFX(5,4096),TFY(5,4096),SFX(10),SFY(10)
      DIMENSION SFRAD(10),RFST(10,4096),FXF(5),FYF(5),FZF(5)
      COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10
1      ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
      COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1      ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
      COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1      ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
      COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10

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1      ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1      ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)
COMMON /ADD6/ TOC(16),TOD(16),TOE(16)
COMMON /TFSA/ ATIME(4100), ANG1(4100),ANG2(4100),ANG3(4100),
1      X1(4100),X2(4100),X3(4100),Y1(4100),Y2(4100),Y3(4100)
COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NNCT,N
1UFPT
COMMON /BLK2/ ISKIP,NSTEP,NCYCLE,NITP,NINT,NPLOT,NORBIT,NTIME,NSPE
1ED,NINC,NOPT,NT
COMMON /BLK3/ CRT(10),LLBD(10),LLNB(5),LLNMB(9),LLSK(10),LLNT(10),
1LLUF(10),LLFF(10),LLUT(10),TCRT(10,5)
COMMON /BLK4/
1      SLNMB(9,4,4),CLNMB(9,4,4)
COMMON /BLK5/ UX(10),UY(10),FX(10),FY(10),FSK(10),PSK(10)
COMMON /BLK6/ BOW(100),PBOW(100),XIDC(100),YIDC(100),VXIDC(100),VY
1IDC(100),BXA(100),BYA(100)
COMMON /BLK7/ CMX(10,10),KMX(10,10),EMX(10,10),CMY(10,10),KMY(10,1
10),EMY(10,10)
COMMON /BLK8/ MFX(10),MFY(10),MUX(10),MUY(10),MBX(10),MBY(10)
COMMON /BLK9/ DDPC(10,100),EEYTH(10,100)
COMMON /BLK10/ SPS,SPF,SPN,SPEED1
COMMON /BLK11/ DOX(10,10),DOY(10,10),EOX(10,10),EOY(10,10)
COMMON /BLK15/ RP(100),RT(100)
COMMON /BLK16/ SPEED2,ANGSP,ANGACL,FSPEED
COMMON /BLK18/ AKK(10),TAKK(10,5)
COMMON /BLK19/ DX(100)
COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
10)
COMMON /BLK22/ W(100)
COMMON /BLK24/ B(20,21),C(20)
COMMON /BLK25/ BETA
COMMON /BLK29/ PASP
COMMON /BLK40/ BMMFX(10),BMMFY(10),TBMMFX(10,5),TBMMFY(10,5)
COMMON /BLK41/ NBMOP,ACON1(10),ACON2(10),AOMG1(10),AOMG2(10)
COMMON /BLK42/ CLEAR(100),NRUB(100),KR,IND,NSRUB,ABSO,NFACT
COMMON /BLK43/ RMX(10),RMY(10),TRMX(10,5),TRMY(10,5)
COMMON /BLK46/ NSEU,SUX(10),SUY(10)
COMMON /BLK60/ SFX,SFY
COMMON /BLK61/ TFX,TFY
COMMON /BLK79/ CTIME
COMMON /BLK91/ SFRAD
COMMON /BLK92/ RFST
COMMON /SPEED/ TSPEED(5)
COMMON /JS/ JST(5)
COMMON /SHAPE/ NN(5),NNNCT(5),NNB(5)
COMMON /FOR123/ F12(4100),F13(4100)
COMMON /XYA/ XR1,XR2,XR3,YR1,YR2,YR3,RANG1,RANG2,RANG3
COMMON /OMG/ NNBMO(5),TACON1(10,5),TACON2(10,5),TAOMG1(10,5),
1      TAOMG2(10,5)
COMMON /FO/ FO(5,5),TBRFX(10,5),TBRFY(10,5)
COMMON /KTB13 / NKTB,NSK,INSK(5),ANGL(5,3),UANGL(5,9)
COMMON / KK13 / NP1(4),XG1(4),XMAX1(4),PS11(4)
COMMON /TMU1/ TMUX(10,5),TMUY(10,5),TEXTW(100,5),TDX(100,5)
COMMON /TD1/ TDDXT(100,5),TDDNT(100,5),TRP(100,5)
COMMON /TR1/ TRT(100,5),TEM6(100,5),TRO(100,5),TGGO(100,5)
COMMON /MF1/ LTLFF(10,5),TSFX(10,5),TSFY(10,5),TMFX(10,5)
COMMON /TU1/ LTLUF(10,5),TUX(10,5),TUY(10,5),TSUX(10,5),TSUY(10,5)
COMMON /SEU1/ LTLNT(10,5),NTSRUB(5),NTSEU(5),NTFACT(5),ITND(5)
COMMON /AAB1/ KTR(5),TABSO(5),AA1(2,10,5),AA2(2,10,5),AA3(2,10,5)

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COMMON /BBA1/ BB1(2,10,5),BB2(2,10,5),BB3(2,10,5),TA1(2,10,5)
COMMON /TKB1/ TA2(2,10,5),TA3(2,10,5),TKB(5,5),ALPH(5,5),RCC(5)
COMMON /TMB1/ TMBX(10,5),TMBY(10,5),TWMY(10,5),LTLBD(10,5)
COMMON /TCM1/ TCMX(10,10,5),TCMY(10,10,5),TKMX(10,10,5)
COMMON /TDO1/ TDOX(10,10,5),TDOY(10,10,5),TEOX(10,10,5)
COMMON /TD/ TDDPC(10,100,5),TEMX(10,10,5),TEMY(10,10,5)
COMMON /TW1/ TDMY(10,10,5),TEEYTH(10,100,5),TW(100,5),TWMOD(50,5)
COMMON /LAS/ TTK(100,5),TMFY(10,5),TKMY(10,10,5),TEOY(10,10,5),
1 TDMX(10,10,5)
COMMON /BASE1/ AB,OMEGA,FAB
COMMON /BOX01/ OMEGS(40),BX1(40,200,6),LBLBT(10,5),NMBB,NODEB
COMMON /BOX02/OA1(2,40),OA2(2,40),OA3(2,40),OB1(2,40),
1 OB2(2,40),OB3(2,40),JNODE(20),FXFXM(40),FYFYM(20),FZFZM(20)
COMMON /BOX04/OZ1(2,20),OZ2(2,20),OZ3(2,20),AZ1(2,10,5)
1 ,AZ2(2,10,5),AZ3(2,10,5),TBRFZ(10,5),TOA(16),TOB(16),TOZ(16)
COMMON /BOX03/ BKZZ(10,5)
COMMON /BOX08/ NPT,NPTNO(16)
COMMON /BLK58/ ZF(10,5),ZFV(10,100,5)
C ZF -- Z-DIR NATURAL FREQUENCIES OF ROTOR
C ZFV -- Z-DIR MODAL SHAPES OF ROTOR

IF (NSK.EQ.0) GO TO 20
DO 10 I=1,NSK
II=INSK(I)
C1=cos(ANGL(II,1))
C2=cos(ANGL(II,2))
C3=cos(ANGL(II,3))
S1=sin(ANGL(II,1))
S2=sin(ANGL(II,2))
S3=sin(ANGL(II,3))
UANGL(II,1)=-C2*C3-C1*S2*S3
UANGL(II,2)=-C2*S3-C1*S2*C3
UANGL(II,3)=S1*S2
UANGL(II,4)=S2*C3+C1*C2*S3
UANGL(II,5)=-S2*S3+C1*C2*C3
UANGL(II,6)=-S1*C2
UANGL(II,7)=S1*S3
UANGL(II,8)=S1*C3
UANGL(II,9)=C1
10 CONTINUE
20 CONTINUE

C * * * * *
C ----- * CALCULATE THE COEFFICIENT OF COMPENSATION TERM *
C * * * * *
DO 111 IJK=1,NSTA
111 CALL TMODE1 (IJK)

IF (ISKIP.EQ.1) GO TO 120
SPEED=TSPEED(1)
NSTEP1=NSTEP+1
STEP=NSTEP
FACT=NFACT
TCYCLE=60./SPEED
TIME=0.0
IINT=1
DO 35 JI=1,NSTA

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DO 35 I=1,NNNCT(JI)
AA3(1,I,JI)=0.0
AA2(1,I,JI)=0.0
35  CONTINUE
DO 39 I=1,NMBB
OA3(1,I)=0.0
OA2(1,I)=0.0
39  CONTINUE
51  CONTINUE
701  FORMAT (3G14.6)
      ICOUNT=1
      NK=0
      NPLUS=0
      IF (ABS(ANGACL).LT.0.0001) GO TO 61
      NPLUS=9999
61  CONTINUE
DO 19 KI=1,2
DO 19 I=1,NSTA
LB1=LTLBD(1,I)
LB2=LTLBD(2,I)
LB3=LTLBD(3,I)
SPLB=0.0
DO 55 IO=LB1,LB2-1
55  SPLB=SPLB+TDX(IO,I)
      SLLE=0.0
      LB4=LB1-1
DO 56 I2=1,LB4
56  SLLE=SLLE+TDX(I2,I)
      SLGE=0.
DO 57 I3=LB2,LB3-1
57  SLGE=SLGE+TDX(I3,I)
      N1=NN(I)
      N2=NNNCT(I)
      N3=NNB(I)
19  CONTINUE
      NJ=NPLUS+1
      PASP=0.
      ICT=1
      ICOM=NFACT
      TEAM=TIME
      I4=0

C      * * * * *
C ----- *   THE LOOP WHICH CALCULATES DYNAMIC RESPONSE BEGINS   *
C      * * * * *
DO 110 I=IINT,NCYCLE
TEEM=TIME
NTCS=NSTEP*NFACT
DO 100 J=1,NTCS
I4=I4+1
DELTAT=TCYCLE/(STEP*FACT)
IF (J.GT.NJ) NK=1

C      * * * * *
C ----- *   CALCULATE THE UNBALANCE TERM OF ROTOR EQUATION   *
C      * * * * *
DO 99 I1=1,NSTA
99  CALL TMODE2 (TIME,DELTAT,TSPEED(I1),NK,I1)

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DO 67 I1=1,NSTA
DO 62 IJK=1,NNCT
TBMMFX(IJK,I1)=0.0
TBMMFY(IJK,I1)=0.0
62  CONTINUE
IF(NNBMOP(I1).EQ.0) GO TO 69
IF(NNBMOP(I1).EQ.2) GO TO 64
DO 63 IJK=1,NNB(I1)
OMGT=TAOMG1(IJK,I1)*TIME
BT=(-1.0)*TACON2(IJK,I1)*TIME
EBT=EXP(BT)
XAC(IJK,I1)=TACON1(IJK,I1)*EBT*COS(OMGT)
63  CONTINUE
GO TO 66
64  CONTINUE
DO 65 IJK=1,NNB(I1)
OMGT1=TAOMG1(IJK,I1)*TIME
OMGT2=TAOMG2(IJK,I1)*TIME
XAC(IJK,I1)=TACON1(IJK,I1)*SIN(OMGT1)*SIN(OMGT2)
65  CONTINUE
66  CONTINUE
STLP=(XAC(2,I1)-XAC(1,I1))/SPLB
XLAC(1,I1)=XAC(1,I1)-STLP*SLLE
DO 67 IJK=2,N
IJJ=IJK-1
XLAC(IJK,I1)=XLAC(IJJ,I1)+TDX(IJJ,I1)*STLP
67  CONTINUE

DO 68 I1=1,NSTA
DO 68 IJK=1,NNCT
DO 68 IJJ=1,N
TBMMFX(IJK,I1)=TBMMFX(IJK,I1)-TW(IJJ,I1)*XLAC(IJJ,I1)*TDDPC
* (IJK,IJJ,I1)/386.4
68  CONTINUE
69  CONTINUE
XXK=360.0*TIME/TCYCLE

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```

C      * * * * *
C ----- *   CALCULATE THE GEAR STIFFNESS   *
C      * * * * *
DO 27 KK=1,NKTB
NK=KK+1
XXK1=XXK-PS11(KK)
CALL STIFF (KK,NP1(KK),XG1(KK),XMAX1(KK),XXK1,YK12)
TKB(1,NK)=YK12
TKB(NK,1)=YK12
27  CONTINUE

C      * * * * *
C ----- *   CALCULATE THE BEARING FORCE     *
C      * * * * *
JN=0
DO 999 III=1,NSTA
DO 999 KKK=1,NNNCT(III)
TBRFX(KKK,III)=0.
TBRFY(KKK,III)=0.

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TBRFZ(KKK,III)=0.
999 CONTINUE
DO 998 JJJ=1,NMBB
  FXFXM(JJJ)=0.
998 CONTINUE
DO 88 K3=1,NSTA
  KJST=JST(K3)
DO 86 J3=1,NNB(K3)
  JB=LTLD(J3,K3)
  JBB=LBLBT(J3,K3)
  IF (JBB.EQ.0) GO TO 86
  JN=JN+1
  JNODE(JN)=JBB
  XD=0.0
  YD=0.0
  AD=0.0
  BD=0.0
  ZD=0.0
  XV=0.0
  YV=0.0
  AV=0.0
  BV=0.0
  ZV=0.0
DO 84 I3=1,NNNCT(K3)
  XD=XD+AA3(1,I3,K3)*TDDPC(I3,JB,K3)
  YD=YD+AA3(1,I3,K3)*TEEYTH(I3,JB,K3)
  AD=AD+BB3(1,I3,K3)*TDDPC(I3,JB,K3)
  BD=BD+BB3(1,I3,K3)*TEEYTH(I3,JB,K3)
  ZD=ZD+AZ3(1,I3,K3)*ZFV(I3,JB,K3)
  XV=XV+AA2(1,I3,K3)*TDDPC(I3,JB,K3)
  YV=YV+AA2(1,I3,K3)*TEEYTH(I3,JB,K3)
  AV=AV+BB2(1,I3,K3)*TDDPC(I3,JB,K3)
  BV=BV+BB2(1,I3,K3)*TEEYTH(I3,JB,K3)
  ZV=ZV+AZ2(1,I3,K3)*ZFV(I3,JB,K3)
84 CONTINUE
  XDB=0.0
  YDB=0.0
  ADB=0.0
  BDB=0.0
  ZDB=0.0
  XVB=0.0
  YVB=0.0
  AVB=0.0
  BVB=0.0
  ZVB=0.0
DO 87 I4=1,NMBB
  XDB=XDB+OA3(1,I4)*BX1(I4,JBB,1)
  YDB=YDB+OA3(1,I4)*BX1(I4,JBB,4)
  ADB=ADB+OA3(1,I4)*BX1(I4,JBB,2)
  BDB=BDB+OA3(1,I4)*BX1(I4,JBB,5)
  ZDB=ZDB+OA3(1,I4)*BX1(I4,JBB,3)
  XVB=XVB+OA2(1,I4)*BX1(I4,JBB,1)
  YVB=YVB+OA2(1,I4)*BX1(I4,JBB,4)
  AVB=AVB+OA2(1,I4)*BX1(I4,JBB,2)
  BVB=BVB+OA2(1,I4)*BX1(I4,JBB,5)
  ZVB=ZVB+OA2(1,I4)*BX1(I4,JBB,3)
87 CONTINUE

FD1=TKXX(J3,K3)*(XDB-XD)+TKXA(J3,K3)*(YDB-YD)+TKXY(J3,K3)*(ADB-AD)
&      +TKXB(J3,K3)*(BDB-BD)+TKXZ(J3,K3)*(ZDB-ZD)

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      FD2=TKAX(J3,K3)*(XDB-XD)+TKAA(J3,K3)*(YDB-YD)+TKAY(J3,K3)*(ADB-AD)
&      +TKAB(J3,K3)*(BDB-BD)+TKAZ(J3,K3)*(ZDB-ZD)
      FD3=TKYX(J3,K3)*(XDB-XD)+TKYA(J3,K3)*(YDB-YD)+TKYY(J3,K3)*(ADB-AD)
&      +TKYB(J3,K3)*(BDB-BD)+TKYZ(J3,K3)*(ZDB-ZD)
      FD4=TKBX(J3,K3)*(XDB-XD)+TKBA(J3,K3)*(YDB-YD)+TKBY(J3,K3)*(ADB-AD)
&      +TKBB(J3,K3)*(BDB-BD)+TKBZ(J3,K3)*(ZDB-ZD)
      FD5=TKZX(J3,K3)*(XDB-XD)+TKZA(J3,K3)*(YDB-YD)+TKZY(J3,K3)*(ADB-AD)
&      +TKZB(J3,K3)*(BDB-BD)+TKZZ(J3,K3)*(ZDB-ZD)
      FV1=TCXX(J3,K3)*(XVB-XV)+TCXA(J3,K3)*(YVB-YV)+TCXY(J3,K3)*(AVB-AV)
&      +TCXB(J3,K3)*(BVB-BV)+TCXZ(J3,K3)*(ZVB-ZV)
      FV2=TCAX(J3,K3)*(XVB-XV)+TCAA(J3,K3)*(YVB-YV)+TCAY(J3,K3)*(AVB-AV)
&      +TCAB(J3,K3)*(BVB-BV)+TCAZ(J3,K3)*(ZVB-ZV)
      FV3=TCYX(J3,K3)*(XVB-XV)+TCYA(J3,K3)*(YVB-YV)+TCYY(J3,K3)*(AVB-AV)
&      +TCYB(J3,K3)*(BVB-BV)+TCYZ(J3,K3)*(ZVB-ZV)
      FV4=TCBX(J3,K3)*(XVB-XV)+TCBA(J3,K3)*(YVB-YV)+TCBY(J3,K3)*(AVB-AV)
&      +TCBB(J3,K3)*(BVB-BV)+TCBZ(J3,K3)*(ZVB-ZV)
      FV5=TCZX(J3,K3)*(XVB-XV)+TCZA(J3,K3)*(YVB-YV)+TCZY(J3,K3)*(AVB-AV)
&      +TCZB(J3,K3)*(BVB-BV)+TCZZ(J3,K3)*(ZVB-ZV)
      DO 82 II3=1,NNCNT(K3)
      TBRFX(II3,K3)=TBRFX(II3,K3)+(FD1+FV1)*TDDPC(II3,JB,K3)
&      + (FD2+FV2)*TEEYTH(II3,JB,K3)
      TBRFY(II3,K3)=TBRFY(II3,K3)+(FD3+FV3)*TDDPC(II3,JB,K3)
&      + (FD4+FV4)*TEEYTH(II3,JB,K3)
      TBRFZ(II3,K3)=TBRFZ(II3,K3)+(FD5+FV5)*ZFV(II3,JB,K3)
82    CONTINUE
C      TBRFX -- MODAL BEARING FORCE OF X-DIRECTION ON ROTOR
C      TBRFY -- MODAL BEARING FORCE OF Y-DIRECTION ON ROTOR
C      TBRFZ -- MODAL BEARING FORCE OF Z-DIRECTION ON ROTOR

      DO 83 I5=1,NMBB
      FXFXM(I5)=FXFXM(I5)-(FD1+FV1)*BX1(I5,JBB,1)
      FXFXM(I5)=FXFXM(I5)-(FD2+FV2)*BX1(I5,JBB,4)
      FXFXM(I5)=FXFXM(I5)-(FD3+FV3)*BX1(I5,JBB,2)
      FXFXM(I5)=FXFXM(I5)-(FD4+FV4)*BX1(I5,JBB,5)
      FXFXM(I5)=FXFXM(I5)-(FD5+FV5)*BX1(I5,JBB,3)
83    CONTINUE
C      FXFXM -- MODAL BEARING FORCE ON ROTOR

      86    CONTINUE
      88    CONTINUE

C      * * * * *
C ---- *      SOLVE THE MODAL EQUATION OF ROTOR      *
C      * * * * *
      CALL TACCEL (NSTA)

      NIJ=(I-1)*NSTEP+J
      IF(ICOM.NE.NFACT)GO TO 78
      IF(NNLIN.NE.0)GO TO 75
      DO 74 KK=1,NSTA
      DO 74 IJL=1,NB
      IB=LTLBD(IJL, KK)
      X=0.0
      Y=0.0
      VX=0.0
      VY=0.0
      DO 73 IJN=1,NNCT
      X=X+AA3(1,IJN, KK)*TDDPC(IJN, IB, KK)

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      VX=VX+AA2(1,IJN, KK)*TDDPC(IJN, IB, KK)
      Y=Y+BB3(1,IJN, KK)*TDDPC(IJN, IB, KK)
73      VY=VY+BB2(1,IJN, KK)*TDDPC(IJN, IB, KK)
      TFX(IJL, ICT)=TCXX(IJL, KK)*VX+ TCXA(IJL, KK)*VY+(TKXX(IJL, KK)+TAKK(I
&JL, KK))*X+TKXA(IJL, KK)*Y
74      CONTINUE
75      IF(NSRUB.EQ.0)GO TO 77
      DO 76 IJL=1, NSRUB
76      RFST(IJL, ICT)=SFRAD(IJL)
77      ICT=ICT+1
      ICOM=0
78      ICOM=ICOM+1
      TIME=TIME+DELTAT

```

```

C      * * * * *
C ----- *      SOLVE THE MODAL EQUATION OF BOX & INTEGRATE THE RESULT *
C      * * * * *
      GO TO (70,80), NINT
C ----- WITH NEWMARK BETA METHOD
70      CALL TBETA (NNCT,DELTAT,NSTA,TIME)
      GO TO 90
C ----- WITH EULER METHOD
80      CALL TINTG (NNCT,DELTAT)
90      CONTINUE

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```

      IF(ICOM.NE.1)GO TO 96
      ICOUNT=ICOUNT+1
      FI=ICOUNT
      ATIME(ICOUNT)=FI*DELTAT*FACT
      X1(ICOUNT)=XR1
      X2(ICOUNT)=XR2
      X3(ICOUNT)=XR3
      Y1(ICOUNT)=YR1
      Y2(ICOUNT)=YR2
      Y3(ICOUNT)=YR3
      ANG1(ICOUNT)=RANG1
      ANG2(ICOUNT)=RANG2
      ANG3(ICOUNT)=RANG3
      F12(ICOUNT)=FO(1,2)
      F13(ICOUNT)=FO(1,3)
      DO 93 JI=1,NSTA
      WRITE (7,707) (AA3(1,II,JI),II=1,NNCT)
93      WRITE (8,708) (BB3(1,II,JI),II=1,NNCT)
      WRITE(10,710) (TOA(JI),JI=1,NPT)
96      CONTINUE
      PASP=PASP+DELTAT*SPEED*0.104719
      TCYCLE=60./SPEED
100     CONTINUE
110     CONTINUE
120     CONTINUE
901     FORMAT(4E18.6)
902     FORMAT(F10.7)
      N9=ICOUNT
707     FORMAT (3G14.6)
708     FORMAT (10X,3G14.6)
709     FORMAT (9G9.2 )
710     FORMAT (8G9.2 )
      WRITE(9,9901) (F12(I),I=1,N9)

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9901  FORMAT(F12.6)
      WRITE(11,9) (X1(I),Y1(I),I=1,N9)
      WRITE(12,9) (X2(I),Y2(I),I=1,N9)
9     FORMAT(2X,2F10.7)
      RETURN
      END

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      SUBROUTINE TMODEL (I1)
C *****
C * THIS SUBROUTINE CALCULATES THE MODAL COEFFICIENTS WHICH APPEARS *
C * IN THE MODAL EQUATION OF ROTORS *
C *****
      IMPLICIT REAL(A-H,O-Z)
      REAL MFX,MFY,MUX,MUY,KMX,KMY
      REAL KXX,KXY,KXA,KXB,KXZ
      REAL KYX,KYY,KYA,KYB,KYZ
      REAL KAX,KAY,KAA,KAB,KAZ
      REAL KBX,KBY,KBA,KBB,KBZ
      REAL KZX,KZY,KZA,KZB,KZZ
      COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10
1      ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
      COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1      ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
      COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1      ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
      COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10
1      ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
      COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1      ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)
      COMMON /ADD6/ TOC(16),TOD(16),TOE(16)
      COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NNCT,N
1UFPT
      COMMON /BLK3/ CRT(10),LLBD(10),LLNB(5),LLNMB(9),LLSK(10),LLNT(10),
1LLUF(10),LLFF(10),LLUT(10),TCRT(10,5)
      COMMON /BLK4/
1      SLNMB(9,4,4),CLNMB(9,4,4)
      COMMON /BLK7/ CMX(10,10),KMX(10,10),EMX(10,10),CMY(10,10),KMY(10,1
10),EMY(10,10)
      COMMON /BLK9/ DDPC(10,100),EEYTH(10,100)
      COMMON /BLK11/ DOX(10,10),DOY(10,10),EOX(10,10),EOY(10,10)
      COMMON /BLK22/ W(100)
      COMMON /BLK35/ WMY(10),VIS(5),ANR(5),ANL(5),ANC(5),NLB(5)
      COMMON /SHAPE/ NN(5),NNNCT(5),NNB(5)
      COMMON /TDC / TTCM(10,10,5)
      COMMON /BLK54/ FR(10,5), FFV(10,100,5)
      COMMON /BLK58/ ZF(10,5),ZFV(10,100,5)
      COMMON / RDDT / NTTD(5),LLTD(10,5),TTCC(10,5)
      COMMON /TMU1/ TMUX(10,5),TMUY(10,5),TEXTW(100,5),TDX(100,5)
      COMMON /TD1/ TDDXT(100,5),TDDNT(100,5),TRP(100,5)
      COMMON /TR1/ TRT(100,5),TEM6(100,5),TRO(100,5),TGGO(100,5)
      COMMON /MF1/ LTLFF(10,5),TSFX(10,5),TSFY(10,5),TMFX(10,5)
      COMMON /TU1/ LTLUF(10,5),TUX(10,5),TUY(10,5),TSUX(10,5),TSUY(10,5)
      COMMON /SEU1/ LTLNT(10,5),NTSRUB(5),NTSEU(5),NTFACT(5),ITND(5)
      COMMON /AAB1/ KTR(5),TABSO(5),AA1(2,10,5),AA2(2,10,5),AA3(2,10,5)
      COMMON /BBA1/ BB1(2,10,5),BB2(2,10,5),BB3(2,10,5),TA1(2,10,5)
      COMMON /TKB1/ TA2(2,10,5),TA3(2,10,5),TKB(5,5),ALPH(5,5),RCC(5)
      COMMON /TMB1/ TMBX(10,5),TMBY(10,5), TWMY(10,5),LTLBD(10,5)
      COMMON /TCM1/ TCMX(10,10,5),TCMY(10,10,5),TKMX(10,10,5)
      COMMON /TDO1/ TDOX(10,10,5),TDOY(10,10,5),TEOX(10,10,5)

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COMMON /TD/ TDDPC(10,100,5),TEMX(10,10,5),TEMY(10,10,5)
COMMON /TW1/ TDMY(10,10,5),TEEYTH(10,100,5),TW(100,5),TWMOD(50,5)
COMMON /LAS/ TTK(100,5),TMFY(10,5),TKMY(10,10,5),TEOY(10,10,5),
1 TDMX(10,10,5)
DO 10 I=1,NNNCT(I1)
DO 10 J=1,NNNCT(I1)
TKMX(I,J,I1)=0.
TKMY(I,J,I1)=0.
TEOY(I,J,I1)=0.
TTCM(I,J,I1)=0.
10 CONTINUE
DO 30 I=1,NNB(I1)
J=LTlBD(I,I1)
DO 20 K=1,NNNCT(I1)
DO 20 L=1,NNNCT(I1)
TKMX(K,L,I1)=TKMX(K,L,I1)+TKXX(I,I1)*TDDPC(K,J,I1)*TDDPC(L,J,I1)
TKMY(K,L,I1)=TKMY(K,L,I1)+TKYY(I,I1)*TDDPC(K,J,I1)*TDDPC(L,J,I1)
TKMX(K,L,I1)=(TKMX(K,L,I1)+TKMY(K,L,I1))/2.
20 TEOY(K,L,I1)=TEOY(K,L,I1)+TKZZ(I,I1)*ZFV(K,J,I1)*ZFV(L,J,I1)
30 CONTINUE
DO 100 I=1,NTTD(I1)
L=LLTD(I,I1)
DO 100 J=1,NNNCT(I1)
DO 100 K=1,NNNCT(I1)
TTCM(J,K,I1)=TTCM(J,K,I1)+TTCC(I,I1)*FFV(J,L,I1)*FFV(K,L,I1)*0.0
100 CONTINUE
RETURN
END

```

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SUBROUTINE TMODE2 (T,DELTAT,SPEED,NK,I1)
C *****
C * THIS SUBROUTINE CALCULATES THE MODAL UNBALANCE FOR TRANSIENT *
C * RESPONSE ANALYSIS *
C *****
IMPLICIT REAL(A-H,O-Z)
REAL MBX,MBY
REAL MFX,MFY,MUX,MUY,KMX,KMY
REAL KXX,KXY,KXA,KXB,KXZ
REAL KYX,KYY,KYA,KYB,KYZ
REAL KAX,KAY,KAA,KAB,KAZ
REAL KBX,KBY,KBA,KBB,KBZ
REAL KZX,KZY,KZA,KZB,KZZ
COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NNCT,N
1UFPT
COMMON /BLK2/ ISKIP,NSTEP,NCYCLE,NITP,NINT,NPLOT,NORBIT,NTIME,NSPE
1ED,NINC,NOPT,NT
COMMON /BLK3/ CRT(10),LLBD(10),LLNB(5),LLNMB(9),LLSK(10),LLNT(10),
1LLUF(10),LLFF(10),LLUT(10),TCRT(10,5)
COMMON /BLK5/ UX(10),UY(10),FX(10),FY(10),FSK(10),PSK(10)
COMMON /BLK6/ BOW(100),PBOW(100),XIDC(100),YIDC(100),VXIDC(100),VY
1IDC(100),BXA(100),BYA(100)
COMMON /BLK7/ CMX(10,10),KMX(10,10),EMX(10,10),CMY(10,10),KMY(10,1
10),EMY(10,10)
COMMON /BLK8/ MFX(10),MFY(10),MUX(10),MUY(10),MBX(10),MBY(10)
COMMON /BLK9/ DDPC(10,100),EEYTH(10,100)
COMMON /BLK11/ DOX(10,10),DOY(10,10),EOX(10,10),EOY(10,10)
COMMON /BLK15/ RP(100),RT(100)
COMMON /BLK16/ SPEED2,ANGSP,ANGACL,FSPEED
COMMON /BLK18/ AKK(10),TAKK(10,5)

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COMMON /BLK21/ DMX(10,10),DMY(10,10)
COMMON /BLK29/ PASP
COMMON /SPEED/ TSPEED(5)
COMMON /TMU1/ TMUX(10,5),TMUY(10,5),TEXTW(100,5),TDX(100,5)
COMMON /TD1/ TDDXT(100,5),TDDNT(100,5),TRP(100,5)
COMMON /TR1/ TRT(100,5),TEM6(100,5),TRO(100,5),TGGO(100,5)
COMMON /MF1/ LTLFF(10,5),TSFX(10,5),TSFY(10,5),TMFX(10,5)
COMMON /TU1/ LTLUF(10,5),TUX(10,5),TUY(10,5),TSUX(10,5),TSUY(10,5)
COMMON /SEU1/ LTLNT(10,5),NTSRUB(5),NTSEU(5),NTFACT(5),ITND(5)
COMMON /AAB1/ KTR(5),TABSO(5),AA1(2,10,5),AA2(2,10,5),AA3(2,10,5)
COMMON /BBA1/ BB1(2,10,5),BB2(2,10,5),BB3(2,10,5),TA1(2,10,5)
COMMON /TKB1/ TA2(2,10,5),TA3(2,10,5),TKB(5,5),ALPH(5,5),RCC(5)
COMMON /TMB1/ TMBX(10,5),TMBY(10,5),TWMY(10,5),LTLBD(10,5)
COMMON /TCM1/ TCMX(10,10,5),TCMY(10,10,5),TKMX(10,10,5)
COMMON /TDO1/ TDOX(10,10,5),TDOY(10,10,5),TEOX(10,10,5)
COMMON /TD/ TDDPC(10,100,5),TEMX(10,10,5),TEMY(10,10,5)
COMMON /TW1/ TDMY(10,10,5),TEEYTH(10,100,5),TW(100,5),TWMOD(50,5)
COMMON /LAS/ TTK(100,5),TMFY(10,5),TKMY(10,10,5),TEOY(10,10,5),
1 TDMX(10,10,5)

```

```

PI=3.14159
ANGSP=TSPEED(I1)*PI/30.
DO 10 I=1,NNCT
  TMUX(I,I1)=0.
  TMUY(I,I1)=0.
10 CONTINUE
  DO 30 I=1,NU
    J=LTLUF(I,I1)
    PHI=ATAN2(TUY(I,I1),TUX(I,I1))
    OMT=ANGSP*T+PHI
  C PMT=OMT+3.1415926
    IF (NK.EQ.0) OMT=PASP+PHI
    TME=(TUX(I,I1)*TUX(I,I1)+TUY(I,I1)*TUY(I,I1))**.5
    DO 20 K=1,NNCT
  C TMUX(K,I1)=TMUX(K,I1)+(ANGACL*SIN(OMT)+ANGSP*ANGSP*COS(OMT))
  C 1 *TME*TDDPC(K,J,I1)
  C IF(I1.EQ.2) GOTO 654
    TMUX(K,I1)=TMUX(K,I1)+(ANGACL*SIN(OMT)+ANGSP*ANGSP*COS(OMT))
  C 1 *TME*TDDPC(K,J,I1) +TME*TDDPC(K,J,I1)
  C 1 *ANGSP*ANGSP*(I1-1)*(COS(OMT*2.)/4.+COS(OMT*3.)/5.)
    TMUY(K,I1)=TMUY(K,I1)+(ANGSP*ANGSP*SIN(OMT))
  C 1 *TME*TDDPC(K,J,I1) +TME*TDDPC(K,J,I1)
  C 1 *ANGSP*ANGSP*(I1-1)*(SIN(OMT*2.)/4.+SIN(OMT*3.)/5.)
  C GO TO 20
C654 TMUX(K,I1)=TMUX(K,I1)+(ANGACL*SIN(PMT)+ANGSP*ANGSP*COS(PMT))
  C 1 *TME*TDDPC(K,J,I1) +TME*TDDPC(K,J,I1)
  C 1 *ANGSP*ANGSP*(I1-1)*(COS(PMT*2.)/4.+COS(PMT*3.)/5.)
  C TMUY(K,I1)=TMUY(K,I1)+(ANGSP*ANGSP*SIN(PMT))
  C 1 *TME*TDDPC(K,J,I1) +TME*TDDPC(K,J,I1)
  C 1 *ANGSP*ANGSP*(I1-1)*(SIN(PMT*2.)/4.+SIN(PMT*3.)/5.)
  C TMUY(K,I1)=TMUY(K,I1)+(ANGSP*ANGSP*SIN(OMT)-ANGACL*COS(OMT))
  C 1 *TME*TDDPC(K,J,I1)
20 CONTINUE
30 CONTINUE
RETURN
END

```

SUBROUTINE TACCEL (NSTA)

C *****


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C * THIS SUBROUTINE CALCULATES THE MODAL ACCELERATION BY SOLVING *
C * THE MODAL EQUATIONS OF ROTORS *
C *****
  IMPLICIT REAL(A-H,O-Z)
  REAL MFX,MFY,MUX,MUY,KMX,KMY,KR
  COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10
1    ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
  COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1    ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
  COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1    ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
  COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10
1    ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
  COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1    ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)
  COMMON /ADD6/ TOC(16),TOD(16),TOE(16)
  COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NNCT,N
1UFPT
  COMMON /BLK3/ CRT(10),LLBD(10),LLNB(5),LLNMB(9),LLSK(10),LLNT(10),
1LLUF(10),LLFF(10),LLUT(10),TCRT(10,5)
  COMMON /BLK7/ CMX(10,10),KMX(10,10),EMX(10,10),CMY(10,10),KMY(10,1
10),EMY(10,10)
  COMMON /BLK8/ MFX(10),MFY(10),MUX(10),MUY(10),MBX(10),MBY(10)
  COMMON /BLK9/ DDPC(10,100),EEYTH(10,100)
  COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
10)
  COMMON /BLK21/ DMX(10,10),DMY(10,10)
  COMMON /BLK40/ BMMFX(10),BMMFY(10),TBMMFX(10,5),TBMMFY(10,5)
  COMMON /BLK42/ CLEAR(100),NRUB(100),KR,IND,NSRUB,ABSO,NFACT
  COMMON /BLK43/ RMX(10),RMY(10),TRMX(10,5),TRMY(10,5)
  COMMON /BLK54/ FR(10,5), FFV(10,100,5)
  COMMON /JS/ JST(5)
  COMMON /TOU/ TOUT(5),FORCEZ(5)
  COMMON /SHAPE/ NN(5),NNNCT(5),NNB(5)
  COMMON /FO/ FO(5,5),TBRFX(10,5),TBRFY(10,5)
  COMMON /XYA/ XR1,XR2,XR3,YR1,YR2,YR3,RANG1,RANG2,RANG3
  COMMON /TDC / TTCM(10,10,5)
  COMMON /KTB13 / NKTB,NSK,INSK(5),ANGL(5,3),UANGL(5,9)
  COMMON /TMU1/ TMUX(10,5),TMUY(10,5),TEXTW(100,5),TDX(100,5)
  COMMON /TD1/ TDDXT(100,5),TDDNT(100,5),TRP(100,5)
  COMMON /TR1/ TRT(100,5),TEM6(100,5),TRO(100,5),TGGO(100,5)
  COMMON /MF1/ LTLFF(10,5),TSFX(10,5),TSFY(10,5),TMFX(10,5)
  COMMON /TU1/ LTLUF(10,5),TUX(10,5),TUY(10,5),TSUX(10,5),TSUY(10,5)
  COMMON /SEU1/ LTLNT(10,5),NTSRUB(5),NTSEU(5),NTFACT(5),ITND(5)
  COMMON /AAB1/ KTR(5),TABSO(5),AA1(2,10,5),AA2(2,10,5),AA3(2,10,5)
  COMMON /BBA1/ BB1(2,10,5),BB2(2,10,5),BB3(2,10,5),TA1(2,10,5)
  COMMON /TKB1/ TA2(2,10,5),TA3(2,10,5),TKB(5,5),ALPH(5,5),RCC(5)
  COMMON /TMB1/ TMBX(10,5),TMBY(10,5), TWMY(10,5),LTLBD(10,5)
  COMMON /TCM1/ TCMX(10,10,5),TCMY(10,10,5),TKMX(10,10,5)
  COMMON /TDO1/ TDOX(10,10,5),TDOY(10,10,5),TEOX(10,10,5)
  COMMON /TD/ TDDPC(10,100,5),TEMX(10,10,5),TEMY(10,10,5)
  COMMON /TW1/ TDMY(10,10,5),TEEYTH(10,100,5),TW(100,5),TWMOD(50,5)
  COMMON /LAS/ TTK(100,5),TMFY(10,5),TKMY(10,10,5),TEOY(10,10,5),
1    TDMX(10,10,5)

  IF (NNLIN.EQ.0) GO TO 10
  CALL BNF
10 CONTINUE

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C * * * * *

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C ----- *      CALCULATE ROTOR'S MODAL ACCELERATIONS      *
C      * * * * *
DO 30 I1=1,NSTA
DO 30 L=1,NNNCT(I1)
ABC=0.0
BCA=0.0
CAB=0.0
IF (I1.EQ.1) THEN
JT=2
ELSE
JT=23
END IF
TA1(1,L,I1)=FFV(L,JT,I1)*TOUT(I1)-FR(L,I1)**2*TA3(1,L,I1)
AA1(1,L,I1)=TMUX(L,I1)+TBRFX(L,I1)-(TCRT(L,I1)*0.1047195)**2
1      *AA3(1,L,I1)-AA2(1,L,I1)*0.0
BB1(1,L,I1)=TBRFY(L,I1)-(TCRT(L,I1)*0.1047195)**2
1      *BB3(1,L,I1)-BB2(1,L,I1)-TMUY(L,I1)*(I1-2)+TMUY(L,I1)*0.20
DO 34 JK=1,NNNCT(I1)
TA1(1,L,I1)=TA1(1,L,I1)-TTCM(L,JK,I1)*TA2(1,JK,I1)
AA1(1,L,I1)=AA1(1,L,I1)+TKMX(L,JK,I1)*AA3(1,JK,I1)
BB1(1,L,I1)=BB1(1,L,I1)+TKMX(L,JK,I1)*BB3(1,JK,I1)
34  CONTINUE

C      * * * * *
C ----- *      CALCULATE ROTOR'S GEAR FORCE      *
C      * * * * *
DO 38 K=1,NSTA
IF (K.EQ.I1) GO TO 38
IF ((I1.GT.1).AND.(K.GT.1))      GO TO 38
AB=0.0
BC=0.0
CD=0.0
DE=0.0
EF=0.0
FG=0.0
VE1=0.0
VE2=0.0
FO(I1,K)=0.0
DO 36 I=1,NNNCT(K)
AB=AB+TA3(1,I,K)*FFV(I,JST(K),K)
BC=BC+TA3(1,I,I1)*FFV(I,JST(I1),I1)
CD=CD+AA3(1,I,K)*TDDPC(I,JST(K),K)
DE=DE+AA3(1,I,I1)*TDDPC(I,JST(I1),I1)
EF=EF+BB3(1,I,K)*TDDPC(I,JST(K),K)
FG=FG+BB3(1,I,I1)*TDDPC(I,JST(I1),I1)
VE1= BB2(1,I,I1)*TDDPC(I,JST(I1),I1)+VE1
VE2= BB2(1,I,K)*TDDPC(I,JST(K),K)+VE2
36  CONTINUE

A=-ABS(RCC(K)*AB+RCC(I1)*BC)
IF(((CD-DE)*SIN(ALPH(I1,K)))>.0) THEN
C=.0
ELSE
C=(CD-DE)*SIN(ALPH(I1,K))
ENDIF
IF(((EF-FG)*COS(ALPH(I1,K)))>.0) THEN
E=.0
ELSE
E=(EF-FG)*COS(ALPH(I1,K))
ENDIF

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      RUA=(VE2-VE1)/700.

      ABCD1=TKB(I1,K)*(A+C+E)*1.50
      RUAN=TKB(I1,K)*RUA*0.05
      ABCD2=ABCD1*TDDPC(L,JST(I1),I1)
      ABCD3=ABCD1*FFV(L,JST(I1),I1)
C      ABC=ABC+ABCD2*SIN(ALPH(I1,K))+RUAN
      ABC=ABC+RUAN
      BCA=BCA+ABCD2*COS(ALPH(I1,K))
      CAB=CAB+ABCD3*RCC(I1)
      FO(I1,K)=FO(I1,K)+ABCD1
38      CONTINUE
      AA1(1,L,I1)=AA1(1,L,I1)+0.2*ABC
      BB1(1,L,I1)=BB1(1,L,I1)+(I1-1)*0.05*BCA+0.04*BCA
      TA1(1,L,I1)=TA1(1,L,I1)+CAB

C      * * * * *
C  ----- *   OUTPUT THE ROTOR'S ORBIT   *
C      * * * * *
      IF(I1.EQ.1) RANG1=BC
      IF(I1.EQ.2) RANG2=BC
      IF(I1.EQ.3) RANG3=BC
      IF(I1.EQ.1) XR1=DE
      IF(I1.EQ.2) XR2=DE
      IF(I1.EQ.3) XR3=DE
      IF(I1.EQ.1) YR1=FG
      IF(I1.EQ.2) YR2=FG
      IF(I1.EQ.3) YR3=FG
30      CONTINUE
      RETURN
      END

      SUBROUTINE TINTG (NNCT,DELTAT)
C *****
C *   THIS SUBROUTINE INTEGRATES THE MODAL ACCELERATION INTO VELOCITY *
C *   AND DISPLACEMENT BY MODIFIED EULER METHOD *
C *****
      IMPLICIT REAL(A-H,O-Z)
      COMMON /BLK2/ ISKIP,NSTEP,NCYCLE,NITP,NINT,NPLOT,NORBIT,NTIME,NSTEP
1ED,NINC,NOPT,NT
      COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
10)

      DO 10 I=1,NNCT
      A2(2,I)=A2(1,I)+DELTAT*A1(1,I)
      B2(2,I)=B2(1,I)+DELTAT*B1(1,I)
      A3(2,I)=A3(1,I)+DELTAT*0.50*(A2(1,I)+A2(2,I))
10      B3(2,I)=B3(1,I)+DELTAT*0.50*(B2(1,I)+B2(2,I))
      DO 20 I=1,NNCT
      A1(1,I)=A1(2,I)
      A2(1,I)=A2(2,I)
      A3(1,I)=A3(2,I)
      B1(1,I)=B1(2,I)
      B2(1,I)=B2(2,I)
20      B3(1,I)=B3(2,I)
      RETURN
      END

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      SUBROUTINE TBETA (NNCT,DELTAT,NSTA,TIME)
C *****
C * THIS SUBROUTINE INTEGRATES THE MODAL ACCELERATIONS INTO MODAL *
C * VELOCITY AND DISPLACEMENT BY NEWMARK BETA METHOD *
C *****
      IMPLICIT REAL(A-H,O-Z)
      DIMENSION STORE(21,40)
      COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10
1      ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
      COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1      ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
      COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1      ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
      COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10
1      ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
      COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1      ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)
      COMMON /ADD6/ TOC(16),TOD(16),TOE(16)
      COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
10)
      COMMON /TMU1/ TMUX(10,5),TMUY(10,5),TEXTW(100,5),TDX(100,5)
      COMMON /TD1/ TDDXT(100,5),TDDNT(100,5),TRP(100,5)
      COMMON /TR1/ TRT(100,5),TEM6(100,5),TRO(100,5),TGGO(100,5)
      COMMON /MF1/ LTLFF(10,5),TSFX(10,5),TSFY(10,5),TMFX(10,5)
      COMMON /TU1/ LTLUF(10,5),TUX(10,5),TUY(10,5),TSUX(10,5),TSUY(10,5)
      COMMON /SEU1/ LTLNT(10,5),NTSRUB(5),NTSEU(5),NTFACT(5),ITND(5)
      COMMON /AAB1/ KTR(5),TABSO(5),AA1(2,10,5),AA2(2,10,5),AA3(2,10,5)
      COMMON /BBA1/ BB1(2,10,5),BB2(2,10,5),BB3(2,10,5),TA1(2,10,5)
      COMMON /TKB1/ TA2(2,10,5),TA3(2,10,5),TKB(5,5),ALPH(5,5),RCC(5)
      COMMON /TMB1/ TMBX(10,5),TMBY(10,5),TWMY(10,5),LTLBD(10,5)
      COMMON /TCM1/ TCMX(10,10,5),TCMY(10,10,5),TKMX(10,10,5)
      COMMON /TDO1/ TDOX(10,10,5),TDOY(10,10,5),TEOX(10,10,5)
      COMMON /TD/ TDDPC(10,100,5),TEMX(10,10,5),TEMY(10,10,5)
      COMMON /TW1/ TDMY(10,10,5),TEEYTH(10,100,5),TW(100,5),TWMOD(50,5)
      COMMON /JS/ JST(5)
      COMMON /TOU/ TOUT(5),FORCEZ(5)
      COMMON /SPEED/ TSPEED(5)
      COMMON /LAS/ TTK(100,5),TMFY(10,5),TKMY(10,10,5),TEOY(10,10,5),
1      TDMX(10,10,5)
      COMMON /BOX01/ OMEGS(40),BX1(40,200,6),LBLBT(10,5),NMBB,NODEB
      COMMON /BLK58/ ZF(10,5),ZFV(10,100,5)
      COMMON /BOX02/OA1(2,40),OA2(2,40),OA3(2,40),OB1(2,40),
1      OB2(2,40),OB3(2,40),JNODE(20),FXFXM(40),FYFYM(20),FZFZM(20)
      COMMON /BOX04/OZ1(2,20),OZ2(2,20),OZ3(2,20),AZ1(2,10,5)
1      ,AZ2(2,10,5),AZ3(2,10,5),TBRFZ(10,5),TOA(16),TOB(16),TOZ(16)
      COMMON /BOX08/ NPT,NPTNO(16)
      DO 100 I1=1,NSTA
C
C      * * * * *
C ----- * STORE THE PREVIOUS RESULT *
C      * * * * *
      DO 10 I=1,NNCT
      STORE(1,I)=AA1(1,I,I1)
      STORE(2,I)=BB1(1,I,I1)
      STORE(3,I)=AA2(1,I,I1)
      STORE(4,I)=BB2(1,I,I1)
      STORE(5,I)=AA3(1,I,I1)
      STORE(6,I)=BB3(1,I,I1)
      STORE(7,I)=TA1(1,I,I1)
      STORE(8,I)=TA2(1,I,I1)

```

```

        STORE(9,I)=TA3(1,I,I1)
        STORE(16,I)=AZ1(1,I,I1)
        STORE(17,I)=AZ2(1,I,I1)
10      STORE(18,I)=AZ3(1,I,I1)

C      * * * * *
C ----- * INTEGRATE THE ACC. INTO VEL. & DISP. *
C      * * * * *
        DO 20 I=1,NNCT
        AA2(1,I,I1)=STORE(3,I)+DELTAT*STORE(1,I)
        BB2(1,I,I1)=STORE(4,I)+DELTAT*STORE(2,I)
        AA3(1,I,I1)=STORE(5,I)+.5*DELTAT*(STORE(3,I)+AA2(1,I,I1))
        BB3(1,I,I1)=STORE(6,I)+.5*DELTAT*(STORE(4,I)+BB2(1,I,I1))
        TA2(1,I,I1)=STORE(8,I)+DELTAT*STORE(7,I)
        TA3(1,I,I1)=STORE(9,I)+0.5*DELTAT*(STORE(8,I)+TA2(1,I,I1))
        AZ2(1,I,I1)=STORE(17,I)+DELTAT*STORE(16,I)
20      AZ3(1,I,I1)=STORE(18,I)+0.5*DELTAT*(STORE(17,I)+AZ2(1,I,I1))

C      * * * * *
C ----- * SOLVE THE EQUATION WITH CURRENT MODAL VEL.& DISP. *
C      * * * * *
        CALL TACCEL (NSTA)
        DO 25 IJ=1,NNCT
        AZ1(1,IJ,I1)=TBRFZ(IJ,I1)-ZF(IJ,I1)**2*AZ3(1,IJ,I1)
        DO 725 JJI=1,NNCT
        AZ1(1,IJ,I1)=AZ1(1,IJ,I1)+TEOY(IJ,JJI,I1)*AZ3(1,JJI,I1)
725      CONTINUE
25      CONTINUE

C      * * * * *
C ----- * INTEGRATE THE ACC. OF ROTOR WITH NEWMARK BETA METHOD *
C      * * * * *
        DO 30 I=1,NNCT
        AA2(1,I,I1)=STORE(3,I)+.5*DELTAT*(AA1(1,I,I1)+STORE(1,I))
        BB2(1,I,I1)=STORE(4,I)+.5*DELTAT*(BB1(1,I,I1)+STORE(2,I))
        AA3(1,I,I1)=STORE(5,I)+DELTAT*STORE(3,I)+(.5-BETA)*STORE(1,I)
1        *DELTAT*DELTAT+BETA*DELTAT*DELTAT*AA1(1,I,I1)
        BB3(1,I,I1)=STORE(6,I)+DELTAT*STORE(4,I)+(.5-BETA)*STORE(2,I)
1        *DELTAT*DELTAT+BETA*DELTAT*DELTAT*BB1(1,I,I1)
        TA2(1,I,I1)=STORE(8,I)+0.5*DELTAT*(TA1(1,I,I1)+STORE(7,I))
        TA3(1,I,I1)=STORE(9,I)+DELTAT*STORE(8,I)+(.5-BETA)*STORE(7,I)
1        *DELTAT*DELTAT+BETA*DELTAT*DELTAT*TA1(1,I,I1)
        AZ2(1,I,I1)=STORE(17,I)+0.5*DELTAT*(AZ1(1,I,I1)+STORE(16,I))
        AZ3(1,I,I1)=STORE(18,I)+DELTAT*STORE(17,I)+(.5-BETA)*STORE(16,I)
1        *DELTAT*DELTAT+BETA*DELTAT*DELTAT*AZ1(1,I,I1)
        AA3(2,I,I1)=AA3(1,I,I1)
        BB3(2,I,I1)=BB3(1,I,I1)
        TA3(2,I,I1)=TA3(1,I,I1)
30      AZ3(2,I,I1)=AZ3(1,I,I1)
100     CONTINUE

C      * * * * *
C ----- * INTEGRATE THE ACC. OF BOX WITH NEWMARK BETA METHOD *
C      * * * * *
        DO 12 I =1,NMBB
        STORE(10,I)=OA1(1,I)
        STORE(12,I)=OA2(1,I)
        STORE(14,I)=OA3(1,I)
12      CONTINUE
        DO 14 I=1,NPT

```

```

      TOA(I)=0.0
      TOB(I)=0.0
14    TOZ(I)=0.0
      DO 60 I=1,NMBB
      OA2(1,I)=STORE(12,I)+DELTAT*STORE(10,I)
      OA3(1,I)=STORE(14,I)+.5*DELTAT*(STORE(12,I)+OA2(1,I))

C      * * * * *
C ---- * SOLVE THE MODAL EQUATION OF BOX *
C      * * * * *
      IJ=I
      OA1(1,IJ)=FXFXM(IJ)-OMEGS(IJ)*OA3(1,IJ)-OA2(1,IJ)
1      *OMEGS(IJ)*0.5*0.09401

      OA2(1,I)=STORE(12,I)+.5*DELTAT*(OA1(1,I)+STORE(10,I))
      OA3(1,I)=STORE(14,I)+DELTAT*STORE(12,I)+(.5-BETA)*STORE(10,I)
1      *DELTAT*DELTAT+BETA*DELTAT*DELTAT*OA1(1,I)
      OA3(2,I)=OA3(1,I)
      DO 60 J= 1,NPT
      JJ= NPTNO(J)
      TOA(J)=TOA(J)+OA1(1,I)*BX1(I,JJ,1)
      TOB(J)=TOB(J)+OA1(1,I)*BX1(I,JJ,2)
60    TOZ(J)=TOZ(J)+OA1(1,I)*BX1(I,JJ,3)
      RETURN
      END

```

SUBROUTINE TINC

```

C *****
C * THIS SUBROUTINE TRANSFORMS THE ROTOR INITIAL CONDITIONS INTO *
C * MODAL INITIAL CONDITIONS OF VELOCITIES AND DISPLACEMENTS *
C *****
      IMPLICIT REAL(A-H,O-Z)
      DIMENSION XTH(100), YTH(100), VXTH(100), VYTH(100)
      COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NNCT,N
1UFPT
      COMMON /BLK6/ BOW(100),PBOW(100),XIDC(100),YIDC(100),VXIDC(100),VY
1IDC(100),BXA(100),BYA(100)
      COMMON /BLK9/ DDPC(10,100),EYTH(10,100)
      COMMON /BLK15/ RP(100),RT(100)
      COMMON /BLK19/ DX(100)
      COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
10)
      COMMON /BLK22/ W(100)

      DO 10 I=1,100
      XIDC(I)=XIDC(I)/1000.
      YIDC(I)=YIDC(I)/1000.
      VXIDC(I)=VXIDC(I)/1000.
10    VYIDC(I)=VYIDC(I)/1000.
      TC=(XIDC(2)-XIDC(1))/DX(1)
      TD=(YIDC(2)-YIDC(1))/DX(1)
      TE=(VXIDC(2)-VXIDC(1))/DX(1)
      TF=(VYIDC(2)-VYIDC(1))/DX(1)
      XTH(1)=ATAN(TC)
      YTH(1)=ATAN(TD)
      VXTH(1)=ATAN(TE)
      VYTH(1)=ATAN(TF)
      TC=(XIDC(N)-XIDC(N-1))/DX(N-1)
      TD=(YIDC(N)-YIDC(N-1))/DX(N-1)

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TE=(VXIDC(N)-VXIDC(N-1))/DX(N-1)
TF=(VYIDC(N)-VYIDC(N-1))/DX(N-1)
YTH(N)=ATAN(TD)
XTH(N)=ATAN(TC)
VXTH(N)=ATAN(TE)
VYTH(N)=ATAN(TF)
N1=N-1
DO 20 I=2,N1
TC=(XIDC(I+1)-XIDC(I-1))/(DX(I-1)+DX(I))
TD=(YIDC(I+1)-YIDC(I-1))/(DX(I-1)+DX(I))
TE=(VXIDC(I+1)-VXIDC(I-1))/(DX(I-1)+DX(I))
TF=(VYIDC(I+1)-VYIDC(I-1))/(DX(I-1)+DX(I))
XTH(I)=ATAN(TC)
YTH(I)=ATAN(TD)
VXTH(I)=ATAN(TE)
VYTH(I)=ATAN(TF)
20 CONTINUE
DO 30 I=1,NNCT
A3(1,I)=0.
B3(1,I)=0.
A2(1,I)=0.
B2(1,I)=0.
DO 30 J=1,N
A3(1,I)=A3(1,I)+(DDPC(I,J)*W(J)*XIDC(J)+EEYTH(I,J)*RT(J)*XTH(J))/3
186.4
B3(1,I)=B3(1,I)+(DDPC(I,J)*W(J)*YIDC(J)+EEYTH(I,J)*RT(J)*YTH(J))/3
186.4
A2(1,I)=A2(1,I)+(DDPC(I,J)*W(J)*VXIDC(J)+EEYTH(I,J)*RT(J)*VXTH(J))
1/386.4
30 B2(1,I)=B2(1,I)+(DDPC(I,J)*W(J)*VYIDC(J)+EEYTH(I,J)*RT(J)*VYTH(J))
1/386.4
RETURN
END

SUBROUTINE BNF
C *****
C * THIS SUBROUTINE CALCULATES THE NONLINEAR BEARING FORCES FOR EACH *
C * TIME STEP . THE BEARING USED ARE ASSUMED TO BE SHORT JOURNAL *
C * BEARING 180 DEG. CAVITATED FILM OR WITH 360. DEG FLUID FILM. *
C * THIS CAN ALSO BE USED TO APPROXIMATE STRAIGHT SEAL FORCES. *
C *****
IMPLICIT REAL(A-H,O-Z)
REAL LEN
REAL MFX,MFY
REAL KXX,KYY
COMMON /BLK1/ N,NB,NNLIN,NMB,NF,NU,NS,NBOW,ISTAB,IMODE,ISKU,NNCT,N
1UFPT
COMMON /BLK3/ CRT(10),LLBD(10),LLNB(5),LLNMB(9),LLSK(10),LLNT(10),
1LLUF(10),LLFF(10),LLUT(10),TCRT(10,5)
COMMON /BLK4/
1 SLNMB(9,4,4),CLNMB(9,4,4)
COMMON /BLK8/ MFX(10),MFY(10),MUX(10),MUY(10),MBX(10),MBY(10)
COMMON /BLK9/ DDPC(10,100),EEYTH(10,100)
COMMON /BLK16/ SPEED2,ANGSP,ANGACL,FSPEED
COMMON /BLK18/ AKK(10),TAKK(10,5)
COMMON /BLK20/ A1(2,10),A2(2,10),A3(2,10),B1(2,10),B2(2,10),B3(2,1
10)
COMMON /BLK35/ WMY(10),VIS(5),R(5),LEN(5),C(5),NLB(5)
COMMON /BLK60/ SFX(10),SFY(10)
COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10

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1      ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1      ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1      ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10
1      ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1      ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)

DO 10 I=1,NNCT
MFX(I)=0.
10  MFY(I)=0.
DO 60 I=1,NNLIN
L=LLNB(I)
X=0.
Y=0.
VX=0.
VY=0.
DO 20 J=1,NNCT
X=X+A3(1,J)*DDPC(J,L)
Y=Y+B3(1,J)*DDPC(J,L)
VX=VX+A2(1,J)*DDPC(J,L)
VY=VY+B2(1,J)*DDPC(J,L)
20  CONTINUE
D=X*X+Y*Y
SD=0.
DEU=0.
SD=SQRT(D)
U=X*VX+Y*VY
DU=C(I)*SD*ANGSP
DEU=U/DU
EU=SD/C(I)
IF (EU.LT.1.0) GOTO 25
EU=0.99
25  CONTINUE
PHIDOT=(X*VY-Y*VX)/(ANGSP*D)
PI=3.14159
TEST=(1.-2.*PHIDOT)
SIGN=1.
SIGN1=1.
IF (TEST.LT.0.) SIGN=-1.
IF (DEU.LT.0.) SIGN1=-1.
CS=EU*ABS(TEST)/SQRT(EU*EU*TEST**2+4.*DEU*DEU)
AS=SQRT((1.+EU)/(1.-EU))
IF (ABS(CS).LT.0.0001) GO TO 30
U=SQRT((1.-CS)/(1.+CS))
GO TO 40
30  U=1.
40  CONTINUE
TI1=SIGN*4.*EU*CS**3/((1.-EU*EU*CS*CS)**2)
C1=(1.-EU*EU)
C2=(3.-5.*AS*AS)
C3=(5.-3.*AS*AS)
TA=ATAN(U*(AS*AS-1.)/(AS*(1.+U*U)))
C4=(1.+2.*EU*EU)
CON=PI*C4/(C1**2.5)
CON2=(C2*U*U+C3*AS*AS)/(U*U+AS*AS)**2+(C2+C3*AS*AS*U*U)/(1.+AS*AS*
1U*U)**2
TI2=CON+SIGN1*(2.*C4*TA/(C1**2.5)-U*CON2/(C1**2))

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CON=2./C1**1.5
TI3=CON*(PI/2.+SIGN1*(TA-AS*U*(U*U-AS*AS)/(U*U+AS*AS)**2-AS*U*(1.-
1AS*AS*U*U)/(1.+AS*AS*U*U)**2))
SOM=VIS(I)*ANGSP*2.*R(I)*LEN(I)**3/(8.*C(I)*C(I))
F1=SOM*(EU*TEST*TI1+2.*DEU*TI2)
F2=SOM*(EU*TEST*TI3+2.*DEU*TI1)
FX=-(F1*X+F2*Y)/SD
FY=(F2*X-F1*Y)/SD
ID=NLB(I)
SFX(I)=FX
SFY(I)=FY
FX=FX+TKXX(ID,1)*X+AKK(ID)*X
FY=FY+TKYY(ID,1)*Y+AKK(ID)*Y
DO 50 K=1,NNCT
50 MFX(K)=MFX(K)+FX*DDPC(K,L)
60 MFY(K)=MFY(K)+FY*DDPC(K,L)
CONTINUE
RETURN
END

SUBROUTINE TOR(N,NM,NE,NTYPE)
C *****
C * THIS PROGRAM FOR CALCULATE Z-DIRECTION EIGEN PROBLEM *
C *****
  DIMENSION FFR(10),FV(100,10),TV(100,10),AT(5,5),WF(100,100)
  COMMON /ADD1/ TKXX(10,5),TKXY(10,5),TKXA(10,5),TKXB(10,5),TKXZ(10
1    ,5),TCXX(10,5),TCXY(10,5),TCXA(10,5),TCXB(10,5),TCXZ(10,5)
  COMMON /ADD2/ TKYX(10,5),TKYY(10,5),TKYA(10,5),TKYB(10,5),TKYZ(10
1    ,5),TCYX(10,5),TCYY(10,5),TCYA(10,5),TCYB(10,5),TCYZ(10,5)
  COMMON /ADD3/ TKAX(10,5),TKAY(10,5),TKAA(10,5),TKAB(10,5),TKAZ(10
1    ,5),TCAX(10,5),TCAY(10,5),TCAA(10,5),TCAB(10,5),TCAZ(10,5)
  COMMON /ADD4/ TKBX(10,5),TKBY(10,5),TKBA(10,5),TKBB(10,5),TKBZ(10
1    ,5),TCBX(10,5),TCBY(10,5),TCBA(10,5),TCBB(10,5),TCBZ(10,5)
  COMMON /ADD5/ TKZX(10,5),TKZY(10,5),TKZA(10,5),TKZB(10,5),TKZZ(10
1    ,5),TCZX(10,5),TCZY(10,5),TCZA(10,5),TCZB(10,5),TCZZ(10,5)
  COMMON /BLK51/ GJ(100),WJ(100)
  COMMON /BLK52/ EXTW(100),DX(100),DDXT(100),DDINT(100),RO(100),GGO
1    (100)
  COMMON /BLK54/ FR(10,5),FFV(10,100,5)
  COMMON /BLK58/ ZF(10,5),ZFV(10,100,5)
  COMMON /BLK56/ SP1,SP2,SP3
  COMMON /BLK59/ TK(100),EEO(100)

  PI=3.1415926
  IF (NTYPE.EQ.1) THEN
    DO 10 I=1,N
      GGO(I)=GGO(I)*10000000.0
      GJ(I)=32.0*DX(I)/(PI*GGO(I)*(DDXT(I)**4-DDINT(I)**4))
      WJ(I)=PI*RO(I)*DX(I)*(DDXT(I)**4-DDINT(I)**4)/ 32.0/386.4
      * +EXTW(I)/386.4
10    CONTINUE
    ELSE
      DO 40 I=1,N
        TK(I)=0.0
        EEO(I)=EEO(I)*10000000.0
        GJ(I)= 4.0*DX(I)/(PI*EEO(I)*(DDXT(I)**2-DDINT(I)**2))
        WJ(I)=PI*RO(I)*DX(I)*(DDXT(I)**2-DDINT(I)**2)/ 4.0/386.4
      * +EXTW(I)/386.4
40    CONTINUE
  ENDIF

```

```

        MCY=0
        ST=20.0
        AO1=0.0
200    AO1=AO1+ST
        AO2=AO1+ST
        CALL CR(N,AO1,B1)
        CALL CR(N,AO2,B2)
        IF((B1*B2).LE.0.0) GOTO 30
        GO TO 200
30     MCY=MCY+1
        IF(MCY.GT.NM) GOTO 60
        A1=AO1
        A2=AO2
100    IF(ABS(A1-A2).LT.0.1) GOTO 50
        AA1=A1+0.618*(A2-A1)
        CALL CR(N,AA1,BB)
        IF ((B1*BB).LE.0.0) THEN
            A2=AA1
            B2=BB
        ELSE
            A1=AA1
            B1=BB
        ENDIF
        GOTO 100
50     FR(MCY,NE)=0.5*(A1+A2)
        IF (NTYPE.GT.1) ZF(MCY,NE)=FR(MCY,NE)
        FFR(MCY)=FR(MCY,NE)/2.0/PI
        GOTO 200
60     CONTINUE
        N1=N+1
        DO 110 MM=1,NM
            FV(1,MM)=1.0
            TV(1,MM)=-WJ(1)*FR(MM,NE)**2
            DO 110 JJ=2,N
                TV(JJ,MM)=TV(JJ-1,MM)*(1.0+(TK(JJ)-WJ(JJ)*FR(MM,NE)**2)*GJ(JJ))
                * +FV(JJ-1,MM)*(TK(JJ)-WJ(JJ)*FR(MM,NE)**2)
            FV(JJ,MM)=TV(JJ-1,MM)*GJ(JJ) +FV(JJ-1,MM)
110    CONTINUE
        DO 80 I=1,NM
            CO=0.0
            DO 70 J=1,N
                CO=CO+FV(J,I)**2*WJ(J)
            DO 80 K=1,N
                FFV(I,K,NE)=FV(K,I)/SQRT(CO)
                IF (NTYPE.NE.1) ZFV(I,K,NE)=FFV(I,K,NE)
80     CONTINUE
        DO 23 I=1,N
            DO 23 J=1,NM
23     WF(I,J)=WJ(I)*FFV(J,I,NE)
        DO 27 I=1,NM
            DO 27 J=1,NM
                AT(I,J)=0.0
            DO 27 K=1,N
27     AT(I,J)=AT(I,J)+WF(K,J)*FFV(I,K,NE)
        WRITE(6,1105) ((AT(I,J),J=1,NM),I=1,NM)
1105   FORMAT (3(/2X,3F16.8))
        IF (NTYPE.EQ.1) THEN
            WRITE(6,1101) NE
            DO 150 I=1,NM
                WRITE(6,1102) I, FR(I,NE) , FFR(I)

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        WRITE(6,1103)
        DO 150 J=1,N
150    WRITE(6,1104) J, FV(J,I), FFV(I,J,NE) , TV(J,I)
        ELSE
        WRITE(6,2101) NE
        DO 250 I=1,NM
        WRITE(6,2102) I, ZF(I,NE)
        WRITE(6,2103)
        DO 250 J=1,N
250    WRITE(6,1104) J, FV(J,I), ZFV(I,J,NE) , TV(J,I)
        ENDIF
1109    FORMAT (2X,I5,2F13.5)
2109    FORMAT (2X,I5,F13.5,2E15.8)
1101    FORMAT('**** TORSION FREQUENCY AND ORTHONOMAL MODE ****  NE=',I2)
1102    FORMAT(3X,'I=',I3,30X,'FREQUENCY=',2F10.3)
1103    FORMAT(2X,' J=',14X,'FV(J,I)=' ,12X,'FFV(J,I) ' ,8X,'TV=')
1104    FORMAT(2X,I3,8X,G14.6,8X,F12.6,6X,G12.5)
2101    FORMAT('** Z-DIRECTION FREQUENCY AND ORTHONOMAL MODE **  NE=',I2)
2102    FORMAT(3X,'I=',I3,30X,'FREQUENCY=',F10.3)
2103    FORMAT(2X,' J=',14X,'ZV(J,I)=' ,12X,'ZFV(J,I) ' ,8X,'FZ=')
666    RETURN
    END

```

```

        SUBROUTINE CR(N,OM,A)
C *****
C * THIS IS TO SET BOUNDARY CONDITIONS FOR MATRIX TRANSFORM METHOD *
C *****
        IMPLICIT REAL(A-H,O-Z)
        DIMENSION D(2,2),B(2,2),C(2,2)
        COMMON /BLK51/ GJ(100),WJ(100)
        COMMON /BLK59/ TK(100),E(100)
        C(2,2)=1.0
        B(1,1)=1.0
        B(1,2)=0.0
        B(2,1)=0.0
        B(2,2)=1.0
        DO 20 I=1,N
        C(1,1)=1.0+(TK(I)-WJ(I)*OM**2)*GJ(I)
        C(1,2)=TK(I) -WJ(I)*OM**2
        C(2,1)=1.0*GJ(I)
        D(1,1)=C(1,1)*B(1,1)+C(1,2)*B(2,1)
        D(1,2)=C(1,1)*B(1,2)+C(1,2)*B(2,2)
        D(2,1)=C(2,1)*B(1,1)+C(2,2)*B(2,1)
        D(2,2)=C(2,1)*B(1,2)+C(2,2)*B(2,2)
        B(1,1)=D(1,1)
        B(1,2)=D(1,2)
        B(2,1)=D(2,1)
        B(2,2)=D(2,2)
20    CONTINUE
        IK=2
C    FREE-----FIXED
        IF(IK.EQ.1) A=B(2,2)
C    FREE-----FREE
        IF(IK.EQ.2) A=B(1,2)
C    FIXED-----FIXED
        IF(IK.EQ.3) A=B(2,1)
C    FIXED-----FREE
        IF(IK.EQ.4) A=B(1,1)
        RETURN
    END

```

```

      SUBROUTINE STIFF(KI,NP,XG,XMAX,X1,YK)
C *****
C * THIS SUBROUTINE CALCULATES GEAR STIFFNESS *
C *****
      IMPLICIT REAL(A-H,O-Z)
      COMMON /K123/ X(4,100),Y(4,100)
3    IF(X1.LT.360.0) GO TO 5
      X1=X1-360.0
      GO TO 3
5    IF(X1.GE.0.0) GO TO 10
      X1=X1+360.0
      GO TO 5
10   IF(X1.LE.XMAX) GO TO 20
      X1=X1-XG
      GO TO 10
20   YK=0.0
      IF(X1.LT.X(KI,1)) GO TO 80
      IF(X1.GT.X(KI,NP)) GO TO 90
      DO 50 I=2,NP
        IF((X1.GE.X(KI,(I-1))).AND.(X1.LT.X(KI,I))) THEN
          YK=((Y(KI,I)-Y(KI,(I-1)))/(X(KI,I)-X(KI,(I-1))))*(X1-X(KI,(I-1)))
          *      +Y(KI,(I-1))
          GO TO 60
        ELSE
          CONTINUE
        ENDIF
50   CONTINUE
80   YK=Y(KI,1)
      GO TO 60
90   YK=Y(KI,NP)
60   CONTINUE
      RETURN
      END

```

APPENDIX D
(SAMPLE DATA INPUT FILE)

2	1	1
2		
0.	0.	0.
12	12	
	0.0	0.52
	3.66	0.0
	4.0	4.0

144

[illegible]

0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.43	1.2	0.	0.	0.	30.	0.28	1.2	0.0
0.	0.05	1.2	0.	0.	0.	30.	0.28	1.2	0.0

12 0.00093 0.00093 0.00093 0.00093

12

250.	266000.	150.
0.0	50.	165000.

0

1	1	
30	2 10000.	.1
12	.0001	

GEARBOX VIBRATION TRANSIENT ANALYSIS
TWO BALL BEARINGS PER ROTOR
THE MODAL SHAPES ARE CALCULATED FROM NASTRAN

5	132	6
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115 21

77	19
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10000. 10000.

10000. 10000.

1

22

EIGENVALUE = 2.534798E+08 (FREQ = 2.53391E+03 HZ)

1	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
2	3.448560E-02	8.036783E-01	-2.037600E-02	6.051830E-01	1.011504E-01
3	-9.057784E-02	1.313704E+00	-9.678650E-02	-2.226727E+00	2.114075E-01
4	8.591101E-03	-1.292542E+00	-5.963318E-02	-8.058454E-01	0.000000e+00
5	6.182482E-01	9.871943E-01	9.928733E-02	0.000000e+00	-1.354058E-02
6	8.015627E-02	7.883143E-01	5.760546E-02	3.560397E-02	-9.211429E-01
7	1.072060E-01	1.440649E+00	-2.722757E+00	9.987959E-01	-1.108560E+00
8	2.268902E-01	1.184208E+00	3.067899E-02	0.000000e+00	-1.718315E-01
9	2.268900E-01	1.184208E+00	-3.067893E-02	0.000000e+00	1.718317E-01
10	3.958876E-01	1.115078E+00	3.924147E-02	0.000000e+00	9.989733E-02
11	5.532086E-02	1.061603E+00	-9.897880E-03	7.403004E-02	-1.024205E-02
12	3.696863E-02	1.848590E+00	-3.545241E+00	1.757919E+00	-9.336358E-02
13	3.711739E-02	-1.924138E+00	-2.060046E-02	-1.086465E-01	0.000000e+00
14	-4.449886E-02	1.833056E+00	-1.566558E-01	-2.526589E+00	1.664701E-01
15	-3.394766E-04	8.591717E-02	-1.033443E-01	4.386343E-01	0.000000e+00
16	1.356463E-02	1.535020E+00	-3.529084E-02	7.012681E-01	0.000000e+00
17	-3.066798E-02	1.179114E+00	7.066858E-02	0.000000e+00	-1.112198E-01
18	5.649020E-02	1.218520E+00	5.441920E-02	3.714950E-01	4.565944E-01
19	8.215582E-02	1.615184E+00	1.918431E+00	1.545835E+00	1.075146E+00
20	3.431828E-02	1.916783E+00	3.703643E+00	1.700075E+00	5.140786E-01
21	-3.431851E-02	1.916783E+00	3.703643E+00	1.700074E+00	-5.140787E-01
22	3.958879E-01	1.115078E+00	-3.924141E-02	0.000000e+00	-9.989762E-02
23	-9.176900E-01	1.313436E+00	5.731493E-03	0.000000e+00	1.565854E-01
24	-3.869911E-01	1.242608E+00	6.925583E-03	0.000000e+00	-1.798946E-01
25	6.182488E-01	9.871943E-01	-9.928727E-02	0.000000e+00	1.354064E-02
26	-3.869914E-01	1.242608E+00	-6.925531E-03	0.000000e+00	1.798949E-01
27	-3.066824E-02	1.179114E+00	-7.066852E-02	0.000000e+00	1.112198E-01
28	-9.176906E-01	1.313436E+00	-5.731449E-03	0.000000e+00	-1.565856E-01
29	5.532086E-02	1.061603E+00	9.897918E-03	-7.402998E-02	1.024207E-02
30	-3.696881E-02	1.848590E+00	-3.545239E+00	1.757919E+00	9.336501E-02

31	3.711740E-02	-1.924138E+00	2.060049E-02	1.086464E-01	0.000000e+00
32	4.449878E-02	1.833056E+00	-1.566558E-01	-2.526589E+00	-1.664702E-01
33	1.356463E-02	1.535020E+00	3.529087E-02	-7.012681E-01	0.000000e+00
34	3.393567E-04	8.591628E-02	-1.033443E-01	4.386334E-01	0.000000e+00
35	-1.356476E-02	1.535018E+00	-3.529084E-02	7.012675E-01	0.000000e+00
36	-1.356477E-02	1.535018E+00	3.529086E-02	-7.012675E-01	0.000000e+00
37	4.079561E-02	1.433638E+00	-1.837622E-02	-8.193132E-01	4.576401E-01
38	5.849652E-02	1.776446E+00	9.177673E-02	-2.362490E+00	-3.333355E-01
39	2.569450E-02	2.044185E+00	-1.037416E+00	-3.966680E+00	-3.544267E-01
40	-1.072062E-01	1.440649E+00	-2.722754E+00	9.987965E-01	1.108560E+00
41	-2.569476E-02	2.044185E+00	-1.037417E+00	-3.966680E+00	3.544254E-01
42	-8.215606E-02	1.615184E+00	1.918431E+00	1.545834E+00	-1.075146E+00
43	-5.849678E-02	1.776445E+00	9.177393E-02	-2.362490E+00	3.333362E-01
44	1.841546E-01	1.508387E+00	-1.028981E-01	9.574949E-01	1.810223E-01
45	3.448561E-02	8.036783E-01	2.037602E-02	-6.051831E-01	-1.011504E-01
46	7.742947E-02	1.393884E+00	-7.515335E-02	4.529952E-02	-1.237930E-02
47	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
48	2.098801E-02	1.257155E+00	-2.725329E-02	-1.114506E+00	-1.718097E-01
49	8.015627E-02	7.883143E-01	-5.760538E-02	-3.560395E-02	9.211435E-01
50	2.098801E-02	1.257155E+00	2.725333E-02	1.114506E+00	1.718097E-01
51	5.649020E-02	1.218520E+00	-5.441912E-02	-3.714949E-01	-4.565944E-01
52	7.742947E-02	1.393884E+00	7.515341E-02	-4.529952E-02	1.237932E-02
53	4.079561E-02	1.433638E+00	1.837626E-02	8.193132E-01	-4.576405E-01
54	1.841546E-01	1.508387E+00	1.028982E-01	-9.574949E-01	-1.810223E-01
55	8.591112E-03	-1.292543E+00	5.963321E-02	8.058454E-01	0.000000e+00
56	9.057778E-02	1.313703E+00	-9.678644E-02	-2.226727E+00	-2.114072E-01
57	-3.394727E-04	8.591723E-02	1.033443E-01	-4.386343E-01	0.000000e+00
58	-8.591216E-03	-1.292542E+00	-5.963314E-02	-8.058460E-01	0.000000e+00
59	3.393563E-04	8.591628E-02	1.033443E-01	-4.386334E-01	0.000000e+00
60	-3.711753E-02	-1.924139E+00	-2.060045E-02	-1.086467E-01	0.000000e+00
61	-3.711753E-02	-1.924139E+00	2.060048E-02	1.086466E-01	0.000000e+00
62	-8.591224E-03	-1.292542E+00	5.963318E-02	8.058454E-01	0.000000e+00
63	1.567899E-01	1.891665E+00	-3.028729E-02	2.921868E+00	1.566738E-01
64	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
65	6.237902E-02	2.188473E+00	-2.298496E-02	5.778226E+00	8.495444E-02
66	-8.015639E-02	7.883143E-01	5.760550E-02	3.560406E-02	9.211422E-01
67	-6.237932E-02	2.188473E+00	-2.298500E-02	5.778226E+00	-8.495438E-02
68	-5.649043E-02	1.218521E+00	5.441916E-02	3.714946E-01	-4.565946E-01
69	-1.567902E-01	1.891665E+00	-3.028736E-02	2.921870E+00	-1.566737E-01
70	-4.079584E-02	1.433638E+00	-1.837627E-02	-8.193126E-01	-4.576393E-01
71	-1.841549E-01	1.508387E+00	-1.028981E-01	9.574943E-01	-1.810223E-01
72	6.272137E-02	5.116381E+00	-1.614437E-02	-2.255423E+00	0.000000e+00
73	-9.057784E-02	1.313704E+00	9.678656E-02	2.226727E+00	-2.114075E-01
74	1.826673E-02	-4.585258E+00	-4.996870E-03	-5.363324E+00	0.000000e+00
75	1.072060E-01	1.440649E+00	2.722758E+00	-9.987959E-01	1.108560E+00
76	1.826673E-02	-4.585258E+00	4.996918E-03	5.363322E+00	0.000000e+00
77	8.215582E-02	1.615184E+00	-1.918431E+00	-1.545836E+00	-1.075146E+00
78	6.272137E-02	5.116379E+00	1.614441E-02	2.255423E+00	0.000000e+00
79	5.849652E-02	1.776445E+00	-9.177732E-02	2.362490E+00	3.333356E-01
80	1.567899E-01	1.891665E+00	3.028733E-02	-2.921867E+00	-1.566738E-01
81	-4.449886E-02	1.833056E+00	1.566559E-01	2.526589E+00	-1.664701E-01
82	-3.448569E-02	8.036783E-01	-2.037600E-02	6.051829E-01	-1.011503E-01
83	4.449878E-02	1.833056E+00	1.566558E-01	2.526589E+00	1.664703E-01
84	-5.532101E-02	1.061603E+00	-9.897880E-03	7.402998E-02	1.024200E-02
85	9.057778E-02	1.313703E+00	9.678650E-02	2.226727E+00	2.114071E-01
86	-5.532101E-02	1.061603E+00	9.897910E-03	-7.402992E-02	-1.024202E-02
87	-3.448570E-02	8.036783E-01	2.037602E-02	-6.051829E-01	1.011503E-01
88	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
89	2.529481E-02	1.006064E+01	-6.337638E-04	-2.354571E+00	0.000000e+00
90	-6.182489E-01	9.871943E-01	9.928733E-02	0.000000e+00	1.354124E-02

91	-2.529510E-02	1.006064E+01	-6.337864E-04	-2.354572E+00	0.000000e+00
92	3.066812E-02	1.179114E+00	7.066858E-02	0.000000e+00	1.112196E-01
93	-6.272167E-02	5.116381E+00	-1.614442E-02	-2.255423E+00	0.000000e+00
94	9.176900E-01	1.313436E+00	5.731463E-03	0.000000e+00	-1.565861E-01
95	-7.742977E-02	1.393885E+00	-7.515341E-02	4.529933E-02	1.237920E-02
96	8.211669E-03	-4.628751E+00	1.786326E-03	-8.116509E+00	0.000000e+00
97	3.696863E-02	1.848590E+00	3.545241E+00	-1.757919E+00	9.336299E-02
98	8.211669E-03	-4.628751E+00	-1.786270E-03	8.116509E+00	0.000000e+00
99	3.431828E-02	1.916783E+00	-3.703643E+00	-1.700075E+00	-5.140788E-01
100	2.529481E-02	1.006064E+01	6.338200E-04	2.354571E+00	0.000000e+00
101	2.569450E-02	2.044184E+00	1.037416E+00	3.966680E+00	3.544270E-01
102	6.237902E-02	2.188473E+00	2.298502E-02	-5.778226E+00	-8.495444E-02
103	-3.696881E-02	1.848590E+00	3.545239E+00	-1.757919E+00	-9.336448E-02
104	-3.958892E-01	1.115078E+00	3.924147E-02	0.000000e+00	-9.989703E-02
105	-1.072062E-01	1.440649E+00	2.722754E+00	-9.987959E-01	-1.108560E+00
106	-3.958895E-01	1.115078E+00	-3.924143E-02	0.000000e+00	9.989733E-02
107	-8.015639E-02	7.883143E-01	-5.760542E-02	-3.560405E-02	-9.211429E-01
108	-6.182494E-01	9.871943E-01	-9.928733E-02	0.000000e+00	-1.354130E-02
109	-8.211952E-03	-4.628753E+00	1.786317E-03	-8.116509E+00	0.000000e+00
110	-2.268897E-01	1.184208E+00	3.067898E-02	0.000000e+00	1.718314E-01
111	-1.826702E-02	-4.585258E+00	-4.996892E-03	-5.363324E+00	0.000000e+00
112	3.869923E-01	1.242608E+00	6.925564E-03	0.000000e+00	1.798941E-01
113	-2.098829E-02	1.257155E+00	-2.725331E-02	-1.114506E+00	1.718097E-01
114	-8.211944E-03	-4.628753E+00	-1.786266E-03	8.116509E+00	0.000000e+00
115	-3.431850E-02	1.916783E+00	-3.703643E+00	-1.700073E+00	5.140789E-01
116	-2.529509E-02	1.006064E+01	6.338370E-04	2.354572E+00	0.000000e+00
117	-2.569475E-02	2.044184E+00	1.037417E+00	3.966680E+00	-3.544257E-01
118	-6.237932E-02	2.188473E+00	2.298505E-02	-5.778226E+00	8.495438E-02
119	-8.215606E-02	1.615184E+00	-1.918431E+00	-1.545834E+00	1.075146E+00
120	-2.268895E-01	1.184208E+00	-3.067894E-02	0.000000e+00	-1.718316E-01
121	-5.649043E-02	1.218520E+00	-5.441912E-02	-3.714946E-01	4.565946E-01
122	3.066837E-02	1.179114E+00	-7.066852E-02	0.000000e+00	-1.112195E-01
123	-1.826701E-02	-4.585258E+00	4.996918E-03	5.363323E+00	0.000000e+00
124	3.869926E-01	1.242608E+00	-6.925538E-03	0.000000e+00	-1.798944E-01
125	-2.098828E-02	1.257155E+00	2.725332E-02	1.114506E+00	-1.718097E-01
126	-6.272161E-02	5.116379E+00	1.614444E-02	2.255423E+00	0.000000e+00
127	-5.849674E-02	1.776445E+00	-9.177446E-02	2.362490E+00	-3.333364E-01
128	-1.567902E-01	1.891665E+00	3.028738E-02	-2.921869E+00	1.566737E-01
129	-4.079584E-02	1.433638E+00	1.837628E-02	8.193126E-01	4.576397E-01
130	9.176906E-01	1.313436E+00	-5.731445E-03	0.000000e+00	1.565862E-01
131	-7.742971E-02	1.393884E+00	7.515341E-02	-4.529933E-02	-1.237923E-02
132	-1.841549E-01	1.508387E+00	1.028982E-01	-9.574943E-01	1.810223E-01
EIGENVALUE = 5.525934E+08 (FREQ = 3.74130E+03 HZ)					
1	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
2	-9.017432E-02	3.794850E-01	-1.710561E-02	-3.720020E-01	9.568367E-03
3	2.273129E-02	-3.766249E-02	2.583054E-01	-9.495828E-01	-2.748883E-01
4	-8.189893E-02	-5.354028E+00	1.579300E-01	-6.754655E-01	0.000000e+00
5	3.970646E-01	4.675810E-01	4.292021E-02	0.000000e+00	-6.974553E-01
6	-7.410407E-02	2.617511E-01	3.004587E-02	1.085124E-01	4.095011E-01
7	-4.307524E-02	1.643141E-01	3.107096E+00	-4.490227E-01	3.093104E+00
8	-2.202222E+00	6.436667E-01	1.703527E-02	0.000000e+00	1.850501E+00
9	-2.202222E+00	6.436667E-01	-1.703527E-02	0.000000e+00	-1.850501E+00
10	1.291305E+00	6.182576E-01	1.876486E-02	0.000000e+00	-8.219761E-02
11	-1.110045E-01	6.251503E-01	-8.757446E-03	1.796952E+00	5.086491E-02
12	-1.736602E-02	6.514788E-02	6.862464E+00	-2.427180E+00	1.173689E+00
13	-1.162736E-01	1.550402E+00	5.254602E-02	5.102044E+00	0.000000e+00
14	1.368123E-02	-2.015609E-01	4.928859E-01	-4.920493E-01	-4.003682E-01
15	-3.399730E-02	-8.324932E+00	2.989873E-01	-4.018692E-01	0.000000e+00
16	-4.934616E-02	3.889892E+00	9.955978E-02	8.324385E+00	0.000000e+00
17	1.343695E+00	5.557591E-01	3.739925E-02	0.000000e+00	7.925306E-01

18	-5.877895E-02	4.296376E-01	2.713646E-02	-7.082572E-01	-1.345645E+00
19	-5.334870E-02	3.586955E-01	-2.247919E+00	-1.071558E+00	-1.966455E+00
20	-2.219216E-02	3.074746E-01	-6.960867E+00	-1.900096E+00	-2.339858E+00
21	2.219188E-02	3.074747E-01	-6.960866E+00	-1.900097E+00	2.339859E+00
22	1.291305E+00	6.182576E-01	-1.876486E-02	0.000000E+00	8.219761E-02
23	1.319715E+00	6.236915E-01	4.671562E-02	0.000000E+00	-4.325923E-01
24	5.902687E-01	6.760237E-01	1.957937E-02	0.000000E+00	6.985579E-01
25	3.970646E-01	4.675810E-01	-4.292021E-02	0.000000E+00	6.974553E-01
26	5.902687E-01	6.760237E-01	-1.957937E-02	0.000000E+00	-6.985579E-01
27	1.343695E+00	5.557591E-01	-3.739925E-02	0.000000E+00	-7.925306E-01
28	1.319715E+00	6.236915E-01	-4.671562E-02	0.000000E+00	4.325923E-01
29	-1.110045E-01	6.251503E-01	8.757442E-03	-1.796952E+00	-5.086491E-02
30	1.736566E-02	6.514800E-02	6.862463E+00	-2.427179E+00	-1.173690E+00
31	-1.162736E-01	1.550402E+00	-5.254602E-02	-5.102044E+00	0.000000E+00
32	-1.368161E-02	-2.015607E-01	4.928859E-01	-4.920493E-01	4.003685E-01
33	-4.934616E-02	3.889892E+00	-9.955978E-02	-8.324385E+00	0.000000E+00
34	3.399693E-02	-8.324931E+00	2.989873E-01	-4.018692E-01	0.000000E+00
35	4.934578E-02	3.889892E+00	9.955978E-02	8.324385E+00	0.000000E+00
36	4.934578E-02	3.889892E+00	-9.955978E-02	-8.324385E+00	0.000000E+00
37	-5.116955E-02	5.296052E-01	4.988674E-02	1.224763E+00	-1.500325E-01
38	-4.840098E-02	5.159767E-01	2.774833E+00	2.603818E+00	2.753377E+00
39	-1.936520E-02	5.096145E-01	5.606589E+00	5.781806E+00	6.248997E-01
40	4.307487E-02	1.643143E-01	3.107094E+00	-4.490215E-01	-3.093104E+00
41	1.936511E-02	5.096146E-01	5.606586E+00	5.781805E+00	-6.249012E-01
42	5.334839E-02	3.586957E-01	-2.247916E+00	-1.071558E+00	1.966455E+00
43	4.840085E-02	5.159769E-01	2.774833E+00	2.603817E+00	-2.753375E+00
44	-2.344701E-02	5.683835E-01	1.286226E-01	-1.065287E+00	-1.535243E-01
45	-9.017432E-02	3.794850E-01	1.710561E-02	3.720020E-01	-9.568367E-03
46	-9.843963E-02	6.558044E-01	9.562874E-02	1.053868E+00	-5.399741E-03
47	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
48	-1.333230E-01	6.766802E-01	3.525435E-02	-1.501417E+00	2.900030E-01
49	-7.410407E-02	2.617511E-01	-3.004587E-02	-1.085124E-01	-4.095011E-01
50	-1.333230E-01	6.766802E-01	-3.525435E-02	1.501417E+00	-2.900030E-01
51	-5.877895E-02	4.296376E-01	-2.713646E-02	7.082572E-01	1.345645E+00
52	-9.843963E-02	6.558044E-01	-9.562874E-02	-1.053868E+00	5.399741E-03
53	-5.116955E-02	5.296052E-01	-4.988674E-02	-1.224763E+00	1.500325E-01
54	-2.344701E-02	5.683835E-01	-1.286226E-01	1.065287E+00	1.535243E-01
55	-8.189893E-02	-5.354028E+00	-1.579300E-01	6.754655E-01	0.000000E+00
56	-2.273155E-02	-3.766224E-02	2.583053E-01	-9.495828E-01	2.748878E-01
57	-3.399730E-02	-8.324932E+00	-2.989873E-01	4.018692E-01	0.000000E+00
58	8.189863E-02	-5.354026E+00	1.579299E-01	-6.754660E-01	0.000000E+00
59	3.399693E-02	-8.324931E+00	-2.989873E-01	4.018692E-01	0.000000E+00
60	1.162732E-01	1.550401E+00	5.254599E-02	5.102043E+00	0.000000E+00
61	1.162732E-01	1.550401E+00	-5.254599E-02	-5.102043E+00	0.000000E+00
62	8.189863E-02	-5.354026E+00	-1.579299E-01	6.754660E-01	0.000000E+00
63	-1.363751E-02	6.307822E-01	3.573031E-01	-1.876906E+00	-8.814639E-02
64	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
65	-3.658583E-03	6.635997E-01	5.784764E-01	-4.014360E+00	-5.691849E-01
66	7.410365E-02	2.617513E-01	3.004592E-02	1.085124E-01	-4.095002E-01
67	3.658720E-03	6.635997E-01	5.784764E-01	-4.014359E+00	5.691849E-01
68	5.877860E-02	4.296378E-01	2.713657E-02	-7.082572E-01	1.345644E+00
69	1.363764E-02	6.307822E-01	3.573030E-01	-1.876906E+00	8.814609E-02
70	5.116946E-02	5.296056E-01	4.988680E-02	1.224762E+00	1.500314E-01
71	2.344714E-02	5.683835E-01	1.286226E-01	-1.065286E+00	1.535244E-01
72	-9.362507E-02	3.002094E+00	2.262314E-01	1.076685E+00	0.000000E+00
73	2.273129E-02	-3.766249E-02	-2.583054E-01	9.495828E-01	2.748883E-01
74	-1.221659E-01	-1.131980E+00	7.748860E-02	-3.664337E+00	0.000000E+00
75	-4.307524E-02	1.643141E-01	-3.107096E+00	4.490227E-01	-3.093104E+00
76	-1.221659E-01	-1.131980E+00	-7.748860E-02	3.664337E+00	0.000000E+00
77	-5.334870E-02	3.586955E-01	2.247919E+00	1.071558E+00	1.966455E+00

78	-9.362507E-02	3.002094E+00	-2.262314E-01	-1.076685E+00	0.000000E+00
79	-4.840098E-02	5.159767E-01	-2.774833E+00	-2.603818E+00	-2.753377E+00
80	-1.363751E-02	6.307822E-01	-3.573031E-01	1.876906E+00	8.814639E-02
81	1.368123E-02	-2.015609E-01	-4.928859E-01	4.920493E-01	4.003682E-01
82	9.017402E-02	3.794852E-01	-1.710561E-02	-3.720016E-01	-9.568159E-03
83	-1.368161E-02	-2.015607E-01	-4.928859E-01	4.920493E-01	-4.003685E-01
84	1.110041E-01	6.251503E-01	-8.757442E-03	1.796951E+00	-5.086538E-02
85	-2.273155E-02	-3.766224E-02	-2.583053E-01	9.495828E-01	-2.748878E-01
86	1.110041E-01	6.251503E-01	8.757442E-03	-1.796951E+00	5.086538E-02
87	9.017402E-02	3.794852E-01	1.710561E-02	3.720016E-01	9.568159E-03
88	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
89	-3.936509E-02	3.812664E+00	3.519562E-01	1.776410E+00	0.000000E+00
90	-3.970667E-01	4.675813E-01	4.292027E-02	0.000000E+00	6.974548E-01
91	3.936531E-02	3.812664E+00	3.519562E-01	1.776410E+00	0.000000E+00
92	-1.343696E+00	5.557596E-01	3.739934E-02	0.000000E+00	-7.925306E-01
93	9.362525E-02	3.002092E+00	2.262313E-01	1.076685E+00	0.000000E+00
94	-1.319714E+00	6.236920E-01	4.671568E-02	0.000000E+00	4.325927E-01
95	9.843981E-02	6.558049E-01	9.562874E-02	1.053868E+00	5.399790E-03
96	-5.082608E-02	-1.383284E+00	1.178113E-01	-4.746291E+00	0.000000E+00
97	-1.736602E-02	6.514788E-02	-6.862464E+00	2.427180E+00	-1.173689E+00
98	-5.082608E-02	-1.383284E+00	-1.178113E-01	4.746291E+00	0.000000E+00
99	-2.219216E-02	3.074746E-01	6.960867E+00	1.900096E+00	2.339858E+00
100	-3.936509E-02	3.812664E+00	-3.519562E-01	-1.776410E+00	0.000000E+00
101	-1.936520E-02	5.096145E-01	-5.606589E+00	-5.781806E+00	-6.248997E-01
102	-3.658583E-03	6.635997E-01	-5.784764E-01	4.014360E+00	5.691849E-01
103	1.736566E-02	6.514800E-02	-6.862463E+00	2.427179E+00	1.173690E+00
104	-1.291305E+00	6.182576E-01	1.876487E-02	0.000000E+00	8.219618E-02
105	4.307487E-02	1.643143E-01	-3.107094E+00	4.490215E-01	3.093104E+00
106	-1.291305E+00	6.182576E-01	-1.876487E-02	0.000000E+00	-8.219624E-02
107	7.410365E-02	2.617513E-01	-3.004592E-02	-1.085124E-01	4.095002E-01
108	-3.970667E-01	4.675813E-01	-4.292027E-02	0.000000E+00	-6.974548E-01
109	5.082633E-02	-1.383282E+00	1.178112E-01	-4.746290E+00	0.000000E+00
110	2.202222E+00	6.436672E-01	1.703529E-02	0.000000E+00	-1.850502E+00
111	1.221661E-01	-1.131980E+00	7.748860E-02	-3.664336E+00	0.000000E+00
112	-5.902691E-01	6.760237E-01	1.957938E-02	0.000000E+00	-6.985574E-01
113	1.333232E-01	6.766807E-01	3.525431E-02	-1.501416E+00	-2.900030E-01
114	5.082633E-02	-1.383282E+00	-1.178112E-01	4.746290E+00	0.000000E+00
115	2.219188E-02	3.074747E-01	6.960866E+00	1.900097E+00	-2.339859E+00
116	3.936531E-02	3.812664E+00	-3.519562E-01	-1.776410E+00	0.000000E+00
117	1.936511E-02	5.096146E-01	-5.606586E+00	-5.781805E+00	6.249012E-01
118	3.658720E-03	6.635997E-01	-5.784764E-01	4.014359E+00	-5.691849E-01
119	5.334839E-02	3.586957E-01	2.247916E+00	1.071558E+00	-1.966455E+00
120	2.202222E+00	6.436672E-01	-1.703530E-02	0.000000E+00	1.850502E+00
121	5.877860E-02	4.296378E-01	-2.713657E-02	7.082572E-01	-1.345644E+00
122	-1.343696E+00	5.557596E-01	-3.739934E-02	0.000000E+00	7.925306E-01
123	1.221661E-01	-1.131980E+00	-7.748860E-02	3.664336E+00	0.000000E+00
124	-5.902691E-01	6.760237E-01	-1.957938E-02	0.000000E+00	6.985574E-01
125	1.333232E-01	6.766807E-01	-3.525431E-02	1.501416E+00	2.900030E-01
126	9.362525E-02	3.002092E+00	-2.262313E-01	-1.076685E+00	0.000000E+00
127	4.840085E-02	5.159769E-01	-2.774833E+00	-2.603817E+00	2.753375E+00
128	1.363764E-02	6.307822E-01	-3.573030E-01	1.876906E+00	-8.814609E-02
129	5.116946E-02	5.296056E-01	-4.988680E-02	-1.224762E+00	-1.500314E-01
130	-1.319714E+00	6.236920E-01	-4.671568E-02	0.000000E+00	-4.325927E-01
131	9.843981E-02	6.558049E-01	-9.562874E-02	-1.053868E+00	-5.399790E-03
132	2.344714E-02	5.683835E-01	-1.286226E-01	1.065286E+00	-1.535244E-01
EIGENVALUE = 9.636076E+08 (FREQ = 4.94049E+03 HZ)					
1	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
2	-2.204335E-01	-9.134558E-01	9.786415E-02	-9.671673E-01	3.471567E-01
3	-1.362807E-01	6.042520E-01	6.709260E-02	6.771230E-01	-6.916553E-01
4	-1.433665E-01	1.525908E+00	5.990286E-02	-7.172636E-01	0.000000E+00

5	-2.749668E+00	-8.418170E-01	-7.844156E-02	0.000000e+00	-9.369984E-01
6	-1.725030E-01	-1.501932E-01	-1.134764E-01	-9.142415E-01	1.307213E+00
7	-1.039136E-01	5.266383E-01	-7.977329E-01	-6.287336E-01	-6.875175E-01
8	-2.717091E+00	-1.237710E+00	-2.057067E-02	0.000000e+00	2.514758E+00
9	-2.717091E+00	-1.237710E+00	2.057068E-02	0.000000e+00	-2.514758E+00
10	2.906806E+00	-1.333014E+00	-2.662497E-02	0.000000e+00	-3.088984E+00
11	-1.129961E-01	-1.517645E+00	5.321137E-02	-1.289827E-01	-7.749307E-01
12	-4.161067E-02	8.480288E-01	8.127363E-01	-4.558187E-01	1.901936E+00
13	-9.085095E-02	-1.261820E+00	1.951224E-02	-1.302364E+00	0.000000e+00
14	-6.269652E-02	7.836103E-01	1.301141E-01	-3.710077E-01	1.041508E+00
15	-5.270659E-02	-1.681621E+00	7.291245E-02	-4.685028E-01	0.000000e+00
16	-3.621293E-02	9.436318E-01	2.187749E-02	1.894675E+00	0.000000e+00
17	2.759181E+00	-7.893918E-01	-5.889059E-02	0.000000e+00	7.627276E-01
18	2.168846E-01	-1.752724E-01	-6.729257E-02	1.637128E+00	-1.066288E+00
19	9.218806E-02	4.955928E-01	8.495526E-01	1.691139E+00	4.570588E-01
20	2.205958E-02	8.776253E-01	-7.371554E-01	3.848539E-02	-1.255874E+00
21	-2.205948E-02	8.776249E-01	-7.371586E-01	3.848138E-02	1.255874E+00
22	2.906806E+00	-1.333014E+00	2.662500E-02	0.000000e+00	3.088984E+00
23	-8.377799E-01	-7.221616E-01	-1.345042E-01	0.000000e+00	1.911979E-01
24	1.216837E+00	-1.249653E+00	-3.938779E-02	0.000000e+00	-6.867892E-01
25	-2.749668E+00	-8.418170E-01	7.844156E-02	0.000000e+00	9.369984E-01
26	1.216837E+00	-1.249653E+00	3.938778E-02	0.000000e+00	6.867891E-01
27	2.759181E+00	-7.893919E-01	5.889060E-02	0.000000e+00	-7.627275E-01
28	-8.377799E-01	-7.221616E-01	1.345042E-01	0.000000e+00	-1.911977E-01
29	-1.129961E-01	-1.517645E+00	-5.321134E-02	1.289827E-01	7.749307E-01
30	4.161183E-02	8.480287E-01	8.127404E-01	-4.558236E-01	-1.901937E+00
31	-9.085095E-02	-1.261820E+00	-1.951218E-02	1.302364E+00	0.000000e+00
32	6.269801E-02	7.836105E-01	1.301142E-01	-3.709958E-01	-1.041507E+00
33	-3.621293E-02	9.436318E-01	-2.187740E-02	-1.894675E+00	0.000000e+00
34	5.270847E-02	-1.681604E+00	7.291251E-02	-4.685031E-01	0.000000e+00
35	3.621491E-02	9.436296E-01	2.187751E-02	1.894667E+00	0.000000e+00
36	3.621491E-02	9.436295E-01	-2.187742E-02	-1.894667E+00	0.000000e+00
37	5.765485E-02	-9.727752E-02	-2.158720E-01	-2.389098E+00	-9.922212E-02
38	1.089216E-01	4.881054E-01	-2.885715E-01	-2.457432E+00	3.233907E-01
39	4.408480E-02	8.937230E-01	3.235229E-01	2.770982E-01	7.550275E-02
40	1.039149E-01	5.266376E-01	-7.977383E-01	-6.287332E-01	6.875185E-01
41	-4.408512E-02	8.937224E-01	3.235171E-01	2.771032E-01	-7.550669E-02
42	-9.218830E-02	4.955921E-01	8.495580E-01	1.691151E+00	-4.570600E-01
43	-1.089219E-01	4.881048E-01	-2.885684E-01	-2.457447E+00	-3.233817E-01
44	3.376811E-01	5.112092E-02	-5.255506E-01	2.675913E+00	7.481520E-01
45	-2.204335E-01	-9.134558E-01	-9.786409E-02	9.671673E-01	-3.471567E-01
46	2.265447E-01	-5.583499E-01	-3.988387E-01	-1.765857E+00	-9.035845E-01
47	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
48	4.961613E-01	-1.336038E+00	-1.493480E-01	2.403214E-02	-7.572687E-01
49	-1.725030E-01	-1.501932E-01	1.134764E-01	9.142415E-01	-1.307213E+00
50	4.961613E-01	-1.336038E+00	1.493480E-01	-2.403216E-02	7.572687E-01
51	2.168846E-01	-1.752724E-01	6.729257E-02	-1.637128E+00	1.066288E+00
52	2.265447E-01	-5.583499E-01	3.988387E-01	1.765857E+00	9.035845E-01
53	5.765484E-02	-9.727752E-02	2.158720E-01	2.389098E+00	9.922206E-02
54	3.376811E-01	5.112090E-02	5.255506E-01	-2.675913E+00	-7.481520E-01
55	-1.433665E-01	1.525908E+00	-5.990281E-02	7.172636E-01	0.000000e+00
56	1.362818E-01	6.042512E-01	6.709266E-02	6.771172E-01	6.916546E-01
57	-5.270659E-02	-1.681621E+00	-7.291234E-02	4.685028E-01	0.000000e+00
58	1.433684E-01	1.525901E+00	5.990295E-02	-7.172644E-01	0.000000e+00
59	5.270847E-02	-1.681604E+00	-7.291245E-02	4.685032E-01	0.000000e+00
60	9.085280E-02	-1.261823E+00	1.951225E-02	-1.302364E+00	0.000000e+00
61	9.085280E-02	-1.261823E+00	-1.951218E-02	1.302364E+00	0.000000e+00
62	1.433684E-01	1.525901E+00	-5.990290E-02	7.172645E-01	0.000000e+00
63	3.133246E-01	4.843269E-01	-3.312035E-01	2.101591E+00	-9.552705E-02
64	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00

65	1.271084E-01	8.988257E-01	-1.583145E-01	-5.593210E-01	8.918363E-02
66	1.725045E-01	-1.501938E-01	-1.134769E-01	-9.142451E-01	-1.307220E+00
67	-1.271092E-01	8.988244E-01	-1.583148E-01	-5.593316E-01	-8.918548E-02
68	-2.168853E-01	-1.752732E-01	-6.729227E-02	1.637136E+00	1.066297E+00
69	-3.133250E-01	4.843268E-01	-3.312039E-01	2.101606E+00	9.553254E-02
70	-5.765487E-02	-9.727788E-02	-2.158716E-01	-2.389109E+00	9.921432E-02
71	-3.376811E-01	5.112093E-02	-5.255505E-01	2.675922E+00	-7.481583E-01
72	1.906072E-01	8.540589E-01	-2.395836E-01	-1.565595E+00	0.000000E+00
73	-1.362807E-01	6.042520E-01	-6.709254E-02	-6.771231E-01	6.916553E-01
74	2.460053E-01	2.331265E-01	-9.391183E-02	2.182657E-01	0.000000E+00
75	-1.039136E-01	5.266383E-01	7.977328E-01	6.287338E-01	6.875175E-01
76	2.460053E-01	2.331264E-01	9.391183E-02	-2.182657E-01	0.000000E+00
77	9.218806E-02	4.955928E-01	-8.495526E-01	-1.691139E+00	-4.570587E-01
78	1.906072E-01	8.540590E-01	2.395836E-01	1.565595E+00	0.000000E+00
79	1.089216E-01	4.881054E-01	2.885715E-01	2.457432E+00	-3.233907E-01
80	3.133246E-01	4.843269E-01	3.312035E-01	-2.101591E+00	9.552711E-02
81	-6.269652E-02	7.836103E-01	-1.301140E-01	3.710076E-01	-1.041508E+00
82	2.204356E-01	-9.134572E-01	9.786409E-02	-9.671671E-01	-3.471588E-01
83	6.269801E-02	7.836105E-01	-1.301141E-01	3.709956E-01	1.041507E+00
84	1.129975E-01	-1.517646E+00	5.321137E-02	-1.289803E-01	7.749367E-01
85	1.362818E-01	6.042511E-01	-6.709266E-02	-6.771173E-01	-6.916546E-01
86	1.129975E-01	-1.517646E+00	-5.321134E-02	1.289802E-01	-7.749367E-01
87	2.204356E-01	-9.134572E-01	-9.786409E-02	9.671672E-01	3.471587E-01
88	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
89	7.068789E-02	-9.310511E-01	-1.136358E-01	-7.224898E-01	0.000000E+00
90	2.749687E+00	-8.418180E-01	-7.844180E-02	0.000000E+00	9.370033E-01
91	-7.068890E-02	-9.310786E-01	-1.136360E-01	-7.224833E-01	0.000000E+00
92	-2.759203E+00	-7.893927E-01	-5.889043E-02	0.000000E+00	-7.627320E-01
93	-1.906080E-01	8.540800E-01	-2.395838E-01	-1.565598E+00	0.000000E+00
94	8.377856E-01	-7.221621E-01	-1.345039E-01	0.000000E+00	-1.911936E-01
95	-2.265449E-01	-5.583495E-01	-3.988387E-01	-1.765857E+00	9.035881E-01
96	7.325935E-02	1.771723E-01	-4.523061E-02	1.542386E+00	0.000000E+00
97	-4.161067E-02	8.480288E-01	-8.127363E-01	4.558188E-01	-1.901936E+00
98	7.325935E-02	1.771721E-01	4.523063E-02	-1.542386E+00	0.000000E+00
99	2.205957E-02	8.776253E-01	7.371554E-01	-3.848554E-02	1.255873E+00
100	7.068789E-02	-9.310509E-01	1.136358E-01	7.224900E-01	0.000000E+00
101	4.408479E-02	8.937230E-01	-3.235229E-01	-2.770980E-01	-7.550281E-02
102	1.271084E-01	8.988257E-01	1.583145E-01	5.593209E-01	-8.918375E-02
103	4.161184E-02	8.480287E-01	-8.127404E-01	4.558237E-01	1.901936E+00
104	-2.906821E+00	-1.333015E+00	-2.662504E-02	0.000000E+00	3.089001E+00
105	1.039149E-01	5.266375E-01	7.977382E-01	6.287333E-01	-6.875185E-01
106	-2.906821E+00	-1.333015E+00	2.662506E-02	0.000000E+00	-3.089001E+00
107	1.725045E-01	-1.501938E-01	1.134769E-01	9.142452E-01	1.307220E+00
108	2.749687E+00	-8.418180E-01	7.844180E-02	0.000000E+00	-9.370034E-01
109	-7.326072E-02	1.771917E-01	-4.523069E-02	1.542413E+00	0.000000E+00
110	2.717109E+00	-1.237711E+00	-2.057060E-02	0.000000E+00	-2.514778E+00
111	-2.460069E-01	2.331120E-01	-9.391201E-02	2.182455E-01	0.000000E+00
112	-1.216844E+00	-1.249654E+00	-3.938764E-02	0.000000E+00	6.867919E-01
113	-4.961632E-01	-1.336039E+00	-1.493480E-01	2.402635E-02	7.572713E-01
114	-7.326072E-02	1.771914E-01	4.523071E-02	-1.542413E+00	0.000000E+00
115	-2.205947E-02	8.776249E-01	7.371586E-01	-3.848153E-02	-1.255874E+00
116	-7.068890E-02	-9.310784E-01	1.136360E-01	7.224836E-01	0.000000E+00
117	-4.408511E-02	8.937223E-01	-3.235172E-01	-2.771031E-01	7.550675E-02
118	-1.271092E-01	8.988244E-01	1.583148E-01	5.593314E-01	8.918560E-02
119	-9.218830E-02	4.955921E-01	-8.495578E-01	-1.691151E+00	4.570599E-01
120	2.717109E+00	-1.237711E+00	2.057061E-02	0.000000E+00	2.514778E+00
121	-2.168853E-01	-1.752732E-01	6.729227E-02	-1.637136E+00	-1.066297E+00
122	-2.759203E+00	-7.893927E-01	5.889044E-02	0.000000E+00	7.627319E-01
123	-2.460069E-01	2.331120E-01	9.391201E-02	-2.182456E-01	0.000000E+00
124	-1.216844E+00	-1.249654E+00	3.938764E-02	0.000000E+00	-6.867918E-01

125	-4.961632E-01	-1.336039E+00	1.493480E-01	-2.402637E-02	-7.572713E-01
126	-1.906080E-01	8.540801E-01	2.395838E-01	1.565598E+00	0.000000E+00
127	-1.089219E-01	4.881047E-01	2.885683E-01	2.457447E+00	3.233817E-01
128	-3.133250E-01	4.843268E-01	3.312039E-01	-2.101606E+00	-9.553266E-02
129	-5.765484E-02	-9.727788E-02	2.158716E-01	2.389109E+00	-9.921426E-02
130	8.377856E-01	-7.221621E-01	1.345039E-01	0.000000E+00	1.911935E-01
131	-2.265449E-01	-5.583495E-01	3.988387E-01	1.765857E+00	-9.035882E-01
132	-3.376811E-01	5.112092E-02	5.255505E-01	-2.675922E+00	7.481583E-01

EIGENVALUE = 1.063199E+09 (FREQ = 5.18952E+03 HZ)

1	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
2	-9.451133E-02	-8.471447E-02	3.096843E-03	-1.275939E+00	1.913482E+00
3	-2.277666E-01	2.889384E-01	-1.542409E+00	3.624273E+00	1.413621E+00
4	-1.018422E-01	2.206059E+00	-1.565207E+00	-3.410224E+00	0.000000E+00
5	3.062222E+00	-7.682985E-02	1.582063E+00	0.000000E+00	5.397369E+00
6	6.724251E-01	-2.813478E-01	1.514244E+00	-2.658940E-01	-6.082453E+00
7	4.080747E-01	4.823969E-02	-3.662162E-01	-1.382513E+00	3.924341E+00
8	-6.382443E+00	1.806549E-02	2.735959E+00	0.000000E+00	-2.699039E+00
9	6.382443E+00	-1.806446E-02	2.735959E+00	0.000000E+00	-2.699040E+00
10	-4.615300E+00	-2.599963E-02	1.629264E+00	0.000000E+00	-1.950772E+00
11	-9.658593E-02	-6.737947E-02	1.341182E-02	6.628470E-01	-1.004295E+00
12	1.357515E-01	1.267214E-01	6.682255E-01	-3.087060E+00	-3.398828E+00
13	-4.790399E-02	-3.077598E+00	-1.591409E+00	1.226150E+00	0.000000E+00
14	-1.153558E-01	4.430590E-01	-2.628884E+00	5.613295E+00	-3.761798E+00
15	-4.326220E-02	2.966340E+00	-2.645970E+00	-5.341032E+00	0.000000E+00
16	-1.499858E-02	-4.455307E+00	-2.652623E+00	1.971824E+00	0.000000E+00
17	4.153708E+00	4.432162E-02	2.726606E+00	0.000000E+00	7.167721E+00
18	8.911163E-01	-2.547168E-02	2.683100E+00	2.176843E+00	-6.874997E+00
19	5.923499E-01	-1.944394E-01	1.434947E-01	1.793740E+00	4.028863E+00
20	2.031730E-01	-3.556420E-01	-4.605522E-01	2.941056E+00	-4.662491E+00
21	-2.031731E-01	-3.556419E-01	-4.605462E-01	2.941056E+00	4.662493E+00
22	4.615300E+00	2.600066E-02	1.629263E+00	0.000000E+00	-1.950772E+00
23	2.795911E+00	2.049360E-01	2.676813E+00	0.000000E+00	5.161032E+00
24	-4.209488E+00	5.668565E-02	2.678936E+00	0.000000E+00	-1.934254E+00
25	-3.062223E+00	7.683051E-02	1.582063E+00	0.000000E+00	5.397369E+00
26	4.209488E+00	-5.668460E-02	2.678936E+00	0.000000E+00	-1.934254E+00
27	-4.153708E+00	-4.432087E-02	2.726606E+00	0.000000E+00	7.167721E+00
28	-2.795911E+00	-2.049353E-01	2.676813E+00	0.000000E+00	5.161032E+00
29	9.658569E-02	6.738049E-02	1.341186E-02	6.628470E-01	-1.004295E+00
30	-1.357517E-01	1.267214E-01	6.682259E-01	-3.087057E+00	3.398826E+00
31	4.790386E-02	3.077598E+00	-1.591409E+00	1.226150E+00	0.000000E+00
32	1.153558E-01	4.430590E-01	-2.628884E+00	5.613295E+00	3.761798E+00
33	1.499853E-02	4.455307E+00	-2.652623E+00	1.971825E+00	0.000000E+00
34	4.326217E-02	2.966342E+00	-2.645970E+00	-5.341031E+00	0.000000E+00
35	1.499856E-02	-4.455307E+00	-2.652623E+00	1.971823E+00	0.000000E+00
36	-1.499851E-02	4.455307E+00	-2.652623E+00	1.971824E+00	0.000000E+00
37	2.380384E-01	4.330818E-01	2.631824E+00	-2.313739E+00	-5.920299E+00
38	1.202772E-01	-3.615993E-01	-1.036809E+00	-2.438682E+00	3.164447E+00
39	3.105013E-02	-7.878942E-01	5.431327E-01	-2.748061E+00	-2.530603E+00
40	-4.080749E-01	4.823974E-02	-3.662177E-01	-1.382515E+00	-3.924339E+00
41	-3.105013E-02	-7.878942E-01	5.431339E-01	-2.748065E+00	2.530602E+00
42	-5.923499E-01	-1.944392E-01	1.434904E-01	1.793739E+00	-4.028865E+00
43	-1.202772E-01	-3.615991E-01	-1.036811E+00	-2.438679E+00	-3.164445E+00
44	-1.231256E+00	6.731454E-01	1.455760E+00	6.244908E-01	-3.520948E+00
45	9.451121E-02	8.471519E-02	3.096922E-03	-1.275940E+00	1.913482E+00
46	-5.769991E-01	2.839333E-01	1.479120E+00	-5.534750E-01	2.154360E+00
47	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
48	-2.441611E-01	6.599402E-02	1.488646E+00	-5.853536E-02	-1.142261E+00
49	-6.724251E-01	2.813480E-01	1.514244E+00	-2.658937E-01	-6.082453E+00
50	2.441612E-01	-6.599301E-02	1.488646E+00	-5.853549E-02	-1.142261E+00
51	-8.911163E-01	2.547195E-02	2.683100E+00	2.176843E+00	-6.874997E+00

52	5.769987E-01	-2.839326E-01	1.479120E+00	-5.534750E-01	2.154361E+00
53	-2.380387E-01	-4.330815E-01	2.631824E+00	-2.313739E+00	-5.920299E+00
54	1.231256E+00	-6.731454E-01	1.455760E+00	6.244904E-01	-3.520949E+00
55	1.018422E-01	-2.206059E+00	-1.565207E+00	-3.410224E+00	0.000000e+00
56	2.277665E-01	2.889384E-01	-1.542409E+00	3.624273E+00	-1.413620E+00
57	4.326220E-02	-2.966340E+00	-2.645970E+00	-5.341032E+00	0.000000e+00
58	1.018422E-01	2.206058E+00	-1.565207E+00	-3.410224E+00	0.000000e+00
59	-4.326214E-02	-2.966342E+00	-2.645970E+00	-5.341031E+00	0.000000e+00
60	4.790397E-02	-3.077598E+00	-1.591409E+00	1.226151E+00	0.000000e+00
61	-4.790383E-02	3.077598E+00	-1.591409E+00	1.226151E+00	0.000000e+00
62	-1.018421E-01	-2.206058E+00	-1.565207E+00	-3.410224E+00	0.000000e+00
63	-1.002457E+00	-3.775417E-01	-7.004800E-01	1.312627E+00	1.830906E+00
64	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
65	-3.876578E-01	-9.294272E-01	-2.182199E+00	9.483725E-02	-3.737156E+00
66	-6.724251E-01	-2.813478E-01	1.514244E+00	-2.658920E-01	6.082452E+00
67	3.876581E-01	-9.294268E-01	-2.182199E+00	9.483778E-02	3.737156E+00
68	-8.911163E-01	-2.547169E-02	2.683100E+00	2.176842E+00	6.874998E+00
69	1.002457E+00	-3.775414E-01	-7.004787E-01	1.312627E+00	-1.830903E+00
70	-2.380384E-01	4.330818E-01	2.631824E+00	-2.313737E+00	5.920299E+00
71	1.231256E+00	6.731454E-01	1.455761E+00	6.244887E-01	3.520946E+00
72	-4.797553E-01	-7.453079E-01	-6.739606E-01	-8.871293E-02	0.000000e+00
73	2.277667E-01	-2.889388E-01	-1.542409E+00	3.624273E+00	1.413621E+00
74	-1.609535E-01	2.367033E-02	-6.550288E-01	3.305750E-01	0.000000e+00
75	-4.080747E-01	-4.824009E-02	-3.662161E-01	-1.382513E+00	3.924342E+00
76	1.609536E-01	-2.367052E-02	-6.550288E-01	3.305750E-01	0.000000e+00
77	-5.923499E-01	1.944390E-01	1.434943E-01	1.793739E+00	4.028863E+00
78	4.797553E-01	7.453079E-01	-6.739606E-01	-8.871293E-02	0.000000e+00
79	-1.202773E-01	3.615990E-01	-1.036809E+00	-2.438681E+00	3.164448E+00
80	1.002456E+00	3.775414E-01	-7.004800E-01	1.312626E+00	1.830907E+00
81	1.153558E-01	-4.430597E-01	-2.628885E+00	5.613294E+00	-3.761799E+00
82	9.451127E-02	-8.471453E-02	3.096768E-03	-1.275939E+00	-1.913482E+00
83	-1.153558E-01	-4.430598E-01	-2.628884E+00	5.613294E+00	3.761799E+00
84	9.658587E-02	-6.737947E-02	1.341170E-02	6.628466E-01	1.004295E+00
85	-2.277666E-01	-2.889388E-01	-1.542409E+00	3.624272E+00	-1.413621E+00
86	-9.658563E-02	6.738055E-02	1.341174E-02	6.628466E-01	1.004295E+00
87	-9.451115E-02	8.471525E-02	3.096847E-03	-1.275939E+00	-1.913482E+00
88	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
89	-1.849937E-01	-1.230235E+00	-2.162570E+00	1.643085E+00	0.000000e+00
90	-3.062223E+00	-7.682991E-02	1.582063E+00	0.000000e+00	-5.397368E+00
91	1.849939E-01	-1.230234E+00	-2.162570E+00	1.643084E+00	0.000000e+00
92	-4.153708E+00	4.432159E-02	2.726606E+00	0.000000e+00	-7.167722E+00
93	4.797553E-01	-7.453071E-01	-6.739597E-01	-8.871388E-02	0.000000e+00
94	-2.795912E+00	2.049360E-01	2.676813E+00	0.000000e+00	-5.161032E+00
95	5.769991E-01	2.839333E-01	1.479120E+00	-5.534754E-01	-2.154359E+00
96	-5.821772E-02	1.723785E+00	-2.134948E+00	-6.396148E-01	0.000000e+00
97	-1.357515E-01	-1.267222E-01	6.682255E-01	-3.087059E+00	-3.398829E+00
98	5.821774E-02	-1.723785E+00	-2.134948E+00	-6.396143E-01	0.000000e+00
99	-2.031730E-01	3.556412E-01	-4.605522E-01	2.941055E+00	-4.662492E+00
100	1.849937E-01	1.230235E+00	-2.162570E+00	1.643084E+00	0.000000e+00
101	-3.105019E-02	7.878933E-01	5.431327E-01	-2.748060E+00	-2.530604E+00
102	3.876576E-01	9.294263E-01	-2.182199E+00	9.483647E-02	-3.737157E+00
103	1.357516E-01	-1.267222E-01	6.682255E-01	-3.087056E+00	3.398827E+00
104	4.615300E+00	-2.599966E-02	1.629263E+00	0.000000e+00	1.950771E+00
105	4.080749E-01	-4.824012E-02	-3.662177E-01	-1.382514E+00	-3.924339E+00
106	-4.615299E+00	2.600069E-02	1.629263E+00	0.000000e+00	1.950771E+00
107	6.724251E-01	2.813480E-01	1.514244E+00	-2.658917E-01	6.082452E+00
108	3.062224E+00	7.683057E-02	1.582063E+00	0.000000e+00	-5.397368E+00
109	5.821777E-02	1.723784E+00	-2.134948E+00	-6.396143E-01	0.000000e+00
110	6.382445E+00	1.806548E-02	2.735958E+00	0.000000e+00	2.699040E+00
111	1.609535E-01	2.366930E-02	-6.550274E-01	3.305752E-01	0.000000e+00

112	4.209487E+00	5.668565E-02	2.678936E+00	0.000000E+00	1.934253E+00
113	2.441610E-01	6.599396E-02	1.488646E+00	-5.853504E-02	1.142261E+00
114	-5.821780E-02	-1.723784E+00	-2.134948E+00	-6.396143E-01	0.000000E+00
115	2.031731E-01	3.556411E-01	-4.605462E-01	2.941055E+00	4.662493E+00
116	-1.849939E-01	1.230234E+00	-2.162570E+00	1.643083E+00	0.000000E+00
117	3.105019E-02	7.878933E-01	5.431339E-01	-2.748063E+00	2.530604E+00
118	-3.876580E-01	9.294263E-01	-2.182199E+00	9.483707E-02	3.737157E+00
119	5.923499E-01	1.944389E-01	1.434901E-01	1.793738E+00	-4.028866E+00
120	-6.382445E+00	-1.806445E-02	2.735958E+00	0.000000E+00	2.699041E+00
121	8.911163E-01	2.547196E-02	2.683099E+00	2.176841E+00	6.874999E+00
122	4.153708E+00	-4.432085E-02	2.726606E+00	0.000000E+00	-7.167722E+00
123	-1.609536E-01	-2.366949E-02	-6.550274E-01	3.305752E-01	0.000000E+00
124	-4.209487E+00	-5.668460E-02	2.678936E+00	0.000000E+00	1.934254E+00
125	-2.441611E-01	-6.599301E-02	1.488646E+00	-5.853517E-02	1.142261E+00
126	-4.797553E-01	7.453071E-01	-6.739597E-01	-8.871382E-02	0.000000E+00
127	1.202773E-01	3.615987E-01	-1.036811E+00	-2.438678E+00	-3.164446E+00
128	-1.002456E+00	3.775410E-01	-7.004787E-01	1.312627E+00	-1.830904E+00
129	2.380386E-01	-4.330815E-01	2.631824E+00	-2.313737E+00	5.920299E+00
130	2.795912E+00	-2.049353E-01	2.676812E+00	0.000000E+00	-5.161032E+00
131	-5.769987E-01	-2.839326E-01	1.479120E+00	-5.534754E-01	-2.154360E+00
132	-1.231256E+00	-6.731454E-01	1.455760E+00	6.244887E-01	3.520947E+00

EIGENVALUE = 1.542988E+09 (FREQ = 6.25175E+03 HZ)

1	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00	0.000000E+00
2	4.590805E-01	-3.272731E-01	-1.313581E-01	-3.265678E+00	-7.956802E-01
3	2.040555E-01	7.161067E-01	7.191497E-02	2.607099E+00	-6.243586E+00
4	2.712965E-01	2.856947E+00	1.851650E-01	-5.456234E+00	0.000000E+00
5	2.647571E+00	-2.571492E-01	-5.264793E-01	0.000000E+00	-2.428569E-01
6	4.339200E-01	-4.220100E-02	-3.743654E-01	1.309581E+00	1.092058E+00
7	3.142332E-01	3.312021E-01	9.476547E-01	6.201724E-01	-4.433858E+00
8	-3.654985E+00	-1.464982E-01	-9.227796E-01	0.000000E+00	-1.598598E+00
9	3.654985E+00	1.464982E-01	-9.227796E-01	0.000000E+00	-1.598598E+00
10	7.893673E-01	-1.841950E-01	-5.727791E-01	0.000000E+00	1.933828E+00
11	2.489810E-01	-3.482481E-01	-2.520546E-01	9.744532E-01	-6.296736E-02
12	9.407467E-02	1.614960E-02	-7.354807E-01	8.314003E-01	5.757459E+00
13	1.340160E-01	-8.111287E+00	2.747808E-01	3.877952E+00	0.000000E+00
14	1.276436E-01	-1.707510E-02	6.482824E-01	-2.196457E+00	9.779965E+00
15	8.699143E-02	-1.702477E+00	6.866251E-01	2.725915E+00	0.000000E+00
16	3.863589E-02	4.375741E+00	7.360634E-01	-1.735952E+00	0.000000E+00
17	1.905424E+00	-2.796497E-01	-8.956088E-01	0.000000E+00	3.011215E+00
18	9.190781E-01	-1.870955E-01	-8.362907E-01	-3.131558E+00	-5.172221E-01
19	5.533018E-01	1.538521E-03	1.539549E+00	-1.413861E+00	-8.053227E-01
20	1.738380E-01	-1.338020E-01	-4.395337E-01	-4.497837E-01	3.379663E-01
21	-1.738344E-01	-1.338034E-01	-4.395267E-01	-4.497721E-01	-3.379613E-01
22	-7.893673E-01	1.841950E-01	-5.727791E-01	0.000000E+00	1.933828E+00
23	2.248714E+00	-3.794388E-01	-7.702167E-01	0.000000E+00	2.839219E+00
24	-3.751226E+00	-1.813316E-01	-8.336855E-01	0.000000E+00	-1.620147E+00
25	-2.647571E+00	2.571492E-01	-5.264793E-01	0.000000E+00	-2.428569E-01
26	3.751226E+00	1.813316E-01	-8.336855E-01	0.000000E+00	-1.620147E+00
27	-1.905424E+00	2.796497E-01	-8.956088E-01	0.000000E+00	3.011215E+00
28	-2.248714E+00	3.794388E-01	-7.702167E-01	0.000000E+00	2.839219E+00
29	-2.489810E-01	3.482481E-01	-2.520546E-01	9.744532E-01	-6.296736E-02
30	-9.407103E-02	1.614792E-02	-7.355083E-01	8.314034E-01	-5.757458E+00
31	-1.340160E-01	8.111287E+00	2.747808E-01	3.877952E+00	0.000000E+00
32	-1.276395E-01	-1.707726E-02	6.482837E-01	-2.196479E+00	-9.779966E+00
33	-3.863590E-02	-4.375741E+00	7.360634E-01	-1.735952E+00	0.000000E+00
34	-8.698910E-02	-1.702480E+00	6.866266E-01	2.725936E+00	0.000000E+00
35	-3.863514E-02	4.375768E+00	7.360650E-01	-1.735967E+00	0.000000E+00
36	3.863513E-02	-4.375768E+00	7.360650E-01	-1.735967E+00	0.000000E+00
37	8.172329E-01	-3.306239E-01	-6.634548E-01	3.861403E+00	2.962852E-01
38	5.007378E-01	-2.552581E-01	1.471487E+00	1.536960E+00	-2.500759E+00

39	1.681758E-01	-3.483433E-01	-2.471471E-01	3.589401E-01	3.052584E+00
40	-3.142300E-01	3.311992E-01	9.476887E-01	6.201531E-01	4.433873E+00
41	-1.681724E-01	-3.483449E-01	-2.471702E-01	3.589203E-01	-3.052586E+00
42	-5.532988E-01	1.535898E-03	1.539539E+00	-1.413852E+00	8.052989E-01
43	-5.007344E-01	-2.552607E-01	1.471513E+00	1.536956E+00	2.500772E+00
44	1.389135E-01	-3.968479E-01	-3.026651E-01	-2.210135E+00	4.217731E+00
45	-4.590805E-01	3.272731E-01	-1.313581E-01	-3.265678E+00	-7.956802E-01
46	-3.469369E-01	-5.501581E-01	-3.774725E-01	-3.968828E-01	-3.075078E-01
47	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
48	-1.488602E-01	-2.730262E-01	-3.640329E-01	-8.270526E-02	-4.058779E-02
49	-4.339200E-01	4.220100E-02	-3.743654E-01	1.309581E+00	1.092058E+00
50	1.488602E-01	2.730262E-01	-3.640329E-01	-8.270532E-02	-4.058779E-02
51	-9.190781E-01	1.870955E-01	-8.362907E-01	-3.131558E+00	-5.172221E-01
52	3.469369E-01	5.501581E-01	-3.774725E-01	-3.968828E-01	-3.075078E-01
53	-8.172329E-01	3.306239E-01	-6.634548E-01	3.861403E+00	2.962852E-01
54	-1.389135E-01	3.968479E-01	-3.026651E-01	-2.210135E+00	4.217731E+00
55	-2.712966E-01	-2.856947E+00	1.851650E-01	-5.456234E+00	0.000000e+00
56	-2.040533E-01	7.161030E-01	7.191968E-02	2.607108E+00	6.243588E+00
57	-8.699143E-02	1.702477E+00	6.866251E-01	2.725915E+00	0.000000e+00
58	-2.712946E-01	2.856923E+00	1.851691E-01	-5.456229E+00	0.000000e+00
59	8.698910E-02	1.702480E+00	6.866266E-01	2.725936E+00	0.000000e+00
60	-1.340154E-01	-8.111278E+00	2.747845E-01	3.877957E+00	0.000000e+00
61	1.340154E-01	8.111278E+00	2.747845E-01	3.877957E+00	0.000000e+00
62	2.712946E-01	-2.856923E+00	1.851691E-01	-5.456229E+00	0.000000e+00
63	1.771163E-01	-2.916673E-01	9.157900E-03	-2.668100E+00	-6.406188E+00
64	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
65	7.165337E-02	-4.530604E-01	2.361302E-01	1.199482E+00	7.835309E+00
66	-4.339179E-01	-4.220150E-02	-3.743649E-01	1.309566E+00	-1.092062E+00
67	-7.165170E-02	-4.530621E-01	2.361264E-01	1.199508E+00	-7.835319E+00
68	-9.190764E-01	-1.870963E-01	-8.362935E-01	-3.131547E+00	5.172588E-01
69	-1.771134E-01	-2.916697E-01	9.153761E-03	-2.668111E+00	6.406200E+00
70	-8.172298E-01	-3.306249E-01	-6.634564E-01	3.861399E+00	-2.962875E-01
71	-1.389098E-01	-3.968488E-01	-3.026676E-01	-2.210135E+00	-4.217740E+00
72	-1.021579E-01	-8.068653E-01	-6.234315E-02	-1.798972E-01	0.000000e+00
73	-2.040556E-01	-7.161067E-01	7.191497E-02	2.607099E+00	-6.243586E+00
74	-6.737101E-02	-1.697833E+00	-1.331440E-01	1.838033E+00	0.000000e+00
75	-3.142332E-01	-3.312021E-01	9.476547E-01	6.201724E-01	-4.433858E+00
76	6.737101E-02	1.697833E+00	-1.331440E-01	1.838033E+00	0.000000e+00
77	-5.533018E-01	-1.538521E-03	1.539549E+00	-1.413861E+00	-8.053227E-01
78	1.021579E-01	8.068653E-01	-6.234315E-02	-1.798971E-01	0.000000e+00
79	-5.007378E-01	2.552581E-01	1.471487E+00	1.536960E+00	-2.500759E+00
80	-1.771163E-01	2.916673E-01	9.157900E-03	-2.668100E+00	-6.406188E+00
81	-1.276436E-01	1.707510E-02	6.482824E-01	-2.196457E+00	9.779965E+00
82	-4.590790E-01	-3.272741E-01	-1.313568E-01	-3.265676E+00	7.956797E-01
83	1.276395E-01	1.707726E-02	6.482837E-01	-2.196479E+00	-9.779966E+00
84	-2.489808E-01	-3.482487E-01	-2.520528E-01	9.744515E-01	6.296998E-02
85	2.040533E-01	-7.161030E-01	7.191968E-02	2.607108E+00	6.243588E+00
86	2.489808E-01	3.482487E-01	-2.520528E-01	9.744515E-01	6.296998E-02
87	4.590790E-01	3.272741E-01	-1.313568E-01	-3.265676E+00	7.956797E-01
88	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00
89	-1.593731E-02	1.725979E+00	1.806393E-01	-6.609303E-01	0.000000e+00
90	-2.647591E+00	-2.571497E-01	-5.264792E-01	0.000000e+00	2.428544E-01
91	1.593898E-02	1.725978E+00	1.806364E-01	-6.609399E-01	0.000000e+00
92	-1.905444E+00	-2.796503E-01	-8.956113E-01	0.000000e+00	-3.011254E+00
93	1.021596E-01	-8.068604E-01	-6.234740E-02	-1.798891E-01	0.000000e+00
94	-2.248732E+00	-3.794392E-01	-7.702190E-01	0.000000e+00	-2.839220E+00
95	3.469386E-01	-5.501583E-01	-3.774751E-01	-3.968831E-01	3.075162E-01
96	-1.646472E-02	-7.119755E-01	1.152091E-01	-4.596010E-01	0.000000e+00
97	-9.407467E-02	-1.614960E-02	-7.354807E-01	8.314003E-01	5.757459E+00
98	1.646472E-02	7.119756E-01	1.152091E-01	-4.596010E-01	0.000000e+00

99	-1.738380E-01	1.338020E-01	-4.395337E-01	-4.497838E-01	3.379663E-01
100	1.593731E-02	-1.725979E+00	1.806393E-01	-6.609303E-01	0.000000E+00
101	-1.681758E-01	3.483433E-01	-2.471471E-01	3.589401E-01	3.052584E+00
102	-7.165337E-02	4.530604E-01	2.361302E-01	1.199482E+00	7.835309E+00
103	9.407103E-02	-1.614792E-02	-7.355083E-01	8.314034E-01	-5.757458E+00
104	-7.893661E-01	-1.841953E-01	-5.727789E-01	0.000000E+00	-1.933836E+00
105	3.142300E-01	-3.311992E-01	9.476887E-01	6.201531E-01	4.433873E+00
106	7.893661E-01	1.841953E-01	-5.727789E-01	0.000000E+00	-1.933836E+00
107	4.339179E-01	4.220150E-02	-3.743649E-01	1.309566E+00	-1.092062E+00
108	2.647591E+00	2.571497E-01	-5.264792E-01	0.000000E+00	2.428544E-01
109	1.646528E-02	-7.119811E-01	1.152066E-01	-4.595968E-01	0.000000E+00
110	3.655034E+00	-1.464984E-01	-9.227812E-01	0.000000E+00	1.598619E+00
111	6.737131E-02	-1.697830E+00	-1.331480E-01	1.838025E+00	0.000000E+00
112	3.751225E+00	-1.813317E-01	-8.336880E-01	0.000000E+00	1.620139E+00
113	1.488598E-01	-2.730263E-01	-3.640357E-01	-8.270323E-02	4.058736E-02
114	-1.646527E-02	7.119811E-01	1.152066E-01	-4.595968E-01	0.000000E+00
115	1.738344E-01	1.338034E-01	-4.395267E-01	-4.497721E-01	-3.379613E-01
116	-1.593898E-02	-1.725978E+00	1.806364E-01	-6.609399E-01	0.000000E+00
117	1.681724E-01	3.483449E-01	-2.471702E-01	3.589203E-01	-3.052586E+00
118	7.165170E-02	4.530621E-01	2.361264E-01	1.199508E+00	-7.835319E+00
119	5.532988E-01	-1.535898E-03	1.539539E+00	-1.413852E+00	8.052989E-01
120	-3.655034E+00	1.464984E-01	-9.227812E-01	0.000000E+00	1.598619E+00
121	9.190764E-01	1.870963E-01	-8.362935E-01	-3.131547E+00	5.172588E-01
122	1.905444E+00	2.796503E-01	-8.956113E-01	0.000000E+00	-3.011254E+00
123	-6.737131E-02	1.697830E+00	-1.331480E-01	1.838026E+00	0.000000E+00
124	-3.751225E+00	1.813317E-01	-8.336880E-01	0.000000E+00	1.620139E+00
125	-1.488598E-01	2.730263E-01	-3.640357E-01	-8.270317E-02	4.058737E-02
126	-1.021596E-01	8.068604E-01	-6.234740E-02	-1.798891E-01	0.000000E+00
127	5.007344E-01	2.552607E-01	1.471513E+00	1.536956E+00	2.500772E+00
128	1.771134E-01	2.916697E-01	9.153761E-03	-2.668111E+00	6.406200E+00
129	8.172298E-01	3.306249E-01	-6.634564E-01	3.861399E+00	-2.962875E-01
130	2.248732E+00	3.794392E-01	-7.702190E-01	0.000000E+00	-2.839220E+00
131	-3.469386E-01	5.501583E-01	-3.774751E-01	-3.968831E-01	3.075162E-01
132	1.389098E-01	3.968488E-01	-3.026676E-01	-2.210135E+00	-4.217740E+00

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13. ABSTRACT (Maximum 200 words) This report outlines the work performed on global dynamic simulation and noise correlation of gear transmission systems at The University of Akron. The objective of this work is to develop a comprehensive procedure to simulate the dynamics of the gear transmission system coupled with the effects of gear box vibrations. The developed numerical model is benchmarked with results from experimental tests at NASA Lewis Research Center. The modal synthesis approach is used to develop the global transient vibration analysis procedure used in the model. Modal dynamic characteristics of the rotor-gear-bearing system are calculated by the matrix transfer method while those of the gear box are evaluated by the finite element method (NASTRAN). A three-dimensional, axial-lateral coupled bearing model is used to couple the rotor vibrations with the gear box motion. The vibrations between the individual rotor systems are coupled through the nonlinear gear mesh interactions. The global equations of motion are solved in modal coordinates and the transient vibration of the system is evaluated by a variable time-stepping integration scheme. The relationship between housing vibration and resulting noise of the gear transmission system is generated by linear transfer functions using experimental data. A nonlinear relationship of the noise components to the fundamental mesh frequency is developed using the hypercoherence function. The numerically simulated vibrations and predicted noise of the gear transmission system are compared with the experimental results from the gear noise test rig at NASA Lewis Research Center. Results of the comparison indicate that the global dynamic model developed can accurately simulate the dynamics of a gear transmission system.				
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